

Jessica Hoth, Gabriele Kaiser, Andreas Busse, Martina Döhrmann, Johannes König & Sigrid Blömeke

Professional competences of teachers for fostering creativity and supporting high-achieving students

Keywords: teacher competence, video-based test, creativity, giftedness

Abstract

This paper addresses an important task teachers face in class: the identification and support of creative and high-achieving students. In particular, we examine whether primary teachers (1) have acquired professional knowledge during teacher education that is necessary to foster creativity and to teach high-achieving students, and whether they (2) possess the situation-specific skills necessary to do so. For this purpose, (1) the knowledge of German primary school teachers who participated in the TEDS-M study at the end of teacher education is analyzed. (2), a subset of these teachers interpreted classroom video scenes that require identifying and supporting creative and high-achieving students in the longitudinal Follow-Up study to TEDS-M (TEDS-FU) after three years of work experience. Contingency analyses between teachers' professional knowledge and their skills to identify and support mathematically creative and high-achieving students were carried out. They revealed that those teachers who have difficulties in logical reasoning and understanding structural aspects of mathematics also have difficulties with identifying and supporting creative and high-achieving students. It was difficult for them to identify students' thinking processes based on structural reflections and pattern recognition as well as to further develop mathematically rich answers by students. In line with these results, teachers with strong professional knowledge were able to meet identify and support mathematically creative and high-achieving students. Thus, the study reveals that a connection between teachers' professional knowledge and their skills to identify and support mathematically creative and high-achieving students exists but that many future and early career teachers seem to have deficits in these respects.

J. Hoth
Department 2, University of Vechta, Driverstraße 22,
49377 Vechta, Germany
Jessica.hoth@uni-vechta.de
Tel.: +49-4441 15576

G. Kaiser, A. Busse
Faculty of Education, University of Hamburg, Von-Melle-Park 8, 20146 Hamburg, Germany

M. Döhrmann
Department 2, University of Vechta, Driverstraße 22,
49377 Vechta, Germany

J. König
University of Cologne, Gronewaldstr. 2, 50931 Köln, Germany

S. Blömeke
Centre for Educational Measurement (CEMO) at the University of Oslo,
Gaustadalleen 30, N - 0318 Oslo, Norway

1. Introduction

In mathematics classrooms, teachers are faced with a multitude of challenges. One of these challenges is to meet the heterogeneous learning requirements of their students. Mathematics teachers, therefore, do not only need to see and react on learning difficulties and misconceptions by students, but they also need to be aware of students' strengths, their creativity and abilities. Teachers need to understand students' diverse learning approaches, they must be able to identify quality and creativity in students' multiple solutions and to draw conclusions about students' mathematical ability. Shayshon et al. (2014, p. 410) claim that "the teachers' role in nurturing mathematically talented students should be one of the main focal points in teacher preparation and professional development programs".

The present article focuses on this aspect and examines whether future teachers have developed the mathematics content knowledge (MCK) and mathematics pedagogical content knowledge (MPCK) during teacher education that is necessary to foster creativity and to support mathematically able students. Furthermore, it will be examined whether these teachers possess situation-specific skills to identify and foster creativity and support high-achieving students within mathematics teaching after about three years of teaching practice. The international Teacher Education and Development Study in Mathematics (TEDS-M) assessed mathematics teachers' knowledge at the end of teacher education. Its longitudinal German Follow-Up study (TEDS-FU) focused on the competence development of these teachers during their first years of work experience. The TEDS-FU study included situation-specific skills of teachers using a video-based test that requires from teachers to react to classroom situations. Based on a secondary analysis of these data under the perspective described above, the aim of the present paper is to analyze whether German primary (mathematics) teachers possess the necessary professional competences to foster creativity and act adequately when teaching high-achieving students.

2. Theoretical background

Children bring different prior knowledge and learning strategies to the classroom. However, as Shayshon et al. (2014) point out, teachers often pay more attention to low-achieving students than to high-achieving ones. In order to analyze whether teachers possess the professional competences necessary to foster creativity and act adequately when teaching high-achieving students, the following section characterizes the concepts of mathematical giftedness and creativity. Subsequently, teachers' professional competences will be conceptualized.

2.1 Mathematical giftedness and creativity

Conceptualizing mathematical giftedness and creativity

The two terms mathematical giftedness and creativity are sometimes used synonymously (see f. ex. Krutetskii 1976) whereas Renzulli (2004) differentiates between "schoolhouse giftedness" and creativity. Mann (2006) points out that mathematically gifted students are often identified by their classroom performance, their test scores or by recommendations. But these characteristics constitute only one part of high achievement in mathematics (Hong & Aquí 2004, Mann 2006). Renzulli's model of giftedness includes three different but interdependent attributes of gifted learners, namely above-average ability, task commitment and creativity. According to this model, creativity is a subset of mathematical giftedness. In this regard, Wagner & Zimmermann (1986, p. 276) define mathematical giftedness as "a set

of testable abilities of an individual. If he or she scores high in nearly all of these abilities, there is a high probability of successful creative work later on in the mathematical field and related areas. These abilities are defined [...], stressing the following complex mathematical activities:

1. Organizing material
2. Recognizing patterns or rules
3. Changing the representation of the problem and recognizing patterns and rules in this new area;
4. Comprehending very complex structures and working within these structures;
5. Reversing processes;
6. Finding (constructing) related problems.”

Hong & Aquí (2004) describe the state-of-research about gifted children and list various features that distinguish gifted children from their non-gifted peers. Gifted children are stronger cognitively, intrinsically motivated, they are thinking more strategically and are more likely to have conscious control over solution processes, they use more strategies for organizing and transforming information and use them more effectively, they can transfer these strategies to novel tasks and they use more re-reading, inferring, analyzing structure, predicting, and evaluating strategies.

In the domain of mathematics, the term “creativity” is often used with reference to the work of mathematicians and their novel discoveries. Therefore, creativity in the context of school mathematics is generally related to “problem solving and or problem posing” (Nadjafikhah et al. 2012, p. 290). Haylock (1987) points out that there is no consensus about defining creativity. “Creativity in general is a notion that embraces a wide range of cognitive styles, categories of performance, and kinds of outcomes” (ibid., p. 68). However, Nadjafikhah et al. (2012) identify several criteria that many definitions of mathematical creativity have in common: Mathematically creative people develop new prolific mathematical concepts, they discover unknown relations and reorganize the structure of a mathematical theory. Therefore, creativity in mathematics is more than just profound knowledge and the reliable mastery of algorithms. “It entails incorporating experiences and conceptual understanding to solving authentic mathematical problems” (Mann 2006, p. 243).

In the context of assessing mathematical creativity of students, Mann (2009, p. 340) refers to the Creative Ability in Mathematics test developed by Balka (1974) and lists the following sub-abilities to be assessed, namely “the ability to

- formulate mathematical hypotheses concerning cause and effect in mathematical situations;
- determine and identify patterns in mathematical situations;
- break from established mentalities to develop solutions;
- consider and evaluate unusual mathematical ideas and think through their possible consequences for a mathematical situation;
- sense what is missing from a given mathematical situation and to ask questions that will enable one to retrieve the missing mathematical information;
- divide general mathematical problems into specific sub problems.”

Supporting mathematical giftedness and creativity

The main element in fostering students’ creativity and supporting gifted students in mathematics classrooms is the teacher and the opportunities that he or she offers for the

students to learn (Nadjafikhah et al. 2012). However, mathematics instruction often lacks adequate cognitive challenges for gifted learners but provides similar challenges to all students (Rotigel & Fello 2004), i.e. no model exists for supporting gifted students (Shayshon et al. 2014).

Meeting the needs of *each* individual learner should be the highest goal of education (Shayshon et al. 2014, Bolden et al. 2010). This requires that the teacher differentiates the learning opportunities provided. Learning environments that meet the needs of gifted students should appreciate alternative ideas and acknowledge multiple solutions (Nadjafikhah et al. 2012). The teacher should guide the students to ask suitable questions and give the opportunity to reflect on new ideas and concepts. Furthermore, students should meet opportunities to learn how to make and explore own conjectures, to hypothesize, refute and adapt heuristic strategies, to devise plans, to conclude, reason and justify the conclusions and reflect on them at a metacognitive level as mathematicians do (Nadjafikhah et al. 2012).

In this regard, Diezmann et al. (2002; Diezmann & Watters 2000) emphasize the importance of challenging tasks for effective learning processes and the necessity for teachers to select these tasks and support their students in the solution process (see also Shayshon et al. 2014). In order to enable mathematical discoveries and creativity, the teachers themselves need deep insight into the mathematical structures that they want their students to explore and they need a creative notion allowing the students to explore mathematical ideas and relations. Finally, the teachers need to identify, encourage and improve mathematically gifted students (Nadjafikhah et al. 2012).

“Thus, it is necessary to pay deeper attention to train teachers especially improving teachers' ability to design and implement educational environments that promote creativity in mathematics” (Nadjafikhah et al. 2012, p. 289). In the following, teachers' professional competences are conceptualized and knowledge is identified that teachers need to identify and support mathematical creativity and giftedness.

2.2 Teachers' professional competence

As Hattie (2009) points out, the quality of instruction depends to a large extent on the teacher and his or her professional competences. Therefore, much research was conducted in this area to conceptualize teachers' professional competences and their development during teacher education. The studies MT21 (Mathematics Teaching in the 21st Century; Blömeke, Kaiser & Lehmann 2008), TEDS-M (Teacher Education and Development Study in Mathematics; Blömeke et al. 2014) and COACTIV (Cognitive Activation in the classroom; Kunter et al. 2011) made important contributions in this area. Referring to the concept of competence defined by Weinert (2001, p. 48) as “cognitive abilities and skills possessed by or able to be learned by individuals that enable them to solve particular problems, as well as the motivational, volitional and social readiness and capacity to utilize the solutions successfully and responsibly in variable situations”, these studies include a cognitive and an affect-motivational facet as elements of teacher competences.

With regard to mathematics teachers, the cognitive facet is often distinguished according to the seminal work by Shulman (1986, 1987) in Mathematics Content Knowledge (MCK), Mathematics Pedagogical Content Knowledge (MPCK) and General Pedagogical Knowledge (GPK). The affect-motivational facet often includes epistemological beliefs about mathematics and about mathematical knowledge acquisition as well as motivational aspects

and aspects about the teaching profession (cf. Blömeke et al. 2008, Baumert & Kunter 2011, Peterson et al. 1989, Blömeke & Kaiser 2014).

However, Depaepe et al. (2013) point out that no general consensus exists about MPCK. They identify two different views on this facet. One view identifies MPCK as a dispositional facet which is located “in the head” of the teachers, while the other view emphasizes MPCK as a “social asset” that becomes relevant in the process of teaching. In this regard, Buchholtz et al. (2013) characterize two sub-dimensions of MPCK, namely a more subject-related and a more teaching-related sub-dimension. Other studies followed a similar understanding. For example Ball et al. (2008) developed the Mathematical Knowledge for Teaching (MKT) framework that categorizes the domains of knowledge needed to teach mathematics with various sub-facets.

The German longitudinal TEDS-M follow-up study (TEDS-FU) conceptualizes and assesses therefore teachers’ professional competences in addition to the dispositional approach of TEDS-M in a situated way. The analyses of the present article stem from secondary analyses of data from these two studies and examine the following research aims:

- (1) To what extent have future teachers acquired during their education the MCK and MPCK necessary to foster creativity and support mathematically able students?
- (2) To what extent do mathematics teachers possess the situation-specific skills to identify and foster creativity and support high-achieving students after three years of work experience?

In the following section, TEDS-M and TEDS-FU as well as their conceptualization of teachers’ professional competences are briefly described, before section 3 presents the methodological approach of the present paper.

2.3. The studies TEDS-M and TEDS-FU

TEDS-M (Blömeke et al. 2014) was an international study aiming at a comparison of teachers’ professional competences across countries and the efficiency of teacher education systems. TEDS-M was carried out under the auspices of the International Association for the Evaluation of Educational Achievement (IEA) and assessed future mathematics teachers in 17 participating countries, including about 1200 future primary teachers in Germany.

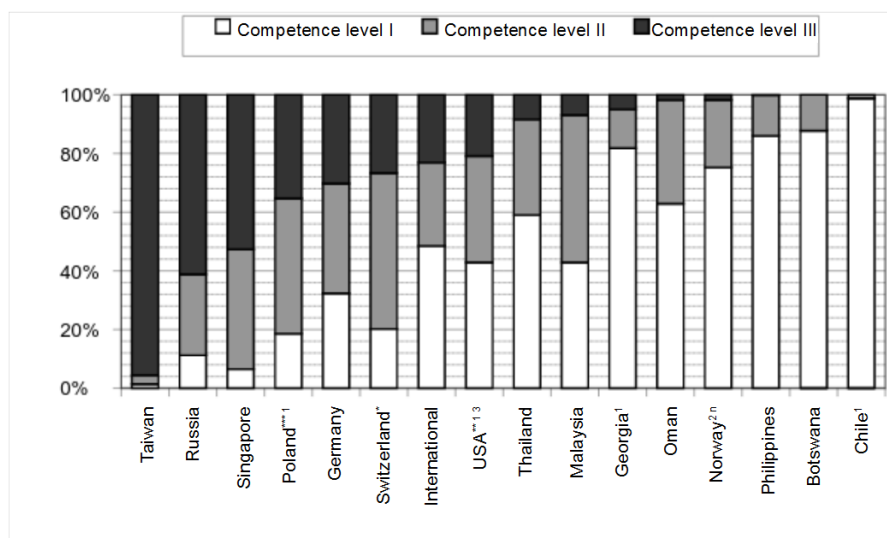
TEDS-M distinguished mathematics teachers’ professional knowledge based on Shulman (1986, 1987) into MCK, MPCK and GPK. MCK and MPCK were internationally assessed by a standardized paper-and-pencil test, while GPK could optionally be assessed in a national option. Regarding future teachers’ MCK and MPCK, key points on the scales, so-called anchor points were identified. For MCK three competence levels could be distinguished, for MPCK two (Tatto et al. 2012, 136-142). Using the description of teachers’ competences being at these levels, it is possible to identify indicators for whether the tested teachers possess the competences necessary for promoting creativity and supporting mathematically talented students. It has to be noted that these competence levels provide only indicators on the group level, and it is possible that single (future) teachers are able to act differently than described by their level. However, these competence levels give a first insight into the capability of the tested future teachers to meet the requirements for promotion of creative and talented students.

Concerning the MCK of future primary (mathematics) teachers the following three competence levels were identified: Competence level I – a level with weak mathematical achievement. Future teachers whose score fit this level missed structural insight, and their example-bound argumentation created difficulties. Competence level II – a level with average mathematical achievement. Future teachers whose score was at this level had sound knowledge and basic ideas at the fundamental level, but experienced problems with argumentative usage in more advanced problems. Competence level III – a level with the highest mathematical achievement. Future teachers at this level were characterized by strong structural mathematical knowledge. They were able to use this knowledge for standard problems in various mathematical areas, and they had skills in argumentation and logical reasoning.

With regard to the MPCK of future primary (mathematics) teachers, two competence levels were defined. Competence level I comprised all future primary mathematics teachers with lower achievement. These teachers had difficulties recognizing the correctness of students' answers and judging the adequacy of specific teaching strategies. Competence level II subsumed all future teachers with higher achievements in the MPCK items. These future teachers were able to interpret students' answers and possible cognitive barriers. In addition, they were able to describe their thinking, and they could identify the more appropriate teaching strategy for specific teaching sequences.

Regarding the requirements necessary to foster creativity and promote talented students, we can state that future (mathematics) teachers, who have difficulties working at an abstract mathematical level, who cannot develop sound mathematical argumentations and proofs or who have difficulties in understanding the adequacy of more complex argumentations by students, are not able to meet these requirements. Under this perspective, the international results of TEDS-M were in many countries not encouraging.

Figure 1 shows that only in Taiwan, Russia and Singapore, the majority of future primary teachers was at competence level III – the level that secures the mathematical knowledge necessary for supporting creativity and high-achieving students – in the field of MCK. The international mean was below a proportion of 50% at competence level III (figure 1). The international MPCK results displayed a similar result. Only the future primary teachers from Taiwan and Singapore reached in their majority the higher competence level. Internationally, only 27% reached this competence level (figure 2).



* Pedagogical universities in German-speaking cantons only

** Public universities only

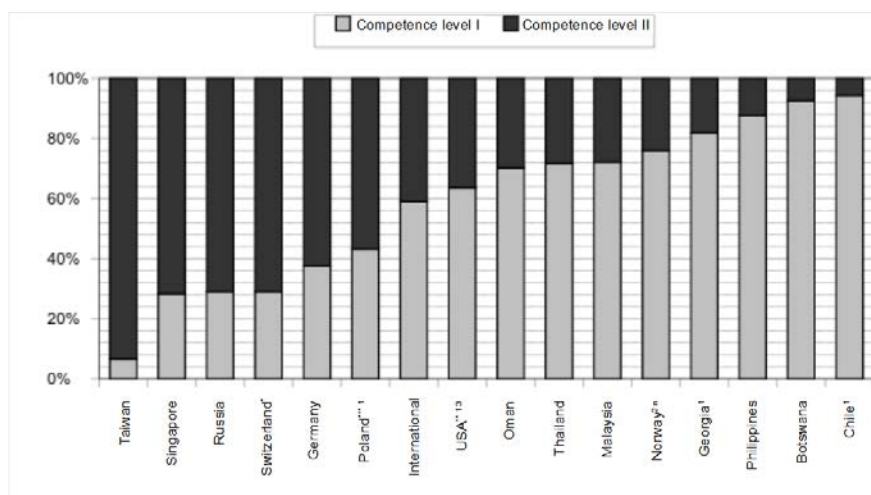
*** Institutions with concurrent teacher-educations programs only

n Sample meets the TEDS-M definition only partly, deviation from the IEA report

1 combined participation rate < 75%

3 substantial proportion of missing values

Figure 1: Competence levels of MCK of future primary (mathematics) teachers (Blömeke et al. 2010, p. 211)



* Pedagogical universities in German-speaking cantons only

** Public universities only

*** Institutions with concurrent teacher-educations programs only

n Sample meets the TEDS-M definition only partly, deviation from the IEA report

1 combined participation rate < 75%

3 substantial proportion of missing values

Figure 2: Competence levels of MPCK of future primary (mathematics) teachers (Blömeke et al. 2010, p. 233)

In order to get closer to actual teaching and classroom reality, the German Follow-up Study of TEDS-M extended the theoretical framework of TEDS-M by enriching the knowledge facets with more situated competence facets referring to the concept of noticing. Furthermore, the instruments of TEDS-M were complemented by video-based instruments evaluating the situated competence facets.

Referring to the concept of teacher noticing (Sherin et al. 2011, Carter et al. 1988), the TEDS-FU framework distinguishes three situation-specific skills, the so-called PID model (Blömeke et al. 2015, Kaiser et al. 2015, p. 373):

- a) “*Perceiving* particular events in an instructional setting,
- b) *Interpreting* the perceived activities in class and
- c) *Decision making*, which either includes to anticipate a response or proposing alternative instructional strategies.”

Thus, the model of teachers’ professional competence underlying the TEDS-FU study includes these situation-specific skills in addition to knowledge and affect-motivational facets. The new test instruments developed for the TEDS-FU study assess these situation-specific skills with a video-based test instrument, which consists of three short video vignettes with corresponding questions. These three video vignettes show mathematics classroom situations and are followed by open and closed questions that assess whether the teacher perceive and interpret relevant aspects of the teaching sequence and whether they decide on adequate possibilities how to continue the situation or propose adequate alternatives. In addition to these newly developed instruments, the TEDS-FU study tested teachers’ knowledge and affect-motivational part using a reduced version of the TEDS-M test.

3. Methodological approach

In order to answer the two research questions formulated in section 2.2., we refer to different test parts from the two studies presented before. Teachers’ skills to identify quality features in students’ solutions and to support high-achieving students can be analyzed with data from the video-based instrument of TEDS-FU. The data from TEDS-M, which was implemented in the last year of teachers’ professional education, can give insight into the extent to which future teachers at the end of their studies have the knowledge to foster creativity and promote high-achieving students.

3.1. Assessment of primary mathematics teachers’ knowledge as a basis for identifying mathematical creativity and high-achieving students

We refer to test parts from the TEDS-M study that tested future teachers’ MCK and their MPCK. These test parts were implemented as a 60-minute paper-and-pencil test. The items assessing the teachers’ MCK covered the domains number, algebra, geometry and data as well as the three cognitive dimensions knowing, applying, and reasoning. The items assessing the teachers’ MPCK also covered the four content domains and referred in addition to MPCK of curricula and planning or to knowledge about how to enact mathematics in the context of teaching and learning. Thus, two facets were distinguished, one that becomes relevant for planning instruction and the other becomes relevant during class. The test included multiple choice items as well as open constructed response items (for details see Blömeke & Kaiser 2014). Scores were created for MCK and MPCK separately in one-dimensional models using item response theory (Blömeke & Kaiser 2014). These results will be used in the following

analyses as an indication of the teachers' preparation to identify and support creative and high-achieving mathematics students.

3.2. Assessment of primary school mathematics teachers' ability to identify and support creativity and high-achieving students

Teachers' answers to the TEDS-FU video-based instrument that assessed teachers' skills in a more situated way built the basis for evaluating whether they are able to identify quality characteristics in students' solutions and support these students' learning. Three short video vignettes show mathematics education in a German third grade classroom. Before watching the video sequence, the teachers receive context information about the mathematical content and the learning conditions of the students. After observing the classroom scene, the teachers are asked several questions concerning mathematics educational and general pedagogical aspects. The questions are presented in two format types: an open response format and rating scale items (example items are presented in figures 4 and 5). Based on the PID model, the questions either focus on perceiving particular events in the video, interpreting the perceived activities and deciding how to respond as well as proposing alternative instructional strategies. For the following analyses, we refer to two of the three video vignettes. In the first video vignette, which covers "Pascal's triangle", the students are working in an open learning environment. All students were asked to calculate and insert numbers into an empty Pascal's triangle. Subsequently, they were asked to color all even numbers and to find structures in the numbers and/or the coloring. The video vignette shows the students working on these tasks within their individual pace. The teacher finally asks some students to present their findings and selects one for continuation of the work. The video vignette stops at this point. This video sequence and its corresponding questions that require teachers to identify mathematical structures and patterns in the diverse students' findings is particularly suitable to analyze the teachers' ability to identify and support creative and high-achieving students.

The second video vignette that refers to these requirements covers "Geometry". Here, the students are confronted with Pentominos and are asked to find all possible figures and to determine the number of existing Pentominos. After the introductory scene, a student is shown, who presents her solution to the teacher.

All teachers' responses to the video instrument were coded. While extensive coding manuals were developed to evaluate the open response questions, several expert ratings generated the coding references for the rating scale items (see cf. Hoth et al. 2016).

We identified four questions that required the teachers to identify mathematically rich students' solutions and two questions that asked the teachers to support high achievement of students and their creativity. The difference between these two challenges can be explained by the different situation-specific skills that are required to solve the tasks. Identifying rich students' solution necessitates perceiving and interpreting while supporting creative and high-achieving students requires the teachers to decide how to continue their teaching (*decision making*) (see Blömeke et al. 2015, Kaiser et al. 2015, section 2.3.). Examples of these items are given below.

Pascal's triangle: Karola's discovery

This rating scale item referring to the video vignette "Pascal's triangle" asks the teachers to rate whether one of the students discovered a structure within the numbers. One girl presented that the second diagonal of Pascal's triangle contains the natural numbers (figure 3). The corresponding item refers to pattern recognition or identification of mathematical structures, which are highly important for fostering creativity and supporting mathematically talented students because teachers need to identify the mathematical quality and the creative potential of students' answers prior to using them effectively during class. This item was answered

correctly by 26% of the teachers who participated in TEDS-FU, 53% gave an incorrect response and there were 21% missing responses for this item. Thus, only about one quarter of the teachers identified the mathematical quality of the girl's discovery.

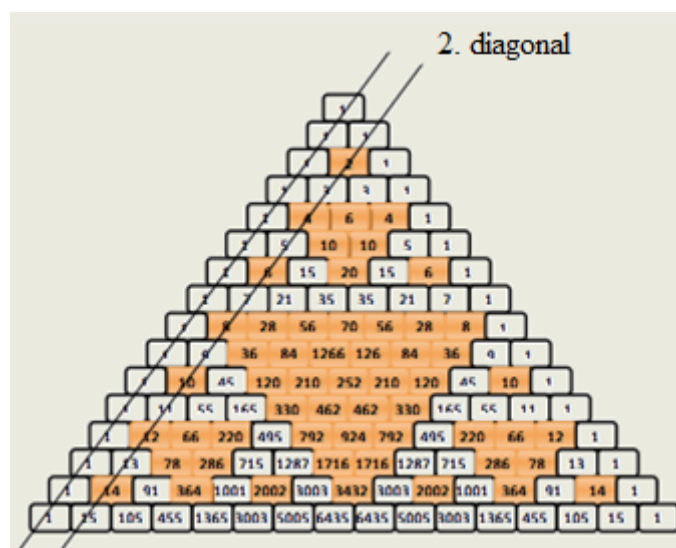



Figure 3: Patterns and structures in Pascal's triangle

Pascal's triangle: Kim's discovery

This rating scale item (see figure 4) asked the teachers, whether one of the presenting students formulates an if-then-sentence. One girl presents that adding two even numbers results in another even number and adding two odd numbers also results in an even number. Thus, she formulates the if-then-sentence "If I add two even numbers, then I get another even number" and "If I add two odd numbers, then I get an even number". Thus, she reasons about mathematical patterns and reasoning is an essential part of creative mathematical work. It can, therefore, be expected that knowledgeable test persons focus especially on this part of the video. Therefore, this item does not only evaluate remembering, but the expertise-guided noticing. Again, teachers need to identify the mathematical potential of the student's finding and abstract from her description the affected mathematical concepts.

All statements refer to the given video clips.
Please mark for each statement the level of your acceptance

Please make ONE choice per line

| | fully correct | partially correct | partially incorrect | not correct at all |
|--|-----------------------|-----------------------|-----------------------|-----------------------|
|  Kim formulates an if-then-sentence | <input type="radio"/> | <input type="radio"/> | <input type="radio"/> | <input type="radio"/> |




Figure 4: Rating scale item "Kim's discovery" referring to the video 'Pascal's triangle'

Geometry: Identifying problems in the teaching strategy

The teacher's introduction of Pentominos and their mathematical structure to the class is characterized by some problems. These cause mistakes in a student's solutions. In her solution, the student disregards the congruency of figures and she generates the different Pentominos based on only one specific Tetromino. This may be caused by several aspects of the teaching such as the material that the teacher presented to the class. This material did not enable the students to turn their Pentominos and, thus, the students were not able to test

congruency. There are about eight teaching elements that can be associated with the student's mistakes. The teachers in the study were asked to list three of these teaching elements. Mathematically correct concept introduction and the usage of rich examples are an indispensable condition for quality-oriented mathematics teaching in general. However, these aspects are especially important for creative and mathematically high-achieving students, who are immediately distracted by restricted or even wrong elaborations of mathematical concepts. In addition, the student in the video presents a creative and profound solution to the proof task. Thus, the teachers are demanded to identify its quality and ascribe the mistakes to the teacher's introduction.

Geometry: Identifying quality features in a student's solution

The student, who presents her solution to the teacher, not only makes mistakes but also develops an abstract mathematical model in answering the proof task. In addition, she gives reasons for her mathematical model on an abstract level. The teachers are subsequently asked to evaluate the quality of the students' solution and name three different aspects indicating its quality. The recognition of mathematical patterns and structures in students' solutions – as evaluated in this item – is especially essential to encourage and further students' creativity.

Pascal's triangle: Homework for a heterogeneous class

This question (see figure 5) asked the teachers to formulate homework. This homework ought to follow the video sequence and refer on the one hand to the content of the teaching sequence and on the other hand to the performance heterogeneity of the class. This item is based on a sound understanding of the students' solutions that contain various underlying mathematical patterns and structures and are generalized to certain degrees. To notice the variety of the proposed patterns and to identify their value is an important condition for formulating homework that fosters the displayed creativity and supports the talented students.

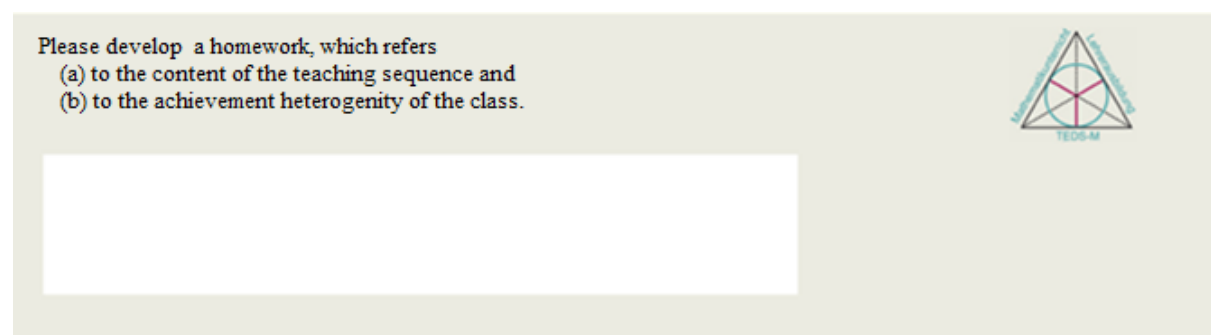


Figure 5: Open response item "Homework for a heterogeneous class" referring to the video 'Pascal's triangle'

Pascal's triangle: Continuing a student's answer

One of the students in the video presented as result of the work that the coloring of even numbers results in top-down triangle shapes while the shapes of the odd numbers look like bottom-up triangles. The teachers were asked to develop a challenging question that continues this student's discovery. This item addresses a profound mathematical finding of a student and demands the teachers to develop a reasonable question that optimally continues the student's approach.

4.3. Data analysis and sample

1032 primary mathematics teachers participated in TEDS-M and 131 were reassessed in TEDS-FU. The following analyses refer to these 131 primary mathematics teachers who participated in both studies and build the basis to evaluate, whether teachers are able to

identify and to promote high-achieving and creative students during class. With regard to the first research question, the teachers' scores in the MCK and MPCK tests of TEDS-M and their corresponding competence level provide insight into the teachers' professional knowledge. In order to evaluate the second research aim, solution frequencies of the selected questions are used to gain insight into teachers' abilities.

To examine the connection between teachers' preparation and their ability to identify and support high-achieving students, the teachers' MCK and MPCK scores will be linked with their scores on the selected tasks from the video instrument. Here, we use contingency analyses (see cf. Mayring 2015) to analyze these relations. We chose contingency analyses over correlation analyses because of the small number of competence levels. Especially with regard to teachers' MPCK, only two competence levels were distinguished. The use of the competence levels provides insight into the knowledge facets that the teachers possess or miss. Because not all teachers answered all items in both sets of data sets, the data basis in the contingency analyses is usually smaller than 131.

3. Results

The first section presents general results on teachers' preparation to support high-achieving and creative students before we continue to analyze more situation-specific skills.

5.1. Results regarding teachers' preparation at the end of teacher education

Only 50% of the German future teachers reached the highest MCK competence level in TEDS-M, a competence level strongly needed to promote giftedness, 40% were at competence level 2 and 10% at competence level 1. About 70% of the German future primary teachers were the lower MPCK competence level in TEDS-M, while only about 30% belonged to the higher level.

Based on the description of the competence levels in chapter 3, it can be assumed that teachers with MCK at the lowest and average competence levels will not be able to recognize or understand creative students' solutions and will not be able to support these students' mathematical learning processes. In addition, teachers who only reach the lower competence level in MPCK will not be able to offer learning opportunities for high-achieving and creative students, to develop different representations for a mathematical problem or choose different teaching strategies for their heterogeneous student body. Altogether, the German teachers – but not only them – show deficits regarding structural aspects of mathematics, logical reasoning and the analysis of students' answers. However, these aspects are of special importance, when teaching mathematically high-achieving and creative students. In the next section, we will analyze the teachers' ability to identify high-achieving and creative students' solutions.

5.2. Results concerning primary mathematics teachers' ability to identify and support high-achieving and creative students' solutions

The solution frequencies of the six selected questions from the TEDS-FU video analysis instrument are shown in table 1.

| | | Frequency of correct responses | Frequency of incorrect responses | Missing responses |
|---|--|--|----------------------------------|-------------------|
| Questions assessing teachers' ability to identify high-achieving and creative student's responses | Pascal's triangle: Karola's discovery | 26% | 53% | 21% |
| | Pascal's triangle: Kim's discovery | 34% | 46% | 20% |
| | Geometry: Identifying deficits in the teaching strategy of the teacher | Fully correct (three correct aspects): 8% | 14% | 20% |
| | | Partially correct (two correct aspects): 31% | | |
| | | Partially correct (one correct aspects): 27% | | |
| | Geometry: Identifying quality aspects in a student's solution | Fully correct (three correct aspects): 2% | 32% | 25% |
| | | Partially correct (two correct aspects): 8% | | |
| | | Partially correct (one correct aspects): 33% | | |
| Questions assessing teachers' ability to support high-achieving and creative students | Pascal's triangle: Homework for a heterogeneous class | 37% | 31% | 32% |
| | Pascal's triangle: Continuing a student's answer concerning its mathematical potential | 12% | 34% | 54% |

Table 1: Solution frequencies of the selected tasks from the TEDS-FU video analysis test

The results indicate that the early career teachers have difficulties identifying creative and high-achieving students' responses as well as supporting these learners. Only about one third of those teachers is able to understand and interpret these students' findings during classroom activities.

In order to analyze the hypothesized relation between teachers' content specific knowledge and their ability to identify and support creative and high-achieving students during class, the following section will connect both sets of data.

5.3. Connection between mathematics teachers' content knowledge and their ability to identify and support creative and high-achieving students

The results of the contingency analyses between the teachers' competence level regarding their MCK at the end of their professional education (TEDS-M data), the competence level of their MPCK at the end of their education (TEDS-M data) and their scores regarding questions that require the teachers to identify and support creative and high-achieving students in a classroom-like situation (TEDS-FU data) are shown in figures 6-9. For reasons of clarity, the teachers' ability to identify creative and high-achieving students' responses is given as a total

score, including the four questions “Karola’s discovery”, “Kim’s discovery”, “Identifying problems in the teaching strategy” and “Identifying quality features in a student’s solution”. This total score ranges from min=0 to max=6. Similarly, the total score including the two questions “Homework for a heterogeneous class” and “Continuing a student’s answer” (min=0, max=2) indicates the teachers’ ability to support high-achieving and creative students in the mathematics classroom. The figures 2-5 show the contingency analyses between the teachers’ professional knowledge facets (represented by the competence levels) and their ability to identify and support high-achieving and creative students (given as the total scores). Each figure shows the percentage of teachers in each of the competence levels and with the respective total scores.

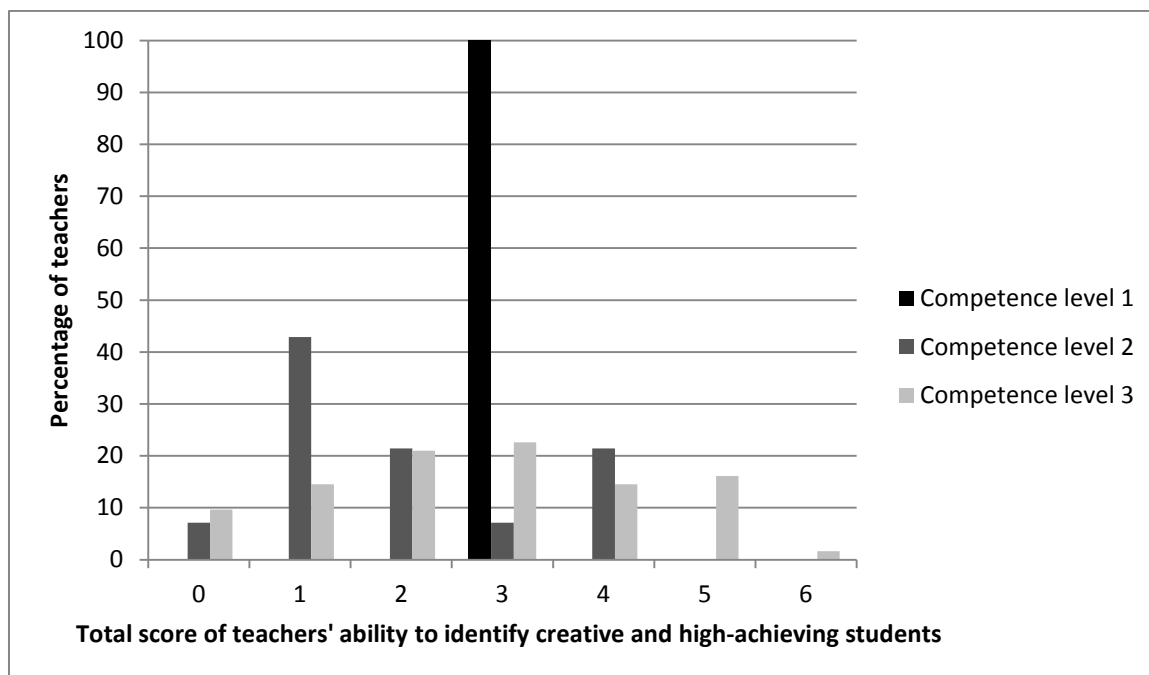


Figure 6: Contingency analysis between the primary teachers' MCK and their ability to identify creative and high-achieving students

Figure 6 shows the relation between the primary school teachers’ MCK at the end of their professional education and their ability to identify high-achieving and creative students. The figure indicates that only teachers of competence level 3 are able to achieve the highest scores (5 or 6) in tasks that require the identification of high-achieving and creative students’ responses during class. About 79% of those teachers with mathematical knowledge that is classified as competence level 2 were only able to achieve half or less of the maximal attainable score. These results indicate that teachers need profound content knowledge in order to identify complex and creative students’ solutions.

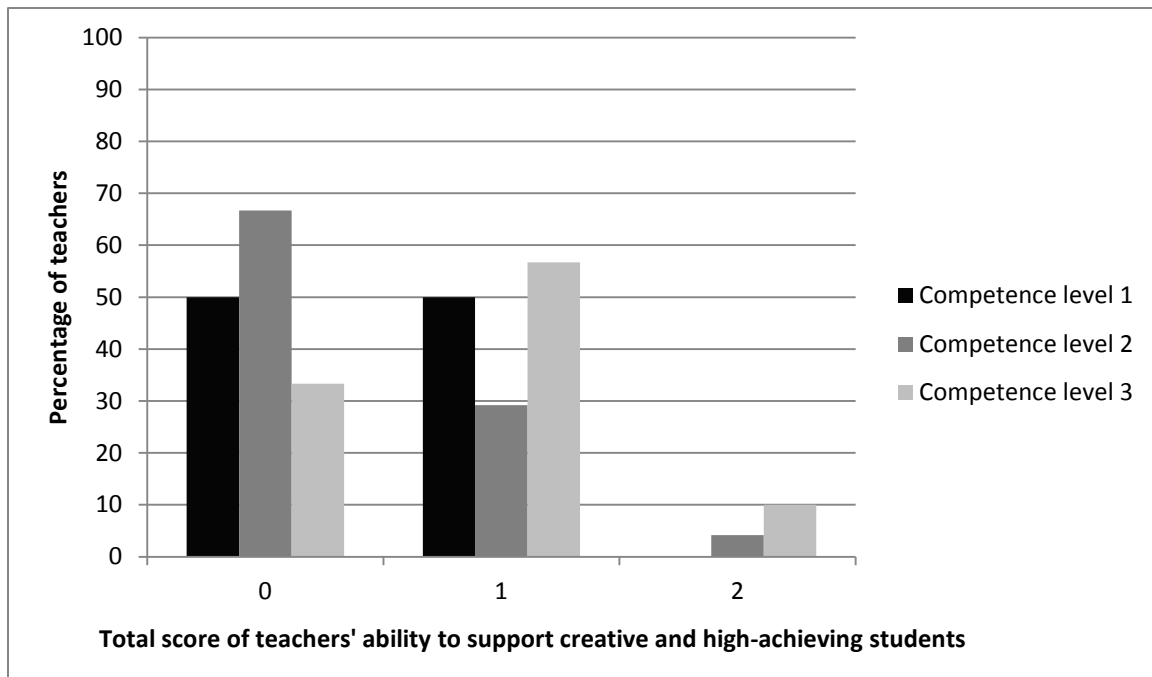


Figure 7: Contingency analysis between the primary teachers' MCK and their ability to support creative and high-achieving students

Figure 7 shows the contingency analysis between the teachers' MCK and their ability to support creative and high-achieving students. Teachers who were able to achieve the highest possible score in supporting creative and high-achieving students exclusively belonged to the competence levels 2 or 3. In addition, two third of the teachers at competence level 3 reached a score of 1 or 2, while this applied only to one third of the teachers whose MPCK was classified as competence level 2. Then again, no teacher in competence level 1 reached a full score, but 50% reached a score of 1.

This contingency analysis again indicates that there is a relation between the MCK of teachers and their ability to support creative and high-achieving students.

Figure 8 shows the connection between the primary teachers' MPCK at the end of their professional education and their ability to identify high-achieving and creative students in a classroom-like situation.

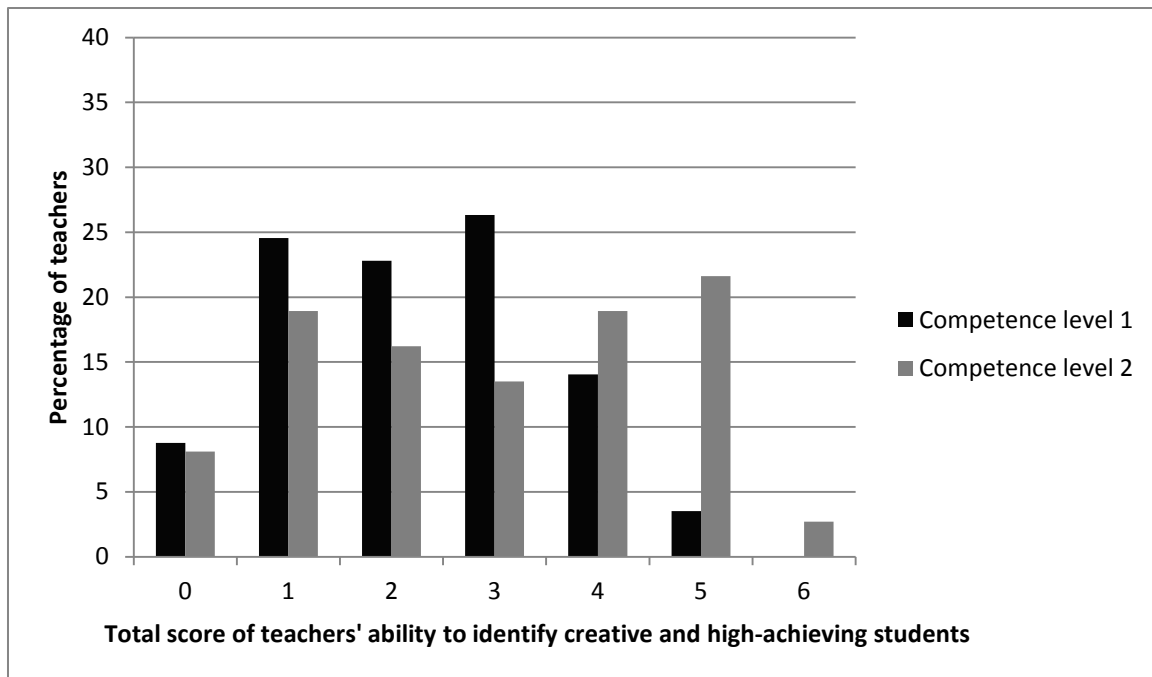


Figure 8: Contingency analysis between the primary teachers' MPCK and their ability to identify creative and high-achieving students

The figure also shows that about 82% of those teachers whose MPCK was classified as competence level 1 were only able to achieve half or less of the score that indicates their ability to identify high-achieving and creative students (one third of the teachers only reached a score of 0 or 1), whereas this is only true for about 57% of those teachers in competence level 2. Therefore, it indicates that the primary school teachers' MPCK is relevant to identify high-achieving and creative students during class.

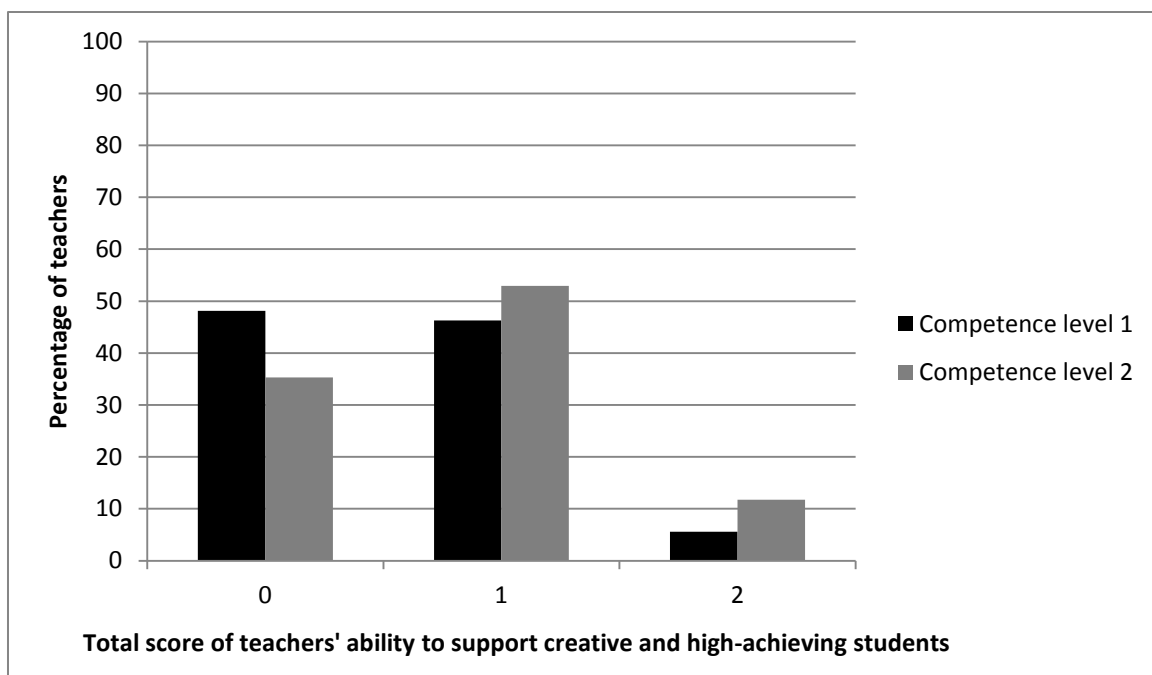


Figure 9: Contingency analysis between the primary teachers' MPCK and their ability to support creative and high-achieving students

With regard to teachers' ability to support creative and high-achieving students during class (see figure 9), the figure shows that 48% of the teachers in competence level 1 were not able to give adequate support (score 0) while this is only true for 35% of the teachers in competence level 2. Only about 6% of the teachers with MPCK at the competence level 1 reached a score of 2. Then again, this score was reached by about 12% of the teachers at competence level 2. This again indicates a relation between teachers' MPCK and their ability to support creative and high-achieving students during class.

6. Summary and discussion

Teachers must be equipped with professional competences to meet the various requirements that they encounter during class. Due to aspects of students' heterogeneity, one main challenge that they face is to teach the high-achieving and creative students as well as learners with great difficulties. In order to analyze whether primary mathematics teachers are able to identify and support high-achieving and creative students in the mathematics classroom and to analyze whether they were prepared to do that, data from the TEDS-M study and its Follow-Up (TEDS-FU) are analyzed. The TEDS-M study assessed mathematics teachers at the end of their professional education and provides information about the teachers' MCK as well as their MPCK that they bring from their teacher education. The TEDS-FU study is a German longitudinal Follow-Up that reassessed those teachers after four years of teaching experience. One of the instruments of the study – a video analysis instrument – assessed the teachers' situation-specific skills. For the purpose of analyzing the teachers' ability to identify and support creative and high-achieving students in class, six questions were selected from the video analysis test instrument that require the teachers to identify and further creative and high-achieving students' responses.

The data of about 131 primary school teachers who participated in TEDS-M gave insight into their knowledge to identify and support creative and high-achieving students while their data from the TEDS-Follow-Up study gave insight into their ability to identify and support creative and high-achieving students during classroom activities. The longitudinal design of the studies allowed for contingency analyses between both data sets. However, it may be noted at this point that the study presented in this article is a secondary analysis of the data of the TEDS-M and TEDS-FU study. Therefore, the selected questions were not developed with the aim of assessing teachers' knowledge and ability to identify and support creative and high-achieving students. This ability is represented in the present study by a quantitative score that results from the TEDS-FU coding process. Using this total score that described the amount of aspects answered "correct" for the purpose of the TEDS-FU study provides a first summarizing approach. Qualitative analyses of the teachers' individual responses might give additional and in depth information about the teachers' dealing with creative and high-achieving students but would exceed the present study at this point. The same applies to the scores resulting from the TEDS-M proficiency tests. These knowledge scores are generated from items spanning different content and cognitive subdomains. The scores, therefore, give comprehensive but also broad information about the teachers' professional knowledge. With regard to the intended research objective, it might be useful to additionally analyze the given requirements in detail.

The results from the TEDS-M proficiency tests regarding the teachers' MCK and their MPCK indicate that there are weaknesses in future teachers' content-specific knowledge concerning structural aspects of mathematics, logical reasoning and their analysis of students' answers. About half of the German future primary school mathematics teachers who participated in TEDS-M were likely to have more difficulty answering problems requiring more complex reasoning in applied or non-routine situations. However, this ability is essential in order to

teach high-achieving students and to foster their creativity. This is in accordance with the results regarding the solution frequencies of the selected tasks from the TEDS-FU video analysis instrument. The teachers especially showed difficulties in naming quality features of a student's solution and formulating a question continuing a student's presented mathematical discovery. However, these two requirements are of special relevance, when teaching creative and high-achieving students in mathematics.

The contingency analyses between the teachers' content-specific knowledge at the end of their teacher education and their ability to identify, interpret and support creative and high-achieving students in the mathematics classroom indicate a connection between the two components. Thus, teachers who are prepared with high content-specific knowledge at the end of their teacher education more often identify creative and high-achieving students' solution during class and they also offer more adequate learning possibilities for these creative learners. Therefore, teacher education programs as well as in-service teacher training should improve and take greater account of the mathematical and didactical aspects teachers need to understand a variety of possible student responses to a given mathematical problem. In our case, teachers would especially need mathematical knowledge to classify the responses and their mathematical value for the main mathematical idea which is in focus. Then again, they require MPCK to work with the given responses, value their representation and if necessary offer other forms of representation etc. Then again, mathematical knowledge is needed to optimally continue the students' mathematical ideas and discoveries, but also guiding the main mathematical idea and goal of the teaching sequence.

These findings are in accordance with many demands formulated in literature concerning the education of high-achieving and creative students (see cf. Mann 2006, Nadjafikhah et al. 2012). As Diezmann and Watters (2002; Watters & Diezmann 2000) point out, teachers require the ability to offer challenging tasks to creative and high-achieving students in order to support effective learning processes. This ability is especially focused in the two selected tasks from the TEDS-FU study that assess the teachers' ability to support creative and high-achieving students. The results regarding these questions show that the primary school mathematics teachers had great difficulties formulating continuing questions and homework that challenge creative and high-achieving students mathematically. Therefore, Nadjafikhah et al.'s (2012) demand to "pay deeper attention to train teachers especially improving teachers' ability to design and implement educational environments that promote creativity in mathematics" (ibid., p. 289) is emphasized by the present findings.

Concluding, the results show a great necessity for supporting teachers' professional dealing with creative and high-achieving students since many future and early career teachers seem to have strong deficits in providing an adequate mathematical education for creative and high-achieving students. In addition, the results show that teachers' ability to support these students is closely connected with their professional knowledge. This also implies that teacher education needs to impart extensive professional knowledge.

7. References

- Balka, D. S. (1974). Creative ability in mathematics. *Arithmetic Teacher*, 21, 633–636.
- Ball, D. L., Thames, M. H. & Phelps, G. (2008). Content knowledge for teaching: What makes it special? *Journal of Teacher Education*, 59(5), 389–407.
- Baumert, J., & Kunter, M. (2011). Das Kompetenzmodell von COACTIV. In M. Kunter, J. Baumert, W. Blum, U. Klusmann, S. Krauss & M. Neubrand (Eds.), *Professionelle Kompetenz von*

- Lehrkräften. Ergebnisse des Forschungsprogramms COACTIV* (pp. 29–53). Münster: Waxmann Verlag GmbH.
- Blömeke, S., Kaiser, G., & Lehmann, R. (Eds.) (2008). *Professionelle Kompetenz angehender Lehrerinnen und Lehrer: Wissen, Überzeugungen und Lerngelegenheiten deutscher Mathematikstudierender und –refendare: Erste Ergebnisse zur Wirksamkeit der Lehrerausbildung*. Münster: Waxmann.
- Blömeke, S., Kaiser, G. & Lehmann, R. (Eds.). (2010). *TEDS-M 2008: Professionelle Kompetenz und Lerngelegenheiten angehender Primarstufenlehrkräfte im internationalen Vergleich*. Münster: Waxmann Verlag.
- Blömeke, S., Kaiser, G., Döhrmann, M., Suhl, U., Lehmann, R. (2010). Mathematisches und mathematikdidaktisches Wissen angehender Primarstufenlehrkräfte im internationalen Vergleich. In S. Blömeke, G., Kaiser, & R. Lehmann (Eds.), *TEDS-M 2008: Professionelle Kompetenz und Lerngelegenheiten angehender Primarstufenlehrkräfte im internationalen Vergleich* (pp. 195-251). Münster: Waxmann Verlag.
- Blömeke, S., Hsieh, F.-J., Kaiser, G., & Schmidt, W. H. (Eds.). (2014). *International Perspectives on Teacher Knowledge, Beliefs and Opportunities to Learn*. Dordrecht, The Netherlands: Springer.
- Blömeke, S., & Kaiser, G. (2014). Theoretical Framework, Study Design and Main Results of TEDS-M. In S. Blömeke, S., F.-J. Hsieh, G. Kaiser, & W. H. Schmidt (Eds.). (2014). *International Perspectives on Teacher Knowledge, Beliefs and Opportunities to Learn* (pp. 19-47). Dordrecht, The Netherlands: Springer.
- Blömeke, S., Gustafsson, J.-E. & Shavelson, R. (2015). Beyond dichotomies: Competence viewed as a continuum. *Zeitschrift für Psychologie*, 223, 3–13.
- Bolden, D., Harries, A. & Newton, D. (2010). Pre-service primary teachers' conceptions of creativity in mathematics. *Educational Studies in Mathematics*, 73(2), 143–157.
- Buchholtz, N., Kaiser, G. & Blömeke, S. (2013). Die Erhebung mathematikdidaktischen Wissens: Konzeptualisierung einer komplexen Domäne. *Journal für Mathematikdidaktik*, 35, 101-128.
- Carter, K., Cushing, K., Sabers, D., Stein, P., & Berliner, D. C. (1988). Expert-novice differences in perceiving and processing visual information. *Journal of Teacher Education*, 39, 25-31.
- Depaepe, F., Verschaffel, L. & Kelchtermanns, G. (2013). Pedagogical content knowledge: A systematic review of the way in which the concept has pervaded mathematical educational research. *Teaching and Teacher Education*, 34, 12–25.
- Diezmann, Carmel M and Watters, James J (2002) Summing up the education of mathematically gifted students. In *Proceedings 25th Annual Conference of the Mathematics Education Research Group of Australasia*, pages 219-226, Auckland.
- Diezmann, C. M., & Watters, J. J. (2000). Catering for mathematically gifted elementary students: Learning from challenging tasks. *Gifted Child Today*, 23(4), 14-19, 52.
- Hattie, J. A. C. (2009). *Visible learning: A synthesis of over 800 meta-analyses relating to achievement*. London, UK: Routledge.
- Haylock, D. W. (1987). A framework for assessing mathematical creativity in school children. *Education Studies in Mathematics*, 18(1), 59–74.
- Hong, E., & Aquí, Y. (2004). Cognitive and motivational characteristics of adolescents gifted in mathematics: Comparisons among students with different types of giftedness. *Gifted Child Quarterly*, 48, 191–201.
- Hoth, J., Schwarz, B., Kaiser, G., Busse, A., König, J. & Blömeke, S. (accepted for publication). Uncovering predictors of disagreement: Ensuring the quality of expert ratings. *ZDM – The International Journal on Mathematics Education*.

- Kaiser, G., Busse, A., Hoth, J., König, J., & Blömeke, S. (2015). About the complexities of video-based assessments: Theoretical and methodological approaches to overcoming shortcomings of research on teachers' competence. *International Journal of Science and Mathematics Education*, 13(2), 369–387.
- Klieme, E., Maag Merki, K. (2008). Introduction of Educational Standards in German-speaking countries. In: J. Hartig, E. Klieme, D. Leutner (Eds.), *Assessment of competences in educational contexts* (pp. 305-314). Göttingen: Hogrefe.
- Krutetskii, V. A. (1976). *The psychology of mathematical abilities in school children*. Chicago: University of Chicago Press.
- Kunter, M., Baumert, J., Blum, W., Klusmann, U., Krauss, S. & Neubrand, M. (Eds.). (2011). *Cognitive activation in the mathematics classroom and professional competence of teachers. Results from the COACTIV project*. New York, NY: Springer.
- Li, Y. & Kaiser, G. (Eds.) (2011). *Expertise in Mathematics Instruction: An International Perspective*. New York, NY: Springer.
- Mann, E. L. (2006). Creativity: The essence of mathematics. *Journal for the Education of the Gifted*, 30(2), 236–260.
- Mann, E. L. (2009). The Search for Mathematical Creativity: Identifying Creative Potential in Middle School Students. *Creative Research Journal*, 21(4), 338–348,
- Mayring, P. (2015). Qualitative Content Analysis: Theoretical Background and Procedures. In A. Bikner-Ahsbahr, C. Knipping, & N. Presmeg (Eds.). *Approaches to Qualitative Research in Mathematics Education. Examples of Methodology and Methods* (pp. 365-380). Dordrecht: Springer.
- Nadjafikhah, M., Yafian, N. & Bakhshalizadeh, S. (2012). Mathematical creativity: some definitions and characteristics. *Procedia - Social and Behavioral Sciences*, 31, 285 – 291.
- Peterson, P., Fennema, E., Carpenter, T. P. & Loef, M. (1989). Teachers' pedagogical content beliefs in mathematics. *Cognition and Instruction*, 6, 1–40.
- Renzulli, J. S. (2004). Introduction to Identification of Students for Gifted and Talented Programs. In J. S. Renzulli & S. I. Reis (Eds.), *Essential Readings in gifted education: Identification of students for gifted and talented programs* (pp. xxxiii-xxxiv). London, Sage.
- Richardson, V. (1996). The role of attitudes and beliefs in learning to teach. In J. Sikula, T. Buttery, & E. Guyton (Eds.), *Handbook of research on teacher education* (pp. 102-119). New York: Macmillan.
- Rotigel, J. & Fello, S. (2004). Mathematically Gifted Students: How Can We Meet Their Needs? *Gifted child today*, 27, 46–51.
- Shayshon, B., Gal, H., Tesler, B. & Ko, E.-S. (2014). Teaching mathematically talented students: a cross-cultural study about their teachers' views. *Educational Studies in Mathematics*, 87, 409–438.
- Sherin, M. G., Jacobs, V. R. & Philipp, R. A. (Eds.). (2011). *Mathematics teacher noticing. Seeing through Teachers' eyes*. New York, NY: Routledge.
- Shulman, L. S. (1986). Those who understand: Knowledge growth in teaching. *Educational Researcher*, 15(2), 4–14.
- Shulman, L. S. (1987). Knowledge and teaching: Foundations of the new reform. *Harvard Educational Review*, 57, 1–21.
- Tatto, M.T., Schille, J., Senk, S.L., Ingvarson, L., Rowley, G., Peck, R., Bankov, K., Rodriguez, M., & Reckase, M. (2012). *Policy, practice, and readiness to teach primary and secondary mathematics in 17 countries: Findings from the IEA Teacher Education and Development Study in Mathematics (TEDS-M)*. Amsterdam: IEA.

- Thompson, A. G. (1992). Teachers' beliefs and conceptions: A synthesis of the research. In D. A. Grouws (Ed.), *Handbook of research on mathematics teaching and learning* (pp. 127–146). Reston, VA: National Council of Teachers of Mathematics.
- Wagner, H. & Zimmermann, B. (1986). Identification and fostering of mathematically gifted children. In A. J. Cropley, K. K. Urban, H. Wagner, & W. Wiczerkowsky (Eds.), *Giftedness: A continuing worldwide challenge* (pp. 273-284). New York: Trillum Press.
- Weinert, F. E. (2001). Concept of competence: a conceptual clarification. In D. Rychen, & L. Salganik (Eds.), *Defining and selecting key competencies* (pp. 45-65). Seattle: Hogrefe and Huber.