A weak lensing analysis of the PLCK G100.2-30.4 cluster

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1. Introduction

Clusters of galaxies are a crucial probe for a variety of key cosmological topics. Among their many applications, knowledge of the mass function and its redshift evolution allows constraints to be put on the matter power spectrum and limits to be set on several cosmological parameters. The construction of the cluster mass function generally involves the following steps: 1) clusters should be identified in large surveys; 2) mass proxies should be used to estimate their masses; and 3) the mass function should be constructed by counting clusters in given mass and redshift bins. This process relies on the fundamental assumption that the scaling relations between the mass and its proxies are well calibrated and unaffected by selection biases (or that the biases have been accounted for). It has been successfully implemented both by using X-rays surveys such as the ROSAT All-Sky Survey, where proxies like the gas mass, the temperature, or the X-ray luminosity have been used to estimate the masses (e.g. Vikhlinin et al. 2009; Mantz et al. 2010), and in optical photometric optical surveys, for example the SDSS, where the masses are usually derived from the cluster richness (e.g. Rozo et al. 2009). More recently, searches for galaxy clusters have been started via the detection of the Sunyaev-Zel’dovich (SZ) effect on the photons of the cosmic microwave background. The newly established millimetric observatories, both ground-based (South Pole Telescope and Atacama Cosmology Telescope) and space-based (Planck), have provided catalogues of hundreds to thousands of clusters. The first cluster detections from the Planck all-sky survey were released in the Planck Early SZ sample (Planck Collaboration VIII 2011). A crucial part of the validation process involved the use of snapshot XMM-Newton observations; in the first two campaigns, 21 out of 25 newly identified cluster candidates were confirmed to be real (Planck Collaboration IX 2011).

The XMM-Newton snapshot observations appeared to reveal a class of massive clusters with low X-ray luminosity and disturbed morphology, which may indicate a population of massive clusters that are under-represented in X-ray surveys. Since the cluster masses in SZ surveys are estimated from the integrated Compton Y parameter via scaling relations calibrated with optical or X-ray observations, this may have an effect on the estimate of the mass function, and thus our understanding of cluster growth and evolution. It is therefore of fundamental importance to study these systems in more detail.

Lensing is a powerful method for recovering the surface density field of clusters, thus allowing the spatial distribution of dark matter to be traced. Simulations have shown that provided widefield observations of excellent quality are available, lensing allows an accurate measurement of the mass profile of clusters...
In this paper we describe the first weak lensing analysis of the cluster PLCK G100.2-30.4 (hereafter PLCKG100), based on deep Subaru SuprimeCam images. PLCKG100 was detected via the SZ effect in the first ten months of the Planck survey and was confirmed by XMM-Newton X-ray observations (Planck Collaboration IX 2011). The cluster redshift was estimated by optical gri observations performed with the 0.80 m IAC80 telescope, and through X-ray spectroscopic observations of the Fe K line, giving $z_{\text{phot}} = 0.38 \pm 0.04$ and $z_K = 0.31 \pm 0.04$, respectively (Planck Collaboration IX 2011). The cluster mass estimate, derived from XMM-Newton X-ray observations via iteration about the $M_{500}-Y_X$ relation of Arnaud et al. (2010), is $M_{500} = (5.60 \pm 0.22) \times 10^{14} \, M_\odot$, and the [0.1–2.4] keV X-ray luminosity was $L_{500} = (3.36 \pm 0.08) \times 10^{44} \, \text{erg s}^{-1}$.

Here we use deep (1 h) r-band and shallower (~30 min) giz images obtained with SuprimeCam at the Subaru telescope to derive the mass of the cluster by weak lensing. The paper is organized as follows. A summary of the observations and data reduction strategy is presented in Sect. 2. Techniques adopted for star/galaxy separation are described in Sect. 3. A comparison with cluster properties derived by optical photometry is given in Sect. 4. The weak lensing analysis is discussed in Sect. 5. We attempt to refine the hydrostatic mass estimate from XMM-Newton data in Sect. 6. Summary and conclusions are given in Sect. 7.

A standard concordance cosmology was adopted: $\Omega_\Lambda = 0.7$, $\Omega_M = 0.3$, $H_0 = 70 \, \text{km s}^{-1} \, \text{Mpc}^{-1}$, giving a scale of 4.7 kpc/arcsec at the redshift of PLCK G100.2-30.4 ($z = 0.36$, as derived in Sect. 4).

2. Observations and data reduction

PLCKG100 (Fig. 1, Fig. 2) was observed in the second part of the night on July 23, 2012, in the griz bands, with the wide-field Suprime-Cam camera (Miyazaki et al. 2002) mounted at the 8 m Subaru telescope. The camera is composed of 10 CCDs, each with 2048 × 4096 pixels and pixel scale 0.207, allowing coverage of a field of $34' \times 27'$. A sequence of 180 s exposures was obtained following the dithering pattern recommended for SuprimeCam. The deepest (1 h) image was taken in the r-band, to be used for the lensing analysis, with optimal seeing conditions (~0.5 arcsec). Images in g and i were obtained with a total exposure time of 1800 s as planned, while due to technical reasons only 8 out of the 10 planned exposures could be done in $z$, for a total exposure of 1440 s. Details of the observations are reported in Table 1.

The prereduction (overscan correction, bias, flat-fielding and masking of bad columns and autoguider) was based on the SDFRED2 (Yagi et al. 2002; Ouchi et al. 2004) pipeline developed for Suprime–Cam.

The tool ASTROMC (Romano et al. 2010) was then used to compute the astrometric solution describing the deformations in the field of view of individual exposures. For each filter, the astrometric solution was computed taking the NOMAD catalogue as reference, and at the same time minimizing the differences in the position of the same sources measured in different exposures; this allowed us to obtain an internal accuracy of ~0.01 arcsec, better than the accuracy of the NOMAD catalogue (rms ~ 0.2 arcsec). Images were then resampled and finally coadded using the SWarp software1 (Bertin 2010).

Photometric calibration was done by observing a field selected from the Stripe 82 area, and using the SDSS Stripe 82 Standard Star Catalog (Ivezić et al. 2007) to derive photometric zero points and SuprimeCam vs. SDSS colour terms. Limiting magnitudes for point-like sources at signal-to-noise levels of $S/N = 5$, 10 were computed as in Radovich et al. (2004): simulated images with the same depth and background rms as each science image were produced using SKYMAKER2 software, and stars were added at random positions; errors on magnitudes were computed from the difference between input and measured

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1. [http://www.astromatic.net/software/swarp](http://www.astromatic.net/software/swarp)
2. [http://www.astromatic.net/software/skymaker](http://www.astromatic.net/software/skymaker)
Table 1. Summary of the observations.

<table>
<thead>
<tr>
<th>Date</th>
<th>Band</th>
<th>Number</th>
<th>Total time</th>
<th>Average seeing (arcsec)</th>
<th>mag(σ = 10)</th>
<th>mag(σ = 5)</th>
</tr>
</thead>
<tbody>
<tr>
<td>23/07/2012</td>
<td>g</td>
<td>10</td>
<td>1800 s</td>
<td>0.7</td>
<td>24.9</td>
<td>25.6</td>
</tr>
<tr>
<td>23/07/2012</td>
<td>r</td>
<td>20</td>
<td>3600 s</td>
<td>0.5</td>
<td>25.5</td>
<td>26.5</td>
</tr>
<tr>
<td>23/07/2012</td>
<td>i</td>
<td>10</td>
<td>1800 s</td>
<td>0.6</td>
<td>24.7</td>
<td>25.2</td>
</tr>
<tr>
<td>23/07/2012</td>
<td>z</td>
<td>8</td>
<td>1440 s</td>
<td>0.6</td>
<td>23.8</td>
<td>24.7</td>
</tr>
</tbody>
</table>

Notes. The average seeing measured on the coadded images, and limiting magnitudes for pointlike sources at $S/N = 5$, 10 are also reported.

...magnitudes, and were used to derive the median magnitude for each value of $S/N$.

In addition to the stacked image obtained as described above, we also produced a set of stacks where the point spread function (PSF) was homogenized to the same Gaussian shape for all filters. This was done as follows:

1. For each exposure, all CCD images were first regridded and combined in one image using SWarp, adopting the same centre, pixel scale, and size as the coadded $r$-band stack derived above.
2. For each image, stars were identified and the PSF fitted as a function of pixel coordinates using the PSFEX software\(^3\) (Bertin \& Arnouts 1996) in dual mode, taking the $r$-band as the detection image, and measuring the photometry on the convolved stacks.
3. The PSFMATCH task in IRAF was used to compute the kernel that transforms the PSF into a Gaussian with the target FWHM, chosen to be 0.9 arcsec, the worst seeing value measured in all exposures and bands; since the PSF changes across the field, we divided each image into sections of $100 \times 100$ pixels, and computed the kernel in each of them.
4. For each filter, all convolved exposures were finally summed together.

These PSF-homogenized stacks were used for the photometric measurements only, not for shape measurements, for which we used the unconvolved $r$-band image. A multi-band photometric catalogue was extracted by running SExtractor\(^4\) (Bertin \& Arnouts 1996) in dual mode, taking the $r$-band as the detection image, and measuring the photometry on the convolved stacks.

The Galactic dust extinction in the field covered by SuprimeCam was computed using the Schlegel maps (Schlegel et al. 1998), obtaining an average value and rms: $E_{B-V} = 0.12 \pm 0.01$. For each galaxy, observed magnitudes were corrected in each filter by adopting the dust extinction computed at its position.

### 3. Star-galaxy classification

The selection of non-saturated stars and galaxies was undertaken in the magnitude ($M_{\text{AUTO}}$) vs. size ($\delta = \text{MU\_MAX} - \text{MAG\_AUTO}$) space (Huang et al. 2011). MU\_MAX is the peak surface brightness above background, which is constant for saturated stars. As in Huang et al. (2011), we rejected those sources with $\delta$ lower than for stars as spurious detections.

As a test of both the photometric accuracies and of the star-galaxy classification, we compared the $g - r$ and $i - z$ observed colours of stars with those derived at the Galactic plane position of PLCKG100 by the TRILEGAL code (Girardi et al. 2005, 2012). TRILEGAL allows the simulation of broad-band photometry of stars in any Galaxy field. The effect of the Galaxy dust extinction on stellar colours was also included in the models, starting from the average and rms $E(B - V)$ values derived from the Schlegel maps, and assigning to each simulated star a random value within this distribution. The transmission curves obtained by the combination of Subaru/SuprimeCam CCD, telescope, atmosphere, and filter contributions were adopted. Model and observed stellar colours are shown in Fig. 3. The zero point offsets required to optimize the overlap of observed and model colours are $+0.038 \text{ mag (g)}, -0.030 \text{ mag (r)}, -0.023 \text{ mag (i)},$ and $-0.016 \text{ mag (z)}$.

Stars with $S/N > 100$ were extracted and used in the PSFEX software, designed to model the PSF variations in astronomical images. The code allows the pixel-by-pixel PSF intensity to be modelled by a polynomial in a stamp of a given size as a function of the position in the field of view. Starting from this model, we can build a PSF stamp at each galaxy position, and derive the terms needed for the PSF correction of ellipticities, as described in Sect. 5.1. Different combinations of polynomial orders and stamp sizes were tried; based on the analysis of the residuals of the correction of the anisotropic PSF component (see Sect. 5.1), we selected a polynomial of order 6 and stamps with a size of $20 \times 20$ pixels ($\sim 5 \times \text{FWHM}$).

### 4. Cluster photometric properties

Figure 2 shows the composite $gri$ image of the cluster field: the ten brightest galaxies within 1 arcmin from the X-ray peak

\(^3\) http://www.astromatic.net/software/psfex
\(^4\) http://www.astromatic.net/software/sExtractor
(Planck Collaboration IX 2011) are marked. Two galaxies of similar brightness \((r \sim 18.20\) mag) are present in this region. We select as the centre of the cluster the galaxy that lies closest to the X-ray peak, and identify it as the brightest cluster galaxy (BCG). Several strong–lensing gravitational arcs are also visible, the brightest of which lies at \(\sim 40\) arcsec from the BCG. Another lies at \(\sim 60\) arcsec from the BCG.

\[ r \text{ vs. } g \text{–} r \text{ colour plot of galaxies in the field. Galaxies classified as likely cluster members from their colours are plotted as green dots; the red dot is the BCG galaxy. The best fitting red sequence line is overplotted.}\]

4.1. Red sequence

We selected the galaxies located in the inner 5 arcmin around the BCG that were classified as cluster members according to their colours, as described in Sect. 5.2. The red sequence, \(g - r = a + b r\), was fitted by a biweight algorithm, giving \(a = 2.6, b = -0.05\) (Fig. 4). Early-type galaxies were selected as those lying within \(2\sigma\) from the best fitting line. Photometric redshifts were computed using the ZEBRA code (Feldmann et al. 2006): the cluster redshift, derived from the average photo-z of \(r < 22\) mag cluster members, is \(z = 0.36 \pm 0.08\). For comparison, we obtain \(z = 0.41 \pm 0.10\) from the Sloan Digital Sky Survey (SDSS) photometric redshifts (DR9).

4.2. Richness

The parameter \(N_{200}\), i.e. the richness of the cluster within \(r_{200}\), was derived both from the selection of red-sequence cluster galaxies, and by making a statistical background subtraction. We used the \(r_{200}\) derived from the weak lensing analysis detailed in Sect. 5: \(r_{200} \sim 6\) arcmin. Absolute \(r\)-band magnitudes and \(k\)-corrections were computed for all galaxies with the cluster redshift, \(z = 0.36\), and to a magnitude limit of \(M_{\text{abs}} = -20\) mag. The richness derived from the selection of red sequence galaxies produces \(N_{200} = 150\). The richness estimate based on statistical background subtraction was done following Popesso et al. (2005); the density of background and foreground galaxies was then computed in each of the 20 sectors in an annulus with thickness 0.1 deg, starting at \(r_{200} + 0.1\) deg. Sectors with too few galaxies were rejected, and the average density was finally computed, giving the number of background/foreground galaxies in the \(r_{200}\) area of the cluster. In this way, we derived a richness \(N_{200} \sim 135\).

The richness can be translated to a mass estimate using e.g. Eq. (16) in Andreon & Hurn (2010): \(\log M_{200} = (0.96 \pm 0.15) (\log N_{200} - 1.5) + 14.36 \pm 0.04\). From these two consistent values of the richness, a mass \(\log M_{200} \sim (15.0 \pm 0.1) M_\odot\) is derived.

5. Weak lensing analysis

5.1. Shape measurement

The derivation of the shear, and the correction of the effect of the PSF on galaxy shapes, is based on the Kaiser, Squires, and Broadhurst approach (Kaiser et al. 1995, hereafter KSB). In the last decade there has been a dedicated effort to develop new algorithms to improve the accuracy in shape measurement (see Kitching et al. 2012, for a comprehensive review), which is crucial in particular in order to derive cosmological parameters from weak gravitational lensing (cosmic shear). However, KSB is still widely used in the case of the analysis of massive structures such as galaxy clusters (see e.g. Okabe et al. 2010; Hoekstra et al. 2012; Umetsu et al. 2014; Applegat et al. 2014). Our implementation follows that described in Huang et al. (2011) with some differences, which are outlined below.

The KSB algorithm is based on the measurement of the following quantities for each galaxy, derived from the source brightness moments: the source ellipticity vector \(e_{\text{obs}}\), and the source anisotropic polarizability (Panh) and shear polarizability (Psh) tensors.

The source ellipticity corrected for the anisotropic component of the PSF, \(e_{\text{aniso}}\), is first derived as

\[
e_{\text{aniso}} = e_{\text{obs}} - P_{\text{aniso}}^e\]

\[
p = e_{\text{obs}} / P_{\text{aniso}}^e\]

where starred terms indicate that they are derived from the measurement of stars. This is then related to the unknown intrinsic ellipticity \(e\) of the source and to the reduced shear, \(g = \gamma / (1 - \kappa)\), by

\[
e_{\text{aniso}} = e + \gamma^r g\]

where \(\gamma^r\) the effect of the (isotropic) seeing is corrected by the term \(\gamma^r\), dubbed by Luppino & Kaiser (1997) as the pre-seeing shear polarizability:

\[
\gamma^r = P_{\text{sh}} - P_{\text{aniso}}^\gamma \equiv P_{\text{sh}} - P_{\text{aniso}}^\gamma.
\]

The tangential and cross components of the reduced shear, \(g_t\) and \(g_x\), are defined as

\[
g_t = -g_1 \cos 2\varphi - g_2 \sin 2\varphi; \quad g_x = -g_1 \sin 2\varphi + g_2 \cos 2\varphi.
\]

\(\varphi\) being the position angle of the galaxy with respect to the assumed cluster centre.

The source brightness moments are weighted by a window function to suppress the outer parts of the galaxies, which are noise dominated. As in Huang et al. (2011), the window function

\[\text{In the following, the vector components along the } X\text{- and } Y\text{-axes are denoted } e_1\text{ and } e_2\text{, respectively.}\]
The uncertainty on the corrected ellipticities, $\Delta e_{\text{iso}}$, derived by PSFex, and fit them as a function of the position.

For each galaxy, we adopted the same weight definition as in Huang et al. (2011),

$$w = \frac{1}{\Delta e_0^2 + \Delta e_{\text{iso}}^2},$$

(7)

where $\Delta e_0 \sim 0.3$ is the typical intrinsic rms of galaxy ellipticities. The uncertainty on the corrected ellipticities, $\Delta e_{\text{iso}}$, was computed following a numeric approach. For each star used in the PSF fitting, we compute the difference between the correction terms measured on the real stars and on the PSF model derived by PSFex, and fit them as a function of the position.

This allows the estimation of an uncertainty on the stellar correction terms at each galaxy’s position. $N$ values of $e_{\text{iso}}$ were then computed (e.g. $N = 100$), randomly drawing both the observed source ellipticity and the stellar correction terms from a Gaussian distribution built from their errors. The error on $e_{\text{iso}}$ used to compute the weight was taken to be the rms of these values.

Sources with $SNe < 5$ were rejected from the analysis. We further excluded those galaxies with $P_\gamma < 0.1$, for which the PSF correction of the ellipticity is less reliable.

The final output of the pipeline is the vector $e_{\text{iso}} = e_{\text{aniso}}/P_\gamma$. Provided that the average intrinsic ellipticity vanishes, $\langle e \rangle = 0$, the average reduced shear is $\langle g \rangle = \langle e_{\text{iso}} \rangle$; it is therefore common to set $g = e_{\text{iso}}$.

As first pointed out by Hoekstra et al. (1998), it is important to adopt the same size of the window function to compute the galaxy ellipticities and the stellar correction terms used for the PSF correction. In Huang et al. (2011) we computed the stellar terms in bins with $\theta$ varying between the minimum and maximum values allowed for the size of the galaxies (2 and 10 pixels, respectively), with a step of 0.5 pixels. For each bin, they were then fitted by a polynomial, as a function of pixel coordinates, so that they could be derived at the position of each galaxy. This approach presents some disadvantages: (i) it is necessary to make a polynomial fit for each PSF correction term and for each window function size; (ii) large window sizes increase the amount of noise in the measurement of moments, even if we are using bright stars, which may contribute to different biases as a function of galaxy size. A more recent approach consists of modelling the PSF (Bergé et al. 2012), enabling us to reproduce the PSF at each galaxy’s position; this is now feasible with accuracies (Kitching et al. 2013) $\sigma(e) < 10^{-3}$. To this end, here we used the PSFEX software, which allows modelling of the PSF as a linear combination of basis vectors and fits their coefficients with a polynomial as a function of the pixel position. For each galaxy position, PSF correction terms are then derived using exactly the same window function adopted for that galaxy. A similar approach was adopted in Gruen et al. (2013), who showed that using PSFEX to model the PSF provides the accuracy required for weak lensing analysis of galaxy clusters. The accuracy of the PSF fitting was checked by deriving the anisotropy corrected ellipticities for stars, and verifying the absence of systematic effects in the residuals across the field of view (see Fig. 5).

Using a polynomial of order 6 as described above, we obtained $\langle e_{\text{aniso}} \rangle = (6 \pm 2) \times 10^{-4}$, $\langle e_{\text{aniso}}^2 \rangle = (2 \pm 1) \times 10^{-2}$. Figure 6 shows the tangential component of the average stellar ellipticity before and after the anisotropic correction ($\langle \Delta e \rangle = 6 \times 10^{-4}$), at different distances from the cluster centre. All of the steps outlined above are implemented in the LENS pipeline introduced in Huang et al. (2011).
5.2. The background sample

The dilution bias introduced by unlensed galaxies in the sample used for the shape measurement can adversely affect the cluster mass estimate. To minimize the contamination of this sample by unlensed sources, we followed the approach described in Formicola et al. (2014). Using the galaxy catalogue with photometry in griz bands, we identified background populations, cluster members, and foreground populations in a colour-colour diagram derived by choosing the appropriate combination of colours to be investigated.

Our selection in the colour-colour (CC) space was based on the simultaneous analysis of galaxy colours and of the shear signal of the galaxies selected as background sources. We used the photometric data from the Cosmic Evolution Survey (COSMOS; Ilbert et al. 2009) to train the colour selection. The accurate photometric redshifts of the sample allow a careful characterization of the distribution of the galaxies belonging to different redshift ranges in CC space. At the same time, we tuned the colour cuts to maximize the amplitude of the tangential shear component (Eq. (5)) measured from the background sources.

Starting from the $i-z$ vs. $g-r$ CC plot of the COSMOS galaxies, we defined criteria based on colour and magnitude cuts allowing each galaxy population in the PLCKG100 images to be identified. To this end, we computed the distance $d$ of each galaxy in the $i-z$ vs. $g-r$ diagram from the line represented in Fig. 7 (upper panel). This line (derived as described in Formicola et al. 2014) separates the overdense region mainly populated by sources at low redshift, from the overdense region mainly populated by sources at redshift higher than that of the cluster.

The background population was selected according to the following criteria:

- galaxies with: $24.5 < r < 26.5$ mag;
- or: $d < 0$, $21.8 < r < 24.5$ mag, $i-z > 0.1$;
- or: $d \geq 0$, $21.5 < r < 24.5$ mag, $i-z < -0.3$.

The foreground and the cluster member populations were identified according to these criteria:

- foreground galaxies: $d \geq 0$, $21.0 < r < 24.5$ mag, $-0.1 < i-z < 0.1$;
- cluster member galaxies: $d \geq 0$, $r < 23.5$ mag, $0.65 < g-r < 2.0$, $0.1 < i-z < 0.5$.

The total sample of background galaxies is represented with magenta dots in Fig. 7 (upper panel), while foreground and cluster galaxies are marked with green and orange dots, respectively. Radial number density profiles for each identified population are shown in Fig. 7 (bottom panel). The radial number density profiles for cluster member sources (orange triangles) indicate a clear identification of the cluster member population as shown by the high clustering at small radii. As expected, the foreground population (green diamonds) appears uniformly distributed. The background sample (magenta squares) shows a drop in number counts towards the cluster centre, which is expected owing to the so-called magnification bias (Broadhurst et al. 2008). Also displayed in Fig. 7 is the depletion in counts expected for a Navarro-Frenk-White profile (Navarro et al. 1996, hereafter NFW) with the parameters derived by the weak lensing analysis in Sect. 5.4, showing good consistency with the observations.

Using the photo-$z$ derived by Ilbert et al. (2009), we extracted the redshift distribution of the COSMOS galaxies with colour and magnitude cuts describing the background population needed for the evaluation of the critical density in the weak lensing analysis as described in Sect. 5.4.

5.3. Simulations

The ellipticities derived from most of the available shape measurement algorithms are affected (see Heymans et al. 2006, and references therein) by a multiplicative ($m$) and an additive ($c$) bias defined as $e_{\text{obs}} = e_{\text{true}} + m e_{\text{true}} + c$. The value of $m$ depends on the PSF type, as well as on the brightness and size of the galaxies, and in the case of KSB it is typically around 10–20% (Heymans et al. 2006).

To investigate this, we produced simulations using the GalSim software (Rowe et al. 2015), which was specifically designed to simulate sheared galaxies within the GREAT effort (see Mandelbaum et al. 2014, and references therein). GalSim offers the possibility of using both analytic models for the galaxies, and/or a sample of 260 000 real galaxies from Hubble Space Telescope COSMOS data. In addition, it can take as input the model produced by PSFex, and hence can produce an image with the same PSF shape and spatial variations as the real image.

We built our simulations so that ellipticities were measured...
on individual stamps of sheared galaxies in order to avoid the effect of blending from neighbour sources.

To evaluate the bias, we first produced images with constant shear values, \( g = 0.01, 0.05, 0.1, 0.15, 0.2 \), for each ellipticity component. We randomly drew 10,000 galaxies from the full sample, and repeated the simulation ten times. For each shear value, we then verified that the expected input value could be recovered, and we evaluated the bias as a function of signal-to-noise ratio, as well as at different positions in the image to check for systematics related to a poor PSF correction. From these tests, we derived a multiplicative bias \( m = 10\% \), and no significant additive bias; we were not able to detect a significant dependence on the signal-to-noise ratio.

Secondly, we used GalSim to simulate the shear signal produced by a cluster having a NFW profile with redshift, virial mass \( M = 10^{15} h^{-1} M_\odot \), and concentration parameter \( c_{200} = 4 \) similar to the values we find here for PLCK-G100. We made ten such simulations and fitted the results in the same way as in Sect. 5.4, where the only free parameter was the mass, and the concentration parameter was set to the input value of the simulation. The mass obtained applying the multiplicative bias was \( M_{200} = (1.0 \pm 0.2) \times 10^{15} h^{-1} M_\odot \).

### 5.4. Mass estimate

For the weak lensing analysis we used the sources in the catalogue satisfying the following criteria: (i) classified as extended (Sect. 3); (ii) with \( P_g > 0.1 \), SNe > 10; e1iso, e2iso < 1; and (iii) outside regions masked by bad columns, haloes, or spikes near bright saturated stars. We further considered only those sources classified as background galaxies in Sect. 5.2. This produced a catalogue of 17,000 sources in a 0.227 sq. deg area, corresponding to a density of 21 gals arcmin\(^{-2}\).

We first extracted (Fig. 8) the S-map (see Huang et al. 2011, and references therein), showing the spatial distribution of the weak lensing signal. The peak is consistent with the position of the galaxy that we identified as the BCG of the cluster in Sect. 4.

[Fig. 8](image) r-band luminosity-weighted map in the PLCKG100 field. The overplotted contour lines are the weak lensing S-map showing the mass distribution derived by weak lensing, at levels \( \sigma = 3, 4.5, 6, 8.5 \). The cross marks the position of the BCG assumed as the centre of the halo.

We therefore took this position as the centre of the cluster, and used it to compute the cross and tangential components of the ellipses whose profiles are displayed in Fig. 9.

[Fig. 9](image) Shear profile detected for PLCKG100 (tangential and cross components, where the latter is expected to be null), and for comparison the values derived adopting the best-fit models. We indicate with mNFW the model obtained using the Duffy et al. (2008) relation and with nfw the model obtained keeping both \( M_{vir} \) and \( c_{vir} \) as free parameters.
Table 2. Best-fit NFW parameters, at different overdensities, derived taking the two brightest galaxies as centre ($n = 1, 2$).

<table>
<thead>
<tr>
<th>$n$</th>
<th>$M_{\text{vir}}$</th>
<th>$c_{\text{vir}}$</th>
<th>$r_{\text{vir}}$</th>
<th>$M_{2500}$</th>
<th>$r_{2500}$</th>
<th>$M_{800}$</th>
<th>$r_{800}$</th>
<th>$M_{500}$</th>
<th>$r_{500}$</th>
</tr>
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<tbody>
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<td>1s</td>
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<td>3.31±0.48</td>
<td>518.27±23.74</td>
<td>7.39±1.50</td>
<td>1158.17±73.45</td>
<td>10.25±1.95</td>
<td>10.24±1.95</td>
</tr>
<tr>
<td>1b</td>
<td>15.31±2.43</td>
<td>3.77±0.34</td>
<td>2318.68±115.70</td>
<td>2.85±0.41</td>
<td>493.32±22.64</td>
<td>8.43±1.17</td>
<td>1210.04±53.61</td>
<td>12.91±2.03</td>
<td>12.90±2.03</td>
</tr>
<tr>
<td>1c</td>
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<td>3.65±0.30</td>
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<td>2.78±0.34</td>
<td>489.09±29.93</td>
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Notes. For each centre, in the upper row (a) both $M_{\text{vir}}$ and $c_{\text{vir}}$ were taken as free parameters; in the next row (b) the ($M_{\text{vir}}$, $c_{\text{vir}}$, $c_{\text{vir}}$) relation (Duffy et al. 2008) was used; in the last three rows we use the $c = M - z$ 2D relations in Meneghetti et al. (2014) (c: all; d: relaxed; e: super-relaxed). Masses are in units of $10^{14} M_{\odot}$, radii in kpc.

Fig. 10. Wavelet reconstructed X-ray image in the [0.5–2.5] keV energy band, obtained from the combination of the three XMM EPIC camera images. The contours show the weak lensing S-map (see Fig. 8), at levels $\sigma = 3.5, 5.5, 7.9$. The circle denotes the cluster centroid derived by the XMM analysis. The cross and square mark the position of the two brightest cluster galaxies (1 and 2, respectively, in the text).

6. X-ray analysis

PLCK G100.230.4 was observed for 13.7 ks with the XMM-Newton (obs-ID 0656202301) European Photon Imaging Cameras (EPIC) during the follow-up campaign of Planck newly detected clusters. This dataset was re-processed using the XMM-Newton Science Analysis System (SAS) version 14.0.0 in order to select the relevant calibration files. To remove any flare contamination, i.e. observation periods with an unusual count rate, we applied a 3σ clipping and a temporal wavelet filter to the histogram of the photon arrival times, with a bin size of 50 s, in the energy band [1–5] and [10–12] keV. After the flare removal procedure we find a useful exposure time of 13.7 ks and 5.2 ks for the two EPIC-MOS and the EPIC-PN datasets, respectively. To prepare the following imaging and spectroscopy analyses, we rebinned the flare-cleaned list of photon events in sky coordinates and energy, and associated both a 2D effective exposure and a background noise model to this data cube (see details in Bourdin & Mazzotta 2008).

The background noise was modelled after subtraction of all detected point-like sources using two components: the instrumental noise caused by high-energy particles interacting with the detectors, and several astrophysical components, namely the cosmic X-ray background (CXB) (e.g. Giacconi et al. 2001) plus...
Radial profiles of the X-ray properties are displayed as follows. Top, left: surface brightness in the [0.5–2.5] keV range. Points and the solid line represent the measured data and the best–fit modified beta profile, respectively. Top, right: electron density. Solid line and grey area represent the best-fit model and the relative error, respectively. Bottom, left: measured temperature profile. Points and solid line represent measured data and the temperature profile, respectively. Bottom, right: 3D temperature profile. Solid line and grey area represent the best-fit model and the error, respectively.

From the cleaned data we produced an image in the [0.5–2.5] keV, which is background subtracted and corrected for any spatial variation of the effective area. From this image we determined the X-ray peak at (RA = 350.56228, Dec = 28.52041). Figure 10 shows a wavelet denoising of this image. As we can see from this figure, the X-ray peak (circle) lies within 5′′ of the galaxy that we assumed to be the BCG (cross), whereas the second brightest galaxy is 18′′ away. It is worth noting that there is also a good agreement between the direction of the elongation of the cluster, going from NE to SW, as seen by the X-ray image and the isocontours from the lensing analysis.

From the photon image we then extracted a point-source excised surface brightness profile, centred on the cluster X-ray peak. In Fig. 11, top left panel, we show this surface brightness profile, which we found to reach the background level at $R = 1450$ kpc. The temperature profile, shown in Fig. 11, bottom
The envelope of the mass profile allowed us to derive a cluster mass equation (e.g. Sarazin 1988 or Ettori et al. 2013). The confidence envelopes of the 3D profiles in Fig. 12 were computed from aperture densitometry (black circles): a small offset in radius is applied here for display purposes.

left panel, was extracted in four bins from the same circular region as the surface brightness. The temperature was measured in each bin by fitting the spectrum in the energy band [0.3−11]keV using an absorbed APEC thermal model with three parameters, namely the normalization, temperature, and metallicity. The thermal models were convolved by the instrument response, as described in detail in Bourdin & Mazzotta (2008). The atomic hydrogen column density was fixed to its Galactic value $N_{\text{HI}} = 6.24 \times 10^{20}$ cm$^{-2}$ (Dickey & Lockman 1990).

To measure the X-ray mass we followed the “forward” procedure described in Meneghetti et al. (2010) and Rasia et al. (2012). In short, analytic profiles of the gas density and temperature Vikhlinin et al. (2006) were projected using the spectroscopic-like temperature Mazzotta et al. (2004) and fitted to the observed surface brightness and projected temperature. The 3D information were then folded into the hydrostatic mass equation (e.g. Sarazin 1988 or Ettori et al. 2013). The confidence envelopes of the 3D profiles in Fig. 12 were computed following a Monte Carlo procedure. More specifically, we generated several realizations of both a Poisson distributed surface brightness profile and a Gaussian distributed temperature profile, which hold the mean values and variances of the derived data quantities. For each of these realizations we fitted a new set of density and 3D temperature profiles, and stored these models when they obeyed the physical prior that the underlying hydrostatic mass profile is increasing and positive. From $N = 500$ remaining hydrostatic density, 3D temperature, and mass models, we drew the confidence envelopes that encompass 68% of the realizations with minimal distance to their relative best fit. The envelope of the mass profile allowed us to derive a cluster mass of $M_{2500} = 3.2^{+0.8}_{-0.5} \times 10^{14} M_{\odot}$, $M_{1000} = 4.4^{+0.8}_{-0.7} \times 10^{14} M_{\odot}$, and $M_{500} = 5.4^{+1.0}_{-0.9} \times 10^{14} M_{\odot}$, which corresponds to $R_{2500} = 541^{+49}_{-39}$ kpc, $R_{1000} = 816^{+39}_{-50}$ kpc, and $R_{500} = 1093^{+66}_{-62}$ kpc, respectively. The latter mass value is in excellent agreement with the mass derived from the iteration of the $M_{500} - Y_X$ relation, $M_{500} = (5.60 \pm 0.22) \times 10^{14} M_{\odot}$ (Planck Collaboration IX 2011).

Figure 12 also shows a comparison of the X-ray total mass profile with those obtained from WL aperture mass densitometry and WL NFW model fitting (obtained with two free parameters). The inset shows the various mass estimates at density contrasts of 2500, 1000, and 500. The agreement between the different mass measurements is remarkably good at all density contrasts.

Planck Collaboration XX (2014) parameterized the difference between their mass estimate and the true mass by the factor $(1-b)$, where $b$ contains all possible sources of bias: neglect of the non-thermal pressure support in the hydrostatic assumption, multi-temperature structure in the ICM, instrumental calibration uncertainties, etc. Assuming a weak lensing reconstructed mass of $M_{500,\text{WL}} \sim (7 \pm 1) \times 10^{14} M_{\odot}$ and comparing this to the mass estimate obtained by Planck Collaboration IX (2011), we obtain $(1-b) = 0.8 \pm 0.1$ from the present observations.

Planck Collaboration XX (2014) obtained a bias factor of $(1-b) = 0.8$ from their calibration of $b$ using numerical simulations, and used this value, with a flat prior of [0.7,1.0], as the baseline for their cosmological analysis. Planck Collaboration XXIV (2015) have updated this analysis to include a calibration of $(1-b)$ using weak lensing mass measurements, taking into account sources of scatter such as triaxiality, the presence of substructures, and systematic errors in the weak lensing measurement itself. Assuming the weak lensing mass to be the true mass, their analysis yields $(1-b)_{\text{WLG}} = 0.69 \pm 0.07$ and $(1-b)_{\text{CCCP}} = 0.78 \pm 0.09$ for the samples of von der Linden et al. (2014, Weighing the Giants) and Hoekstra et al. (2015, Canadian Cluster Cosmology Project), respectively. Under the same assumption, the value we obtain from PLCKG100 is compatible within 1σ with the bias factor derived from these updated measurements.

7. Summary and conclusions

We presented here the first weak lensing analysis of the PLCK G100.2-30.4 cluster. The analysis confirmed that this is a massive cluster ($M_{\text{vir}} > 10^{15} M_{\odot}$), in agreement with the value expected from the richness estimate.

At a density contrast of 500 with respect to the critical density of the Universe at the cluster redshift, the weak lensing mass from aperture densitometry is $M_{500} = (6 \pm 2) \times 10^{14} M_{\odot}$ after deprojection. An NFW fit in the radial range 1−15 arcmin, shown by the dotted line in Fig. 12, yields a mass $M_{500} \sim (7 \pm 1) \times 10^{14} M_{\odot}$. We checked the robustness of the weak lensing mass estimates by repeating the analysis with different choices of the cluster centre and of the NFW model fitting. In particular, we compared the results obtained by leaving both $c_{\text{vir}}$ and $M_{\text{vir}}$ as free parameters, and using different $(c,M,z)$ relations. These yield results consistent with those given above.

Comparing the mass derived by weak lensing with the value obtained by the reanalysis of XMM data, we obtain a bias factor of $(1-b) = 0.8 \pm 0.1$. This is compatible within 1σ with the bias factor obtained by Planck Collaboration XXIV (2015) from their calibration of $(1-b)$ using newly available weak lensing samples from von der Linden et al. (2014) and Hoekstra et al. (2015). The present results illustrate the importance of high-quality data and the need for larger samples in such cluster mass studies.
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