

1 **How microfracture roughness can be used to**
2 **distinguish between exhumed cracks and in-**
3 **situ flow paths in shales**

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15 Keywords:

16 X-ray micro-tomography; fluid flow; faults; crack growth; Hurst exponent; shale gas

17 **Abstract**

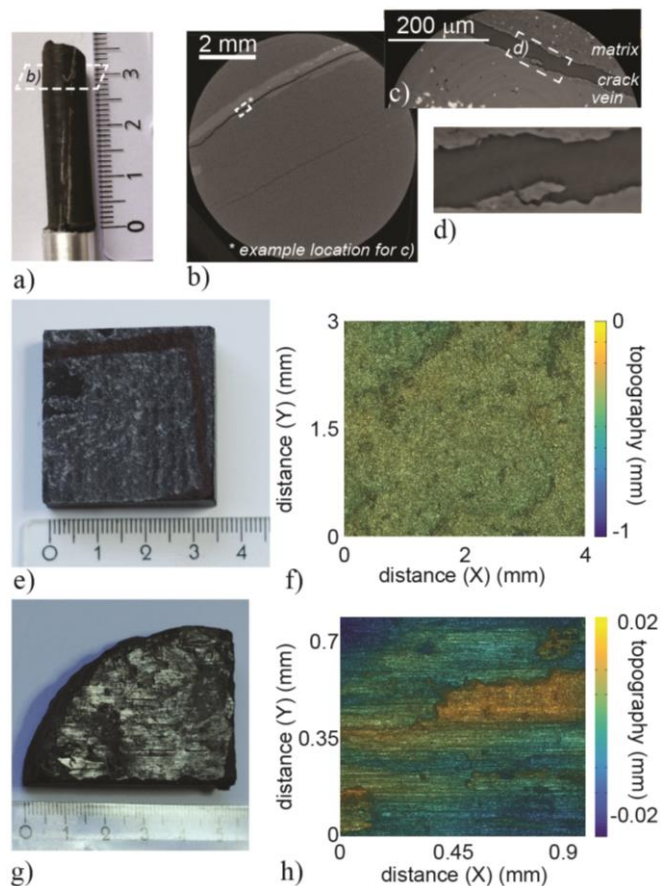
18 Flow through fractures in shales is of importance to many geoengineering purposes. Shales are
19 not only caprocks to hydrocarbon reservoirs and nuclear waste or CO₂ storage sites, but also
20 potential source and reservoir rocks for hydrocarbons. The presence of microfractures in shales
21 controls their permeability and transport properties. Using X-ray micro-tomography and white
22 light interferometry we scanned borehole samples obtained from 4 km depth in the Pomeranian
23 shales in Poland. These samples contain open exhumation/drying cracks as well as intact vein-
24 rock interfaces plus one striated slip surface. At micron resolution and above tensile drying
25 cracks exhibit a power-law roughness with a scaling exponent, called the Hurst exponent H , of
26 0.3. At sub-micron resolution we capture the properties of the clay interface only, with $H = 0.6$.
27 In contrast, the in-situ formed veins and slip surface exhibit $H = 0.4-0.5$, which is deemed
28 representative for in-situ fractures. These results are discussed in relation to the shale
29 microstructure and linear elastic fracture mechanics theory. The data imply that the Hurst
30 roughness exponent can be used as a microstructural criterion to distinguish between exhumation
31 and in-situ fractures, providing a step forward towards the characterization of potential flow
32 paths at depth in shales.

33

34 **1. Introduction**

35 The roughness of natural fault surfaces does not only control many aspects of earthquake
36 mechanics (Scholz, 2002), but is equally of importance for fluid flow through natural and
37 induced fractures (Brown, 1987; Noiriél et al., 2007; Fitts and Peters, 2013). Shales in particular
38 are studied for their importance as caprock to hydrocarbon reservoirs and CO₂ plus nuclear waste
39 storage sites, for which the lack of effective transport pathways is evidently paramount. In
40 contrast, it is the efficiency of transport through existing and induced fractures and faults that
41 controls the primary migration of hydrocarbons and the recovery of shale gas. Fault or fracture
42 roughness is an important control on transmissivity, especially in small aperture cracks (e.g. Fitts
43 and Peters, 2013). Data on roughness of representative fault surfaces in shale rocks is however
44 lacking, mainly because of their fragile nature. Natural fault rocks in these lithologies weather
45 easily unless they are highly cohesive, which may occur when buried deeply, or by experiencing
46 high strain and/or seismic slip. Investigations on natural low displacement faults, mainly on
47 (striated) fault planes in carbonate rocks, have shown that with increasing displacement there is a
48 slight decrease in roughness amplitude (Sagy et al., 2007; Brodsky et al., 2011). However, for
49 total displacements larger than ~10m, common for major continental faults, there are no trends
50 found in roughness data (Candela and Renard, 2012). In this study we investigate low to no
51 displacement faults and fractures found in a shale drill-core. When using drill-core, fractures that
52 contain cement are easily identified as originating in the subsurface, but subsurface fractures are
53 not always cemented. Thus, one of the key challenges is to identify fractures present in-situ
54 compared to those that originate during sample recovery. Correct identification of in-situ
55 fractures will help to determine realistic flow-controlling properties for natural and induced
56 fractures in low-permeability shale formations, such as wall roughness and fracture aperture. It is

57 difficult, if not impossible, to estimate absolute in-situ fracture apertures from borehole samples,
58 therefore our main focus lies on determining the roughness of fracture walls. In the present study,
59 we determine fracture roughness both of veins and decompression fractures of the Pomeranian
60 shales from Poland. Since vein formation occurs at depth, the topography of the vein-rock
61 interface is preserved even when samples are extracted from the subsurface. We use X-ray
62 microtomography and white light interferometry (examples shown in Figure 1) at multiple 2-D
63 pixel and 3-D voxel sizes, ranging from 0.1 to 25 micrometers, with sample sizes between 0.5-
64 7.5 cm. Our data cover spatial scales in the range 0.5 micrometer to 5 centimeters, i.e. five orders
65 of magnitude. These different measurements provide us with information on how scale,
66 resolution, and method affect roughness values in a heterogeneous, fragile rock as shale. The
67 Polish Pomeranian shale has been selected because this formation is prospected for shale gas
68 exploration, even though not all data are yet available in the public domain (Schulz et al., 2010).
69 The core material we obtained originates from a borehole in northern Poland that reached
70 approximately 4 km depth, with a thermal maturity inside the gas window, and a depth that does
71 not exclude economic exploitation (even though currently exploitation at the borehole location is
72 not planned).



73 g) h)

74 Figure 1. Examples of samples plus data. a-d) Sample SQ686.5-SS7 for X-ray microtomography.
 75 Veins and fracture parallel to the bedding. a) Photo. b) Low resolution X-Y slice of raw XCT
 76 data SQ686.5-SS7. Veins and fracture parallel to the bedding. c) Highest resolution X-Y slice of
 77 filtered data, scanned at the synchrotron at the ESRF, Grenoble. The approximate location is
 78 indicated in Figure b. Note that because the scans are made in different locations and at different
 79 resolutions, it is not possible to show exactly the same slice in b) and c). d) Zoom, location
 80 indicated in c), showing the roughness of the vein/air interface and the matrix/air interface. e)
 81 Photo of slab with vein SQ617.15-SS17, analyzed with white light interferometry. f) Example of
 82 white light interferometry data. g) Photo of the shiny slip surface of sample SQ698.0- SS20, also
 83 analyzed with white light interferometry. h) Example of white light interferometry data.

84 The cracks are currently open, but there is no a priori information on opening mode or
 85 mechanism. The storage of the drill core at ambient conditions for several months prior to
 86 characterization was associated with dehydration of the drill core, visible through the
 87 development of the open cracks investigated here. Consequently, it is plausible that these are
 88 related to sample drying, and we thus assume that all the open cracks investigated here are

89 simple mode I fractures. The veins are sealed, cement-filled fractures, where the sealing
 90 presumably occurred at depth. Due to the limitations of the cm-scale core provided, the
 91 maximum length scale is up to multiple centimeters. This means that the fractures in question
 92 here are microfractures from the perspective of engineers and geophysicists, but not for
 93 geologists – for whom the term microfracture indicates a fracture that requires microscopy to
 94 observe.

95 Table 1: Sample details.

Stratigraphy	Lithostratigraphy	Sample code	Analysis method	Resolution / magnification
Silurian - Lower Wenlock Sheinwood	Pelplin Formation	SQ617.15-SS17	WLI	5x & 20x
		SQ629.55-SS16	WLI	5x & 20x
		SQ631.45-SS15	WLI	2.4x to 40x
Silurian - Llandovery	Pasłek Formation	SQ636.5-SS11	XCT	12.7 µm/voxel
	Jantar Member	SQ682.2-SS9	WLI	5x & 20x
		SQ685.65-SS7	XCT	0.16 - 1.7 - 7.8 - 25.7 µm/voxel
		SQ689.3-SS5	XCT	24.5 µm/voxel
Ordovician - Caradocian	Sasino Formation	SQ698.0-SS20 ^{a)}	WLI	2.5x to 100x
		SQ705.3-SS19	WLI, XCT	5x & 20x & 23.5 µm/voxel

96 WLI stands for White Light Interferometer, and XCT for X-ray microtomography.

97 ^{a)} This is the slip surface.

98

99 2. Methods

100 2.1 Sample description

101 The Pomeranian shale is a dark-grey to black rock composed of approximately 50-70% clay
 102 minerals and mica, 20-30% quartz, 1-10% carbonates, 1-10% organic matter, 1-7% pyrite plus
 103 minor amounts of barite, K-feldspar, plagioclase and kaolinite. We had access to a drill-core
 104 from approximately 4 km depth, located on one of the concessions of the Polish Oil & Gas

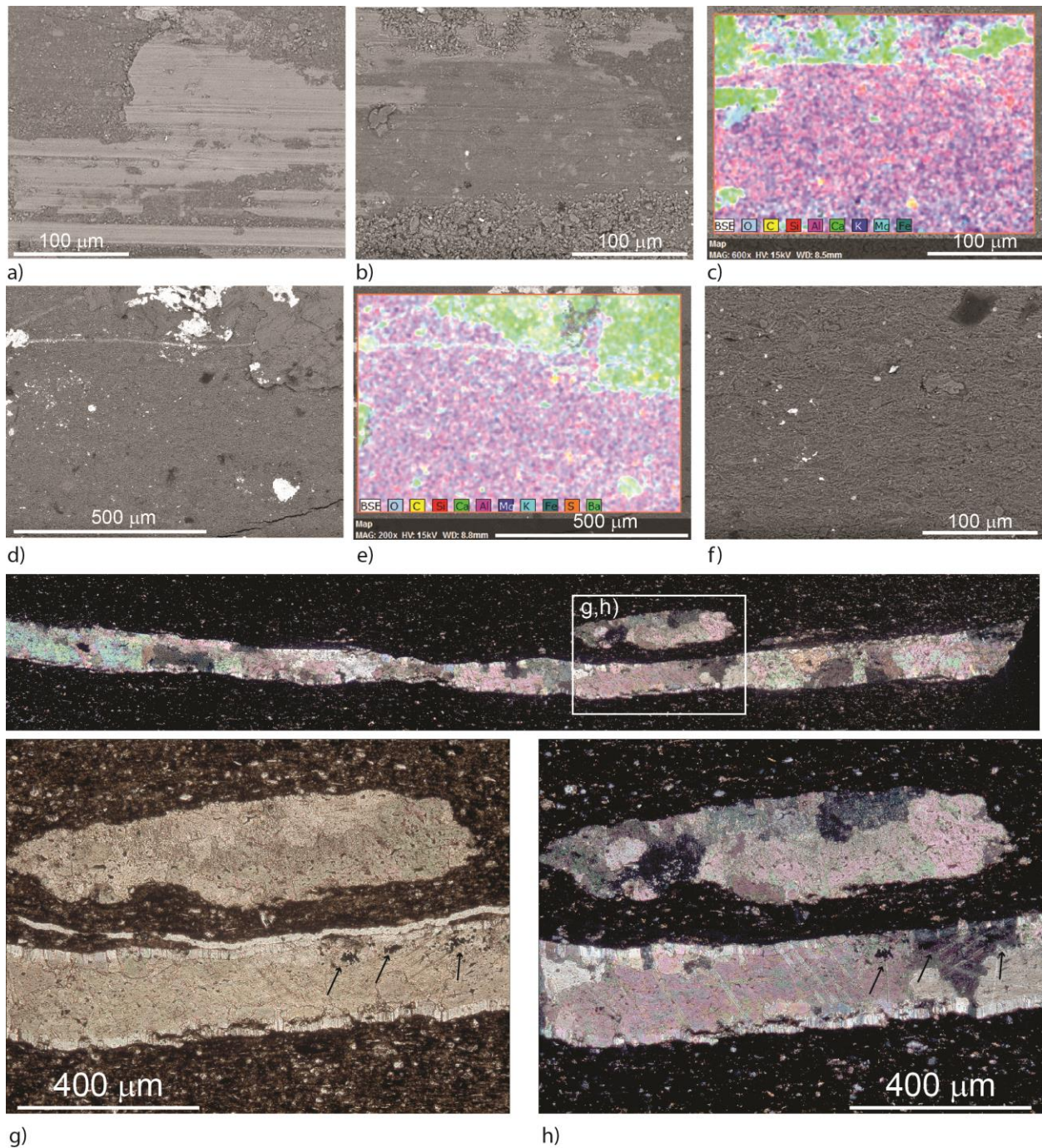
105 Company (PGNiG SA) in northern Poland. We obtained four smaller core samples for 3D X-ray
106 microtomography scans (XCT, Table 1), and five open fracture or vein samples for 2D white
107 light interferometry measurements (WLI, Table 1). Note that even though samples originated
108 from different formations, the composition and structure of the shale was homogeneous
109 throughout the ~30 m long sampling interval. The samples for the tomography scans are 8 mm in
110 diameter, and between 10 and 40 mm long (e.g. Figure 1a). In these cylindrical samples there are
111 several calcite veins present, with a thickness from sub-mm up to 3 mm. These core samples also
112 contain several open cracks, with an aperture up to 2 mm. Due to the fragility of the samples that
113 contain bedding-perpendicular veins, we only obtained tomography cores in which the majority
114 of the veins and cracks in the tomography samples are approximately bedding-parallel.
115 Furthermore, using a white light interferometer, we scanned the surface of five slabs for which
116 the drill core had split, exposing a thin (sub-mm) calcite vein (e.g. Figure 1e, f). For all samples
117 except SQ705.3 the splitting occurred approximately perpendicular to the bedding. In this drill-
118 core we also found one striated, mirror-like slip surface parallel to the bedding, which we also
119 scanned with the white light interferometer (SQ698.0-SS20). All slabs were 35 to 75 mm long
120 and 20 to 45 mm wide. Samples and imaging methods are listed in Table 1.

121 We have imaged two samples, the slip surface of SQ698.0-SS20 and its nearest non-slip
122 neighbour, sample SQ705.3-SS19, with a Hitachi TM3000 (table-top) SEM with EDS capability
123 in electron back-scatter mode (Figure 2a-f). On the slip surface (Figure 2a, b, c) the striations are
124 widespread, though they are more pronounced in the calcite-rich parts than in the clay-rich
125 matrix, and in the clay-rich matrix they are more pronounced than in the silica-rich matrix. The
126 calcite-rich grains are elongated parallel to the striations (Figure 2a). The smooth surface is
127 locally covered by fault gouge that matches the matrix composition, with grain sizes of tens of

128 micrometers (Figure 2c). In the smooth clay-rich matrix, grains are rounded with a maximum
129 length of 1-2 μm , whereas the more silica-rich matrix grains can be slightly coarser, up to 10 μm .
130 There is no visible pore space.

131 The undeformed sample SQ705.3-SS19 exhibited a channel structure exposing the undeformed
132 clay matrix. On the carbonate cover multiple barite crystals are present (Figure 2 d-e) with
133 crystal sizes of roughly 50-500 μm . In the exposed undeformed matrix, the sub-micron clay
134 particles maintain their elongated crystal shape with grain lengths up to tens of micrometers, in
135 contrast to the clay particles on the slip surface of SQ698.0-SS20. Non-clay particles are oriented
136 randomly, and at 600x magnification there is visible pore space (up to 1 μm in size, Figure 2f).

137 We have also imaged a thin section of sample SQ685.65-SS7 using a regular optical microscope
138 (Figure 2g-h). This shows that the veins in this sample consist mainly of calcium carbonate
139 crystals, locally with groups of micron-sized oxides (black polygons in Figure 2g-h, probably
140 barite). The carbonate crystals cover the entire width of the vein and can exhibit lobate grain
141 boundaries. Along the edge of the veins there is also some fibrous calcite. The largest calcite
142 grains exhibit twinning.



143

g)

h)

144 Figure 2. Microstructural observations. a-f) Back scatter electron images from the slip surface
 145 SQ698.0-SS20 (a-c), and the sample SQ705.3-SS19 (d-f) located closest to the slip surface. a)
 146 Close-up of elongated calcite patch, 600x magnification. Striations are omni-present, but more
 147 pronounced in the calcite patch. b) 600x magnification. Clay-rich matrix in the center, with
 148 visible striations and sub-micron grain size. Coarse fault gouge at the bottom. Silica-rich matrix
 149 in the top-left, slightly coarser grained than the clay-rich matrix. c) EDS map of b). d) 200x
 150 magnification. Top edge of the channel structure, with bright barite crystals at the edge, mixed

151 with carbonate. e) EDS image of d). f) 600x magnification. Close-up of the matrix in the channel,
152 with elongated clay particles with random orientation, and visible pore space. g-h) Optical
153 microscope images of the veins in sample SQ685.65-SS7. Note the twinned carbonate crystals.
154 The arrows indicate grouped oxides. g) plane-polarized light. h) cross-polarized light.

155 *2.2 X-ray microtomography imaging*

156 We have scanned four core samples using a laboratory tomograph (Nikon XT H 225 ST), with a
157 beam energy of 180 kV, at voxel sizes of 11 to 26 μm . We also scanned a subvolume of sample
158 SQ685.65 at 7 μm voxel size. A subvolume of this sample has been scanned as well at the
159 beamline ID19 at the European Synchrotron Radiation Facility (ESRF), at two different voxel
160 sizes (1.7 and 0.16 μm), using a beam energy of 40 keV. The possibility to separate two objects
161 in the scans when they are located close to each other is roughly twice the voxel size. The
162 decrease in voxel size of the ESRF scans helps distinguish the cracks and veins with better
163 resolution. At the largest voxel size, the complete samples could be imaged, which allowed for
164 an overview of the entire cm-sized sample. With micron voxel sizes the coarsest individual
165 grains are visible, and at sub-micron size we observe the grains in the matrix, as well as some of
166 the intergranular pore space.

167 The 3D images were processed using the software package AvizoFire© (edition 9), following a
168 new method (described below) to quantitatively determine crack- and vein-geometry and
169 morphology. We isolated crack and vein data of individual features to enable subsequent
170 quantitative analysis of their topography. In order to isolate objects, we traced the matrix-air
171 interface for the cracks, and the vein-matrix interface for the veins. The general procedure for
172 segmenting fractures and veins was to remove the background using a binary mask, after which a
173 non-local-means filter was applied, which is an edge-preserving filter. All samples were
174 processed using the same filter, though the exact parameters were sample-dependent. The details

175 of the filtering procedure are listed in Table 2. Since in the XCT cores all cracks and veins are
 176 oriented parallel to the bedding, we applied the 2-D smoothing filters in the direction
 177 perpendicular to the object planes to ensure minimum effect on the fracture roughness.
 178 Subsequent use of simple thresholding, where necessary combined with a watershed procedure
 179 (Beucher and Meyer, 1992) and/or a region-growing algorithm, enabled us to isolate individual
 180 objects, i.e. cracks and veins, following procedures similar to Kobchenko et al. (2011) and
 181 Panahi et al. (2012). For some samples it was needed to delete an outer ring voxels of the sample
 182 to get rid of beam hardening effects, which effectively decreased sample diameter by ~1 mm.
 183 After filtering individual veins and fractures were isolated for subsequent data processing.

184 Table 2. Details of XCT analysis.

Sample Code	Location	Voxel size (µm/voxel)	Number of extracted veins	Number of extracted cracks	pre-segmentation operations	Filters calcite	Filters cracks	Extra details
SQ689.3-SS5	XCT Oslo	24.6	3	1	conversion to 8-bit unsigned	NLM: 30-10-0.6	NLM: 30-5-0.3	Cracks: tophat filter
SQ636.5-SS11	XCT Oslo	12.7	1	-	conversion to 8-bit unsigned; normalize grayscale	NLM: 21-7-0.4 (2x)	n/a	threshold, use various region-growing algorithms, watershed
SQ685.65-SS7	XCT Oslo	25.7	2	2	conversion to 8-bit unsigned	n/a	NLM: 12-7-0.6	threshold, use various region-growing algorithms, watershed
	XCT Oslo	7.8	-	1	conversion to 8bit unsigned; normalize grayscale	n/a	NLM: 30-10-0.6	threshold, use various region-growing algorithms, watershed
	Synchrotron, ESRF ID 19	1.7	-	1	16-bit	n/a	NLM: 8-4-0.8	Threshold, use various region-growing algorithms, watershed
	Synchrotron, ESRF ID 19	0.16	-	1	16-bit	n/a	NLM: 15-5-0.9	threshold, use various region-growing

								algorithms, watershed
SQ705.3- SS19	XCT Oslo	23.5	-	1	conversion to 8-bit unsigned; normalize grayscale	n/a	NLM: 30-7- 0.5	Beam hardening correction before filtering

185 For slopes and Hurst exponents of the individual objects, see Table SM1. NLM stands for Non-
186 Local Means Filter in AvizoFire© software.

187 *2.3 White light interferometry topography imaging*

188 The topography of the fractures exposed on the surface of the slabs was measured directly using
189 a white light interferometer (Wyko NT1100) plus Veeco software (Figure 1f; 1h). For these slabs
190 we measure the vein-air interface, and we interpret them to be similar to the matrix/air interface
191 of the open cracks extracted in 3-D with microtomography. The interferometer was placed on a
192 damped table, allowing vertical nanometer resolution. All samples were scanned at 5x and 20x
193 magnification (5x Wyko lens and 20x Leica lens, both with a field of view of 1) and sample
194 SQ631.45-SS15 was imaged at magnifications of 2.5x-5x-10x-20x and 40x. The slip surface
195 sample SQ698.0-SS20 was scanned at all available magnifications, so at 2.5x-5x-10x-20x-25x-
196 40x-50x and 100x, with accompanying sampling distances (i.e. pixel size in the height images)
197 between 3.90 μm and 94.51 nm. After scanning, the fracture topography data are imported into
198 Matlab. For locations with insufficient light exposure and missing topography data (between 1
199 and 10% of the scanned area) the data was interpolated using the standard Matlab function
200 'griddata'.

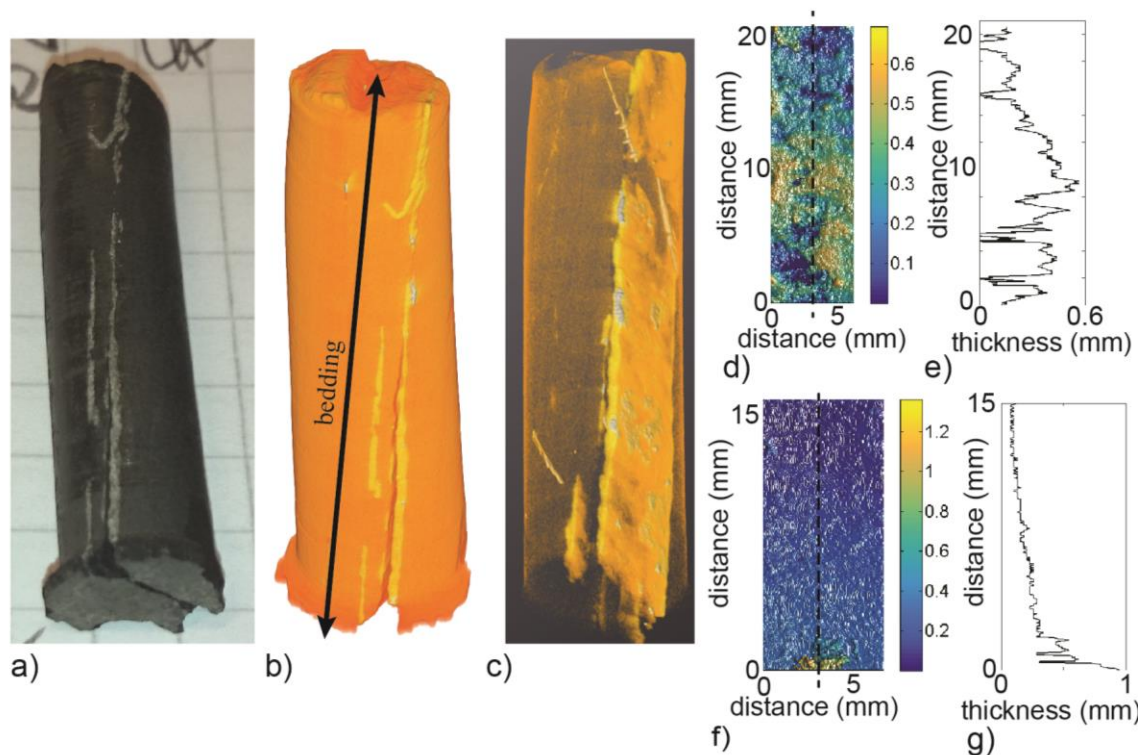
201 *2.4 Data processing*

202 Once the 2D (white light interferometry) and the individual fractures and veins from the 3D
203 (XCT) data were acquired, we analyzed the topography of the fractures and of the vein-matrix
204 interface. The variation of the height of a surface is called the roughness, and we quantify how

205 the roughness amplitude varies with the measurement scale with the Hurst exponent H , in order
206 to characterize the spatial correlations in the samples. First, the isolated cracks and veins derived
207 from the XCT data and the WLI data were imported as height fluctuations around a mean plane.
208 The XCT data were subdivided in out-of-plane fluctuations of the top surface, the bottom surface,
209 and the fluctuation of the thickness or aperture (obtained by subtracting the bottom from the top
210 data). Some examples of 1-D height versus distance profiles are given in Figure 3. To determine
211 the Hurst exponent H , we have followed the standard steps as outlined in detail by Candela and
212 co-authors (Candela et al., 2009; Candela and Brodsky, 2016). In short, we extracted the height
213 profiles in one direction and removed a linear trend if needed. Since the Fourier transform is the
214 least influenced by the noise of the measurement apparatus and by missing data (Schmittbuhl et
215 al., 1995; Candela et al., 2009), we calculated the Fourier power spectrum density for each
216 profile, which were then averaged across the sample. A power-law fit of the linear part of the
217 Fourier spectra in a log-log plot is performed to extract the Hurst exponent, taking into account
218 only the well-resolved wavenumbers. The minimum wavenumber is related to the size of the
219 surface divided by 2 and corresponds to the Nyquist frequency of the data. The maximum
220 wavenumber is limited by the spatial resolution of the acquisition system (see Appendix Table
221 A1 for wavenumbers of each fit). Candela and Renard (2012) have shown that when 40% of the
222 datapoints is missing, it will lead to an error of 4% for the value of H , which implies that the
223 error on the analysis of our white light interferometer data (max. 10% unexposed area) is $< 4\%$.

224 We have verified our calculation against synthetically randomly generated surfaces (Biermé et
225 al., 2007), showing that our code calculates the same Hurst exponent (± 0.02) as the input value.
226 Furthermore, to determine the effect of any geometrical anisotropy, the Hurst exponent of each
227 object is determined in two directions, in the x and y directions of the resulting fracture paths.

228 Each fracture or vein was defined by its own set of (x,y) coordinates, which were then either
229 parallel or perpendicular to the bedding, depending on the orientation of the original object.



230
231 Figure 3. Example of the various analyses performed using XCT for sample SQ686.5-SS7 (25
232 $\mu\text{m}/\text{voxel}$ scan), which contains two calcite veins (in white) as well as open cracks. For the other
233 XCT images, see Figure A1-4 in Appendix 1. a) photo (squares on paper are 5x5 mm). b)
234 unprocessed scan (false color image), including the orientation of the bedding. c) high density
235 data from b) (i.e. vein material). d) largest surface area of the calcite vein. e) example of a 1-D
236 transect of thickness vs. distance in e). f) largest surface area of extracted crack (see also 3D
237 model 2). g) example of a 1-D transect of thickness vs. distance from g).

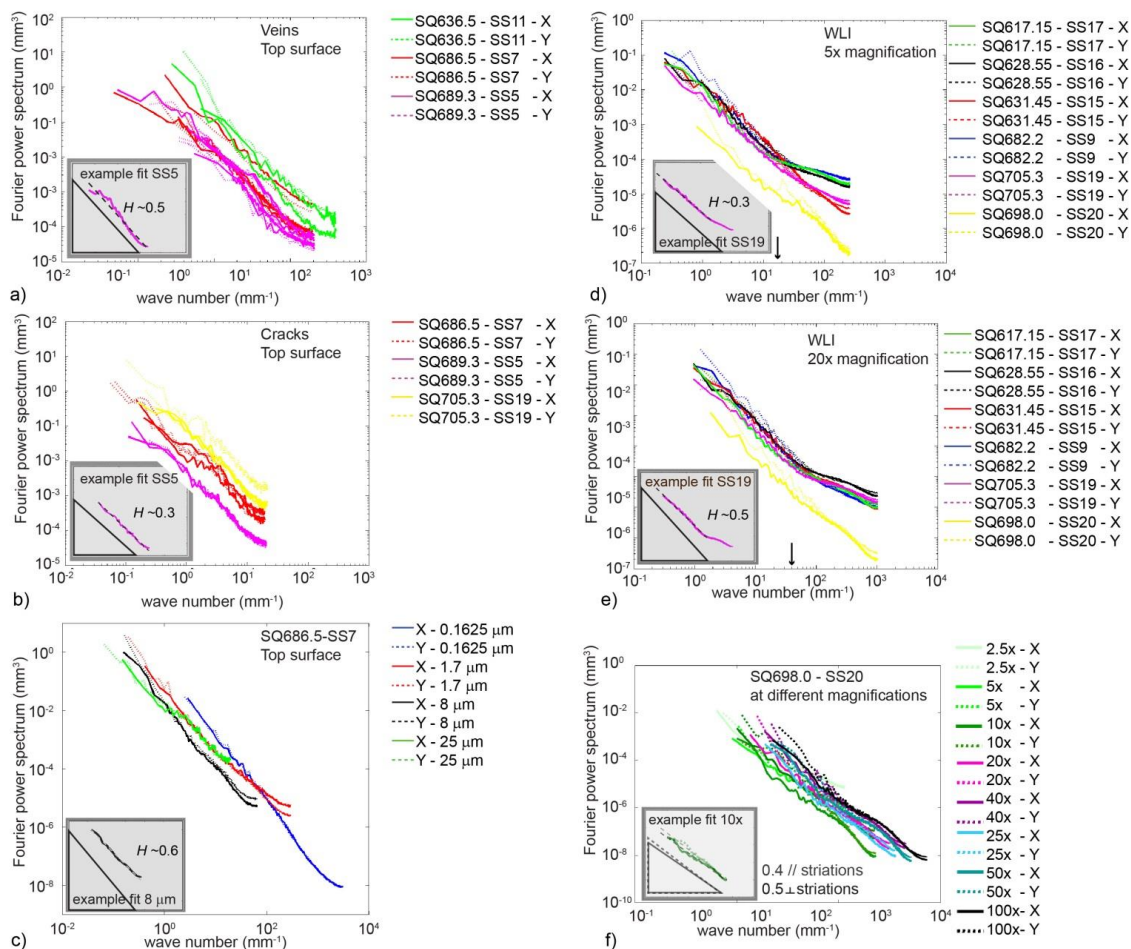
238 3. Results

239 3.1 Roughness

240 3.1.1 X-ray microtomography data

241 At low resolution, we extracted in total thirteen objects, six veins and seven cracks. Example
242 data are shown in Figure 3 and in the 3D models. The results of the Fourier analysis of the top

243 surfaces for these low resolution objects are shown in Figure 4a (veins) and 4b (cracks).
 244 Individual values are given in Appendix Table A1.

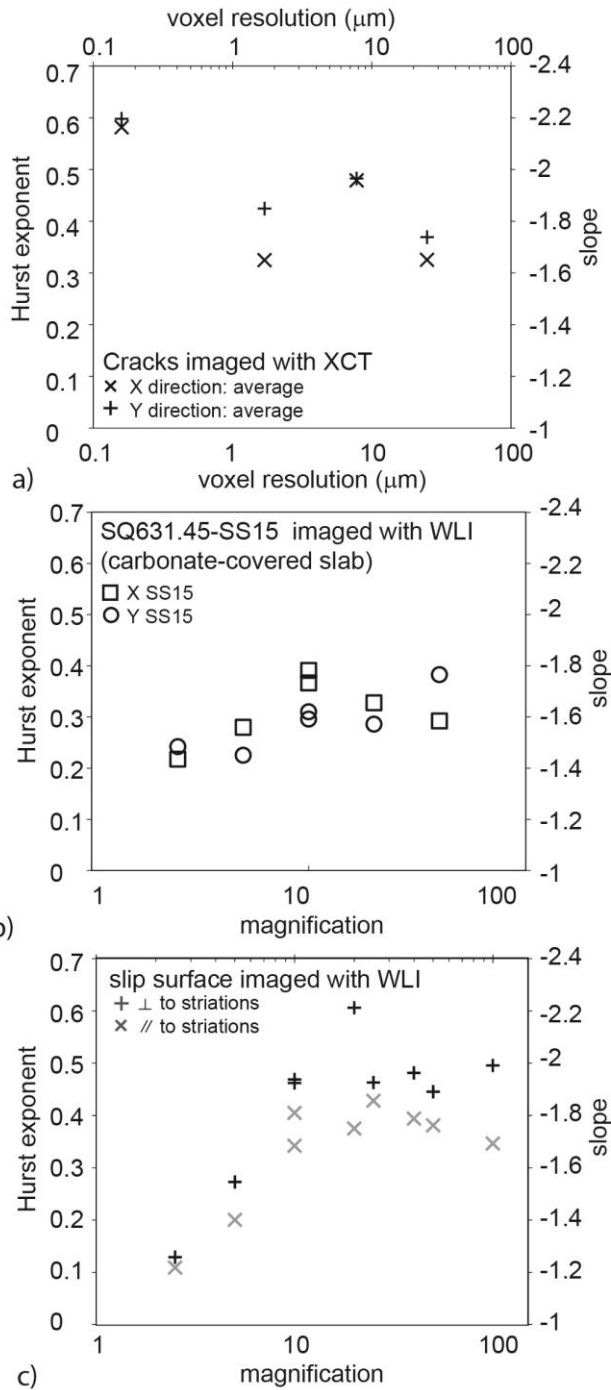


245
 246 Figure 4. Wave number versus Fourier power spectrum for the top surfaces of the veins and
 247 cracks obtained from the XCT scans and for white light interferometry. Appendix 1 contains all
 248 images plus individual Hurst exponents. The different colors indicate different samples, as
 249 shown in the legend. For the XCT data multiple single objects are analyzed from each sample.
 250 Each subplot contains an inset with an example fit. a) XCT data; veins; resolution 11-26
 251 $\mu\text{m}/\text{voxel}$. b) XCT data; cracks; resolution 20-26 $\mu\text{m}/\text{voxel}$ c) XCT data; crack in sample
 252 SQ686.5- SS7 at multiple resolutions. d) WLI data, 5x magnification; sampling distance 1.94 μm .
 253 There is a break in slope at wave number 17.8 mm^{-1} , indicated with an arrow. e) WLI data, 20x
 254 magnification; sampling distance 0.495 μm . There is a break in slope at wave number 39.8 mm^{-1} ,
 255 indicated with an arrow. f) WLI data, the slip surface of sample SQ698.0-SS20 imaged at
 256 multiple magnifications. For this sample X is parallel to the striations, and Y is perpendicular to
 257 the striations.

258 At this lower resolution, the 3D data do not exhibit significant difference between top, bottom
259 and differential surfaces (i.e. fracture aperture or vein thickness), nor any difference in slope for
260 the x - or the y -direction. Thus there is no significant anisotropy at this scale. Slopes are similar
261 between the different objects, regardless from which sample they were extracted. The intercept
262 of the curve (which is indicative of the magnitude of the out-of-plane fluctuation) differs widely
263 between, and there are no clear trends with object type or direction in intercept value. Since the
264 slope of the power spectrum plot exhibits clear trends, it will therefore be the focus of the present
265 study. The vein-rock interface exhibits a Hurst exponent of $\sim 0.53 \pm 0.11$, and the cracks exhibit H
266 $\sim 0.29 \pm 0.1$ (Table 3), showing a significant difference between the roughness exponent of the
267 vein-rock interfaces and exhumation cracks.

268

269 We have imaged SQ686.5-SS7 at four different spatial scales with 0.16, 1.7, 7.8, and 26
270 $\mu\text{m}/\text{voxel}$. Visual inspection of the data shows that the air/matrix interface and the vein/matrix
271 interface become more detailed with increased imaging resolution. With increased resolution the
272 maximum length scale that can be obtained also decreases, due to the accompanying decrease in
273 the size of the volume imaged. We have extracted the open crack with the highest aperture at all
274 resolutions, and the resulting wave number versus Fourier power spectra are shown in Figure 4c.
275 The roughness curves for the different resolutions overlap, leading to a clear trend over four
276 orders of magnitude of spatial scales. At the resolutions above 0.16 $\mu\text{m}/\text{voxel}$ the curves exhibit
277 average Hurst exponents of approximately 0.3 ± 0.1 (Figure 5a). In contrast, at the highest
278 resolution of 0.16 $\mu\text{m}/\text{voxel}$, the Hurst exponent becomes more uniform, with on average $H =$
279 0.51.



280

281 Figure 5. Effect of the scale of the observation. a) For the crack in SQ686.5-SS7 imaged at
 282 multiple XCT resolutions in X and Y directions (both roughly parallel to the bedding). b)
 283 carbonate-covered slab SQ631.45-SS15 imaged at 2.5 to 40x magnification with the WLI. c) The
 284 slip surface imaged at multiple WLI magnifications. At magnifications of 10x and higher the
 285 Hurst exponent is approximately constant and anisotropic; $H = 0.38 \pm 0.03$ parallel to striations,
 286 and $H = 0.49 \pm 0.05$ perpendicular to the striations (see also Figure A6 in Appendix 1).

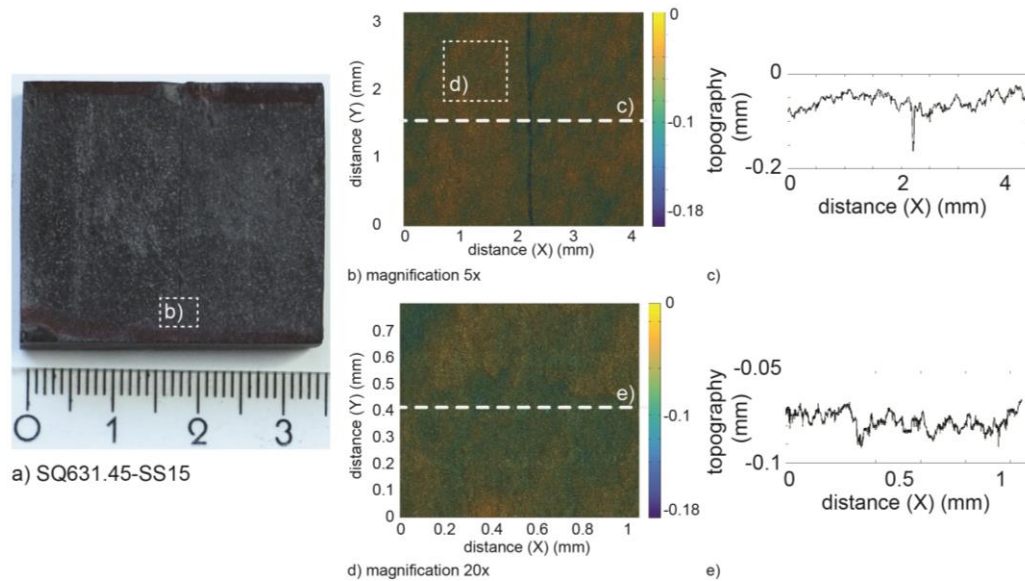
287 Table 3. Slopes and Hurst coefficients.

Analysis	Object	Resolution / Magnification	Direction	α (average \pm standard deviation)	H
XCT	Veins	12-26 $\mu\text{m}/\text{voxel}$	X	-2.09 \pm 0.19	0.55
XCT	Veins	12-26 $\mu\text{m}/\text{voxel}$	Y	-2.03 \pm 0.22	0.52
XCT	Cracks	12-26 $\mu\text{m}/\text{voxel}$	Y	-1.58 \pm 0.15	0.29
XCT	Cracks	12-26 $\mu\text{m}/\text{voxel}$	X	-1.56 \pm 0.19	0.28
WLI	Open vein surfaces	5x; sampling distance 1.9 μm	X	-1.54 \pm 0.074	0.28
WLI	Open vein surfaces	5x; sampling distance 1.9 μm	Y	-1.59 \pm 0.11	0.30
WLI	Open vein surfaces	20x; sampling distance 0.5 μm	X	-1.86 \pm 0.19	0.43
WLI	Open vein surfaces	20x; sampling distance 0.5 μm	Y	-1.94 \pm 0.28	0.47
WLI	Slip surface	Average 10x-100x	X - //	-1.76 \pm 0.06	0.38
WLI	Slip surface	Average 10x-100x	Y - \perp	-1.98 \pm 0.11	0.49

288 XCT stands for microtomography, WLI for White Light Interferometry, α is the average slope of
 289 all samples, and H stands for the Hurst coefficient. See Table SM1 in the Supplementary
 290 Material for the individual values. Note that with respect to α , the given average for the XCT
 291 data is the average of all possible surfaces, i.e. there is no difference between top, bottom or top
 292 – bottom surface.

293 3.1.2 White light interferometer data

294 Because of the clear visual difference in texture between the slabs with a mineral cover and the
 295 slab with the slip surface (Figure 1) we treat these separately. The white light interferometry
 296 scans of sample SQ631.45-SS15, representative for the calcite-covered samples, are shown in
 297 Figure 6, including examples of 1-D profiles (see Appendix 1 for the other surfaces). The wave
 298 number versus Fourier power spectra are shown in Figure 4d-f. At 5x magnification (sampling
 299 distance 1.9 μm) there is a break in slope at a wave number of 17.8 mm^{-1} (Figure 4d),
 300 corresponding to a length scale of 0.028 mm. At 20x magnification (sampling distance 0.5 μm)
 301 there is a break in slope at a wave number of 39.8 mm^{-1} , corresponding to a length scale of 0.013
 302 mm (Figure 4e).



303

304 Figure 6. WLI scans on sample SQ631.45-SS15. The scans of the other samples are in the
 305 Appendix Figures A5 and A6. a) sample photo. Location of scan shown in b) indicated by the
 306 white box. b) WLI scan at 5x magnification (sampling distance 1.94 μm). Location of the profile
 307 shown in c) indicated with the white dotted line. Location of the scan shown in d) indicated by
 308 the white box. c) Example of 1-D profile along X-direction. d) WLI scan at 20x magnification
 309 (sampling distance 0.495 μm). Location of the profile shown in e) indicated with the white
 310 dotted line. e) Example of 1-D profile along X-direction.

311 For length scales shorter than these numbers roughness exponents become lower. SEM-EDS
 312 analysis showed barite crystals in the carbonate cover of approximately that size and since barite
 313 exhibits strong cleavage, we relate these low roughness exponents to interference between the
 314 reflected light from barite cleavage planes and the reference beam in the WLI. Therefore, the
 315 slopes reported in Table 3 are for the length scales exceeding 0.029 and 0.013 mm respectively.
 316 The WLI data exhibit similar slopes in both x and y directions, and there is a clear difference
 317 between low and high magnification. Note that the slabs are all taken perpendicular to the
 318 bedding, so the x and y directions both lie in the plane perpendicular to the bedding. At 5x
 319 magnification, the average Hurst exponent is 0.28 to 0.30, and at 20x it is on average 0.43 to 0.47
 320 (Table 3). We imaged the surface of the carbonate-covered slab SQ631.45-SS15 (Figure 6) at 2.5
 321 to 40x magnification, which indicated little change in roughness with magnification – though a

322 significant increase in the spread at 20x magnification (as shown by the increased standard
323 deviation in Figure 5b; see also Appendix Table A1).

324 We imaged the slip surface at all possible WLI magnifications, from 2.5-100x. At 2.5x
325 magnification (3.9 μm sampling distance) $H \sim 0.11$ and at 5x magnification (1.9 μm sampling
326 distance) $H \sim 0.3$ (Table 3, Figure 4f). For magnifications of 10x and more the Hurst exponent is
327 fairly constant as well as strongly anisotropic (Figure 5b): $H = 0.38 \pm 0.03$ parallel to striations,
328 and $H = 0.49 \pm 0.05$ perpendicular to the striations. The slope is constant over more than three
329 orders of magnitude of length scales (Figure 4f).

330 **4. Discussion**

331 We have shown that roughness values of cracks and veins in the Pomeranian shale can be
332 obtained not only from conventional WLI measurements, but also from segmented XCT images.
333 In the following, we relate the obtained roughness values of the open cracks and discuss the
334 possible origin of the difference between cracks and veins. This is followed by the effect of scale
335 of observation on the roughness, and the implications for modeling flow through fractures in the
336 Pomeranian shale.

337 ***4.1 The roughness of open cracks and the shale microstructure***

338 In general, crack roughness is studied because it is considered as a ‘fossil record’ of crack
339 propagation, the path of which is determined by the stress field at the crack tip. Following
340 continuum theory of crack growth, a crack propagating in an isotropic solid follows a path so the
341 shear stress at the crack tip is eliminated. For isotropic homogeneous materials, this is described
342 by linear elastic fracture mechanics theory (LEFM; i.e. Bonamy, 2009). $H = 0.8$ is in physics
343 frequently reported as the ‘universal’ roughness value for simple fracture (i.e. little displacement)

344 of many different (though usually homogeneous) materials, including some rock materials (c.f.
345 Bouchaud, 1997; Renard et al., 2013). The values reported in this paper are much lower, but
346 recently it has been shown that in Fontainebleau sandstone and sintered glass bead-cylinders
347 simple mode I fracture leads to isotropic Hurst exponents of 0.4 (Ponson et al., 2006, 2007).
348 This sandstone is a homogeneous, pure quartz rock, and observations were from the grain scale
349 and up. On a qualitative basis, the open cracks in our heterogeneous shale samples share
350 similarities to the mode I fractures in sandstone, since they, too, are caused by the simple
351 splitting of the core material after exhumation. Our low resolution observations are up to a few
352 tens of microns in scale, i.e. on the same scale as the grain size of the randomly dispersed strong
353 clasts (quartz, carbonates and feldspar, see also Figure 2f). On this scale, these clasts will have a
354 large influence on the stress field of a crack propagating through the weak, submicron clay
355 matrix. The low value of $H = 0.3$ reported here indicates that the crack path in shale is more
356 irregular than the mode I path in the pure sandstone (Ponson et al., 2006, 2007). Even though no
357 controlled experiments have been performed yet on heterogeneous rock materials such as shale,
358 it is interesting to note that on the nanometer scale, atomic force microscopy studies have shown
359 that the roughness exponent in soda-lime-silica glass was 0.18 versus 0.29 in silica glass. This
360 was attributed to the presence of the different ions in the soda-lime-silica glass (Wiederhorn et al.,
361 2007), and this deviation in Hurst exponent is similar to the difference $H = 0.3$ in shale vs. $H =$
362 0.4 in sandstone for mode I cracking. Differences in material properties, fracture type, pressure,
363 fracture dynamics, temperature, chemistry, and/or deformation mode can lead to a much wider
364 range of roughness exponents than previously thought on the basis of simple fracture mechanics.
365 The microstructure of the Pomeranian shale is fairly typical for shales in general, since shales are
366 defined as rocks that contain about 30% clays (e.g. Horsrud et al., 1998), where the clay particles

367 are usually micro-meter sized (Meunier, 2006). This implies that these low Hurst exponents may
368 be more common than previously thought.

369 *4.2 The difference in roughness between cracks and veins*

370 Following the analogy to mode I cracking in sandstone, the Hurst exponent of 0.3 for the air/rock
371 interface can be explained by the presence of strong clasts that deviate and randomize the path of
372 a propagating crack. But why does the vein-rock interface, with a Hurst exponent of 0.5, exhibit
373 a less random pattern? We postulate three possible causes: i) the open cracks formed at a
374 different in-situ stress than the veins, ii) the opening mode was different, or iii) there is an
375 evolution effect, either through fluid flow (chemical alteration) or through displacement
376 (mechanical alteration).

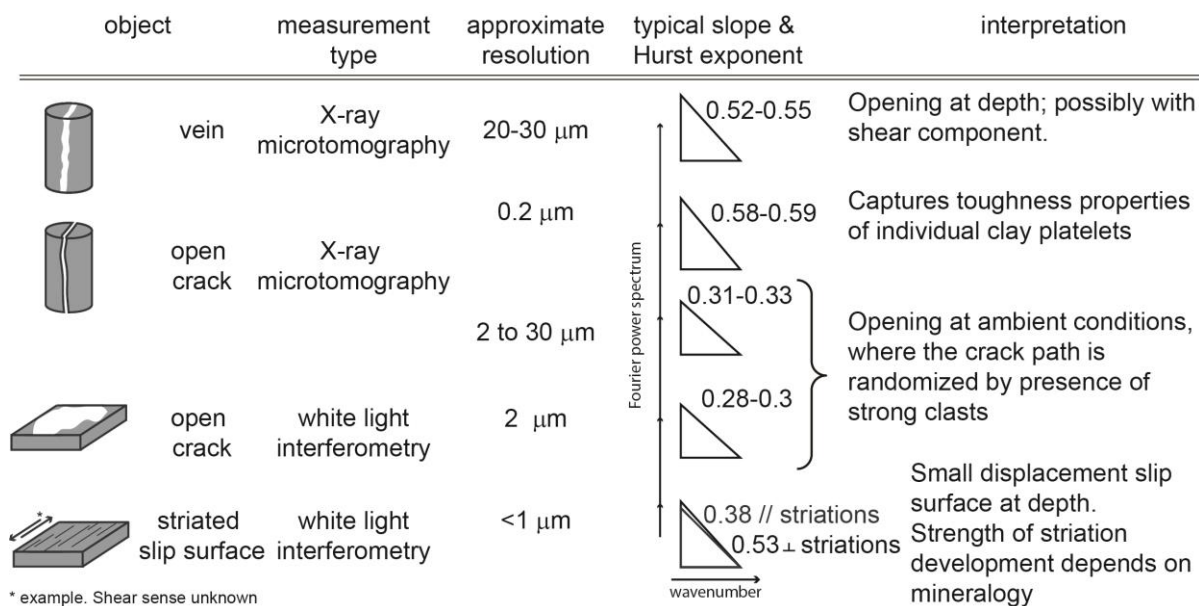
377 First, Griffith crack growth theory states that crack growth only proceeds when the release of
378 mechanical energy exceeds the energy needed to create a new surface. The stress state in the
379 unfractured matrix plays a role in determining the direction of propagating crack (Bonamy,
380 2009), which implies as well that the initial stress state of a rock may play a role. The open
381 cracks propagated at ambient conditions, i.e. where the rock has relatively little stored elastic
382 energy, so they opened in a different stress field than the veins. It is reasonable that the presence
383 of strong inclusions has a higher impact in determining the direction or the deviation of the crack
384 path than for a rock at depth, when the entire system is already under stress. In other words, if the
385 initial stress state of the intact rock is σ_i , and the stress induced by heterogeneities is $\Delta\sigma$, the ratio
386 of $\Delta\sigma / \sigma_i$ is drastically different for the opening of cracks at ambient conditions from opening
387 under in situ stress. In this way the inherently heterogeneous nature of shales may cause the less
388 random nature of the cracks opening in the subsurface.

389 Second, the simple splitting of the shale to form the open cracks likely corresponds to simple
390 mode I opening. For the veins, the large crystals in the center of the veins (Figure 2g-h) are
391 indicative of initial mode I crack opening thereby allowing for slow crystal growth. The small
392 crystals along the side indicate that this phase is followed by a reactivation phase with fluid flow
393 along the vein/matrix interface. However, opening under a confining pressure usually introduces
394 a shear component as well (Bonamy, 2009), and therefore it seems unlikely that tensile opening
395 of subsurface cracks will be pure mode I. It is possible that the difference in roughness between
396 veins and crack is (partially) an effect of pure mode I opening combined with a small shear
397 component for the veins versus simple mode I for the cracks. Most Hurst exponents in the
398 literature are measured on mode I cracks (Bouchaud, 1997). When considering mode II fractures,
399 the shear on the fracture induces usually some anisotropy, which develops as slip increases
400 (Amitrano and Schmittbuhl, 2002). Finally, when considering a fault surface, the anisotropy is
401 pronounced at all scales (Renard et al., 2006; Candela and Renard, 2012). So a difference of
402 Hurst exponent between mode I and mode II fractures and faults is expected, where the
403 anisotropy of the Hurst exponent with direction will be larger for mode II slip surfaces than for
404 mode I fractures.

405 Comparison between the values from the vein/rock interface to those obtained for the slip surface
406 of sample SQ698.0-SS20 helps to constrain if there is an evolution effect. Striations on this
407 surface are omnipresent (Figure 2; Appendix Figure A6), introducing a clear textural anisotropy.
408 The roughness of the slip surface in itself was lower than the roughness reported for the strongly
409 striated slip surfaces reported by Candela and Renard (2012), which we interpret as an effect of
410 small displacement (Sagy et al., 2007; Brodsky et al., 2011). Since the vein/rock interface was
411 perfectly isotropic, this implies there was no or very little mechanical alteration of the interface.

412 The approximate match in roughness values of the striated surface and the vein-rock interface
 413 imply that the mechanical and chemical evolution only have small effects on the roughness of
 414 cracks opening in the subsurface.

415 We have summarized our observations and the possible causes in Figure 7. The most likely
 416 causes of differences between cracks and veins are either the difference in opening mode and/or
 417 the difference in in-situ stress. Both of these explanations imply that cracks that open at depth in
 418 shales produce a different roughness than those opening at ambient conditions. This indicates
 419 that the Hurst roughness exponent can be a microstructural criterion to determine between
 420 exhumation and in-situ fractures. To be fully confident this could be extrapolated to other shales
 421 more research is required, though there seem to be no a priori reasons why the aforementioned
 422 principles/mechanisms would not apply to other drill core shales.



424 Figure 7. Summary of observations and interpretations. The Hurst values indicated in the table
 425 represent the range of average values for each object type.

426 *4.3 The effect of scale*

427 Following Ponson et al (2007) and taking the shale microstructure into account, we can also
428 explain the increase in Hurst exponent with increased scale of observation from 0.3 to 0.51 for
429 open cracks and from 0.3 to 0.4-0.5 for the slip surface (Figure 5a, 5c). At small length scale
430 ('the process zone'), fractures develop from growth and coalescence of small-scale defects. At
431 larger length scales, the characteristics of the fracture surface are determined by the fully brittle
432 manner of continuous crack propagation, and the final roughness is controlled by the toughness
433 distribution at the microscale (Ponson et al., 2007). Translating this concept to fine-grained
434 shales, it is only at the sub-micron scale that the toughness properties of the fine-grained, weak
435 clay platelet topography are captured. At the micron scale and above, crack propagation is
436 controlled by the properties of the heterogeneous distribution of large, strong clasts in an
437 anisotropic fine-grained matrix, but at the submicron resolution the clay platelets data determine
438 material toughness and therefore crack path ($H \sim 0.51$ for high resolution XCT data). A similar
439 argument explains why the Hurst exponent for the carbonate cover does not change with
440 increased magnification (Figure 5b), since the largest sampling distance of $3.9 \mu\text{m}$
441 (magnification 2.5x) is on the same order as the grain size of the carbonate grains. A decrease in
442 sampling distance therefore does not change the type of properties captured. In contrast, when
443 considering the slip surface there is a significant effect of magnification (Figure 5c). With a low
444 resolution (i.e. magnifications below 10x, or scanning distances above 1 micron), the exponent
445 obtained is representative of the spatial distribution of the patchy localities of fault gouge (Figure
446 2b). To capture the anisotropy related to topography of the slickensides, the resolution must be
447 chosen high enough so that the slickensides and their spacing represent a significant part of the
448 topographic signal.

449 The interplay between roughness and processes which each have their own scale causes the
450 change in Hurst exponent when changing the measurement resolution. Different effects are
451 captured when changing the resolution, since increased spatial resolution usually comes with
452 decreased sample size. To decide on the resolution needed to reliably determine the Hurst
453 exponent, first the size of the smallest element of interest needs to be determined (i.e. the
454 structure and grain size of the material), which becomes particularly important in polymineralic
455 materials. Different mineral grains will lead to different fracture patterns on the grain scale,
456 which corresponds to differences in strength on the grain scale as well. Ultimately, imaging and
457 roughness determination need to be done at a resolution that is appropriate for the feature of
458 interest, i.e. taking the microstructure into account.

459 **4.4 Implications**

460 From a geoengineering perspective, the main interest in the roughness of these fractures stems
461 from the need to accurately model fluid flow in (open) fractures at depth. For these purposes it is
462 important to understand the roughness one could expect for fractures at depth in tight rock
463 formations (Noiriel et al., 2007; Fitts and Peters, 2013). For an engineered fracture the expected
464 fracturing mode would be tensile opening of the formation at depth, probably with a small
465 component of shear displacement. Comparing such a fracture to the types of fractures studied
466 here, it would be the striated surface and the vein-rock interface which would have a more
467 representative history. On this basis, we propose a Hurst exponent H in the range 0.4 to 0.5 as
468 most representative for (induced) fractures in the Pomeranian shale. If a flow model is finely
469 enough meshed and only covers an area comparable in size to that of the high resolution XCT
470 scan ($< 1 \times 1$ mm, see Figure A4), a value representative for the clay structure, up to 0.6 could be
471 used. At larger areas the randomizing effect of the heterogeneous distribution of the strong

472 feldspar, quartz and carbonate clasts should be taken into account. However, since many
473 different types of shale exist, with as many different applications, we call for more roughness
474 studies on these strongly heterogeneous and anisotropic geo-materials, especially considering
475 that the values presented here differ significantly from other rocks investigated so far.

476 With respect to the possible apertures of a fracture, the out-of-plane fluctuations of the vein-rock
477 interface as observed with XCT are locally up to 0.3 mm. However, it is not possible to correlate
478 this one-on-one with aperture values, since the XCT data do not provide direct information on
479 timing, and the microstructures of sample SQ685.65-SS7 (Figure 2g-h) indicate multiple phases
480 of opening and precipitation. For the data presented here it is the single striated slip surface
481 which would be the most representative sample for fresh fractures at depth in shale. At low
482 magnifications (i.e. relatively large surface area, 2.5 x 2 mm), it still exhibited out-of-plane
483 fluctuations of 0.1 mm (Appendix Figure A6). The SEM images indicated this is probably
484 related to the presence of fault gouge that adheres to the surface. This is to our knowledge the
485 first measurement of topography on a fresh shale sample representative for low displacement
486 fractures. Assuming this single surface is indeed representative for unmated surfaces at depth, it
487 indicates that minimum apertures for low displacement induced fractures up to 100 μm are
488 plausible.

489 **5. Conclusions**

490 Shales can be caprock and source rock both, where their permeability and transport properties
491 are controlled by the presence of microfractures. Most shales weather easily, so the most pristine
492 samples are usually those obtained from boreholes. However, one of the major challenges with
493 borehole samples is to determine which fractures are present in-situ and which are caused by
494 sample handling. In this study, we determined the roughness of open exhumation/drying cracks

495 as well as intact vein-rock interfaces plus one striated slip surface in Pomeranian shale samples
496 obtained from 4 km depth. We used the new method of X-ray micro-tomography as well as
497 conventional white light interferometry and found the following:

- 498 - Roughness values obtained with both methods are consistent, which indicates that the 3-
499 D data obtained from microtomography scans can indeed be used to extract quantitative
500 properties on the roughness of the vein/rock and fracture/matrix interface.
- 501 - Open cracks in shale and in veins exhibit Hurst exponents of 0.3 ± 0.1 and 0.5 ± 0.1
502 respectively. The two most likely causes of this difference are the difference in opening
503 mode and/or the difference in in-situ stress, which implies that the Hurst roughness
504 exponent can be a microstructural criterion to determine between exhumation and in-situ
505 fractures. To be fully confident this could be extrapolated to other shales more research is
506 required, though there seem to be no a priori reasons why the aforementioned
507 principles/mechanisms would not apply to other drill core shales.
- 508 - For fine-grained heterogeneous rock such as shale the Hurst roughness exponent changes
509 with scale of observation, which is related to the microstructure. Imaging and roughness
510 determination should be performed done at a resolution that is appropriate for the feature
511 of interest, i.e. keeping the microstructure in mind.
- 512 - We propose a Hurst exponent H in the range 0.4 to 0.5 as most representative for
513 (induced) fractures in the Pomeranian shale, since they form in a more similar fashion as
514 the striated surface and the vein-rock interface.

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