

## Planck 2015 results

### XXVI. The Second Planck Catalogue of Compact Sources

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#### ABSTRACT

The Second *Planck* Catalogue of Compact Sources is a list of discrete objects detected in single-frequency maps from the full duration of the *Planck* mission and supersedes previous versions. It consists of compact sources, both Galactic and extragalactic, detected over the entire sky. Compact sources detected in the lower frequency channels are assigned to the PCCS2, while at higher frequencies they are assigned to one of two subcatalogues, the PCCS2 or PCCS2E, depending on their location on the sky. The first of these (PCCS2) covers most of the sky and allows the user to produce subsamples at higher reliabilities than the target 80% integral reliability of the catalogue. The second (PCCS2E) contains sources detected in sky regions where the diffuse emission makes it difficult to quantify the reliability of the detections. Both the PCCS2 and PCCS2E include polarization measurements, in the form of polarized flux densities, or upper limits, and orientation angles for all seven polarization-sensitive *Planck* channels. The improved data-processing of the full-mission maps and their reduced noise levels allow us to increase the number of objects in the catalogue, improving its completeness for the target 80% reliability as compared with the previous versions, the PCCS and the Early Release Compact Source Catalogue (ERCSC).

**Key words.** catalogues – cosmology: observations – radio continuum: general – submillimeter: general

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**Table 1.** Characteristics of the PCCS2 and PCCS2E catalogues.

Channel	Flux density 90% completeness [mJy]	No. of sources		Polarized sources	
		PCCS2	PCCS2E	PCCS2	PCCS2E
30 .....	427	1560	...	122	...
44 .....	692	934	...	30	...
70 .....	501	1296	...	34	...
100 .....	269	1742	2487	20	43
143 .....	177	2160	4139	25	111
217 .....	152	2135	16842	11	325
353 .....	304	1344	22665	1	666
545 .....	555	1694	31068	...	...
857 .....	791	4891	43290	...	...

**Notes.** The table lists: flux density at 90% completeness in total intensity; number of sources detected in each catalogue in total intensity; and number of sources that have a polarized signal is measured above a 99.99% confidence level. See Tables 13 and 14 for more details.

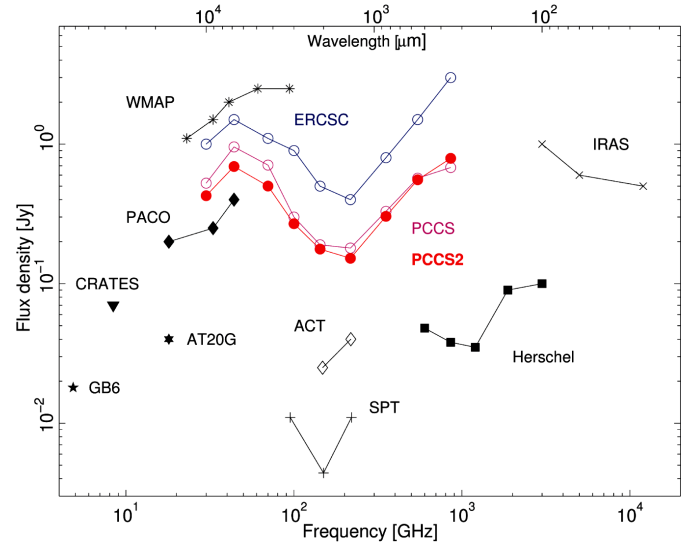
## 1. Introduction

This paper, one of a set associated with the 2015 release of data from the *Planck* mission<sup>1</sup>, describes the second release of the *Planck* Catalogue of Compact Sources (PCCS2)<sup>2</sup>. It outlines the construction of the single-frequency catalogues from an analysis of each of the nine *Planck* frequency-channel, full-mission maps. The construction of these catalogues builds on much of the same infrastructure and methodology as the first incarnation of the *Planck* Catalogue of Compact Sources (PCCS), and the reader is referred to [Planck Collaboration XXVIII \(2014\)](#) for a full description of the catalogue construction procedures, which are only summarized here. Table 1 lists some basic properties of the nine frequency subcatalogues of the current release.

One of the primary differences of this release from the PCCS is the division of the six highest frequency catalogues into two subcatalogues, the PCCS2 and the PCCS2E. This division separates sources for which the reliability (the fraction of sources above a given S/N which are real) can be quantified (PCCS2) from those of unknown reliability (PCCS2E). This separation is primarily based on the Galactic coordinates of the source, as described in Sect. 2.3. The target integral reliability of the entire catalogue, as in the PCCS, is 80% or greater. The advantage of setting the reliability target this low is that it improves the odds of discovering interesting sources with unusual properties, which might otherwise have been rejected by restrictive selection criteria. On the other hand, a highly reliable catalogue is desirable for follow-up observations. That is the aim of the PCCS2. To this end, we have provided additional information in the catalogue which will allow the user to select a subset of highly reliable sources from the PCCS2. This takes the form of an additional flag per source that indicates the highest reliability catalogue to which that source belongs, allowing the user to perform a cut on the PCCS2 to reduce it to the desired percentage reliability subset. To assist users, we also flag those sources identified in other catalogues, mainly at radio wavelengths.

<sup>1</sup> *Planck* (<http://www.esa.int/Planck>) is a project of the European Space Agency (ESA) with instruments provided by two scientific consortia funded by ESA member states and led by Principal Investigators from France and Italy, telescope reflectors provided through a collaboration between ESA and a scientific consortium led and funded by Denmark, and additional contributions from NASA (USA).

<sup>2</sup> <http://archives.esac.esa.int/pla>



**Fig. 1.** Sensitivity (the flux density at 90% completeness) of the PCCS2, compared with PCCS, ERCSC, WMAP and others as described in text. The sensitivities displayed for the LFI channels are for the full sky. For the HFI channels, the 90% completeness limits plotted for the PCCS were evaluated in the extragalactic zone, as defined in [Planck Collaboration XXVIII \(2014\)](#). The regions of sky to which the 90% completeness limits apply are therefore similar (but not identical) to those of the PCCS2. These comparisons are discussed further in Sect. 4.

The principal data-driven difference between the PCCS and the PCCS2 and PCCS2E catalogues is the additional data from the “extended” mission and the inclusion of polarization measurements in seven out of the nine frequency channels. The 545 and 857 GHz channels are not sensitive to polarized signals, so the polarization measurements span the range from 30 to 353 GHz. The polarization measurements provided are based on the positions of the compact sources discovered in the temperature maps; there is no independent search for compact sources in polarization. The additional data, together with improved data processing, have the effect of reducing the noise and hence improving the completeness of the PCCS2 and PCCS2E catalogues over that of the PCCS, as demonstrated in Fig. 1. In this figure we compare the sensitivity of the PCCS2 with that of the PCCS ([Planck Collaboration XXVIII 2014](#)), the Early Release Compact Source Catalogue (see [Planck Collaboration XIII 2011](#) for the 30–70 GHz channels and [Planck Collaboration Int. VII 2013](#) for the others), WMAP (see [González-Nuevo et al. 2008](#) for the channels at 41 GHz and below, and [Lanz et al. 2013](#) for 61 and 94 GHz). The sensitivity levels for the *Herschel* SPIRE and PACS instruments are from [Clements et al. \(2010\)](#) and [Rigby et al. \(2011\)](#), respectively. The other wide-area surveys shown as a comparison are: the Green Bank 6 cm Survey, GB6 ([Gregory et al. 1996](#)), the Combined Radio All-Sky Targeted Eight GHz Survey, CRATES ([Healey et al. 2007](#)), the Australia Telescope 20 GHz Survey, AT20G ([Murphy et al. 2010](#)), the *Planck*–ATCA Co-eval Observation Project, PACO ([Bonavera et al. 2011](#)), the South Pole Telescope, SPT ([Mocanu et al. 2013](#)), the Atacama Cosmology Telescope, ACT ([Marsden et al. 2014](#)), and the Infrared Astronomical Satellite catalogue, IRAS ([Beichman et al. 1988](#)).

In Sect. 2 we describe the construction of the catalogues, including the criteria used to place a source into the PCCS2 or the PCCS2E, and the methods used to measure the flux densities and

linear polarization parameters. Section 3 discusses the validation and quality assessment of the catalogues. Here the internal and external consistency tests are described, as are the completeness (the fraction of the total number of sources above a given flux density that are present in the catalogue) and reliability of the catalogues. The overall characteristics of the PCCS2 and PCCS2E are presented in detail in Sect. 4; they are also compared with the characteristics of the PCCS. The released product, which is composed of the catalogues and their associated maps, is described in Sect. 5. We summarize our conclusions in Sect. 6. Details of the estimators used for photometry and for polarization measurements are given in the Appendices.

## 2. The Second *Planck* Catalogue of Compact Sources

### 2.1. Data

After four years of operations, the data from the full *Planck* mission have been transformed into full-sky HEALPix<sup>3</sup> maps (Górski et al. 2005) by the data processing centres (DPCs) (Planck Collaboration VI 2016; Planck Collaboration VIII 2016). The Low Frequency Instrument (LFI) DPC produced the 30, 44, and 70 GHz maps after the completion of eight full surveys (spanning the period 12 August 2009 to 3 August 2013). In addition, special LFI maps covering the period 1 April 2013 to 30 June 2013 were produced in order to compare the *Planck* flux-density scales with those of the Very Large Array and the Australia Telescope Compact Array, by performing simultaneous observations of a sample of sources over that period. The High Frequency Instrument (HFI) DPC produced the 100, 143, 217, 353, 545, and 857 GHz maps after five full surveys (2009 August 12 to 2012 January 11). The flux densities of all sources measured in the full-mission maps are an average of several observations. Single-survey maps are available from the *Planck* Legacy Archive<sup>4</sup>, but single-survey flux densities are not provided in this catalogue. It is important to note that even single-survey maps may include more than one observation of an individual source, and hence extracting flux densities from the single-survey maps does not guarantee a single-epoch observation for a given source. However, in the *Planck* Legacy Archive the time-ordered data are available and users can produce maps from arbitrary time intervals. Table 2 gives the parameters of the *Planck* beams used in this paper; further details may be found in Planck Collaboration II (2016) and Planck Collaboration VII (2016).

### 2.2. Catalogue construction

The compact sources in the catalogue were detected at each frequency independently using improved versions of the detection pipelines used to create the PCCS. These pipelines are based on the Mexican Hat Wavelet 2 algorithm (MHW2; González-Nuevo et al. 2006; López-Cañiego et al. 2006). This is a cleaning and denoising algorithm used to convolve the maps, preserving the amplitude of the sources while greatly reducing the large-scale structures visible at these frequencies (e.g. diffuse Galactic emission) and small scale fluctuations (e.g. instrumental noise) in the vicinity of the sources. The LFI and HFI DPCs have different implementations of the MHW2 algorithm, but consistency checks between them have been performed.

<sup>3</sup> <http://healpix.sourceforge.net>

<sup>4</sup> <http://archives.esac.esa.int/pla>

**Table 2.** Parameters of the beams used in the construction of the PCCS2 and PCCS2E.

Channel	FWHM		Beam area		
	Fitted [arcmin]	Effective [arcmin]	$\Omega_{\text{beam}}$ [arcmin <sup>2</sup> ]	$\Omega_{\text{beam}_1}$ [arcmin <sup>2</sup> ]	$\Omega_{\text{beam}_2}$ [arcmin <sup>2</sup> ]
30 . . . .	32.29	32.41	1190.06	1117.30	1188.93
44 . . . .	27.00	27.10	832.00	758.00	832.00
70 . . . .	13.21	13.32	200.90	186.10	200.59
100 . . . .	9.66	9.69	106.22	100.78	106.03
143 . . . .	7.22	7.30	60.44	56.97	60.21
217 . . . .	4.90	5.02	28.57	26.46	28.46
353 . . . .	4.92	4.94	27.69	25.32	27.53
545 . . . .	4.68	4.83	26.44	24.06	26.09
857 . . . .	4.22	4.64	24.37	22.58	23.93

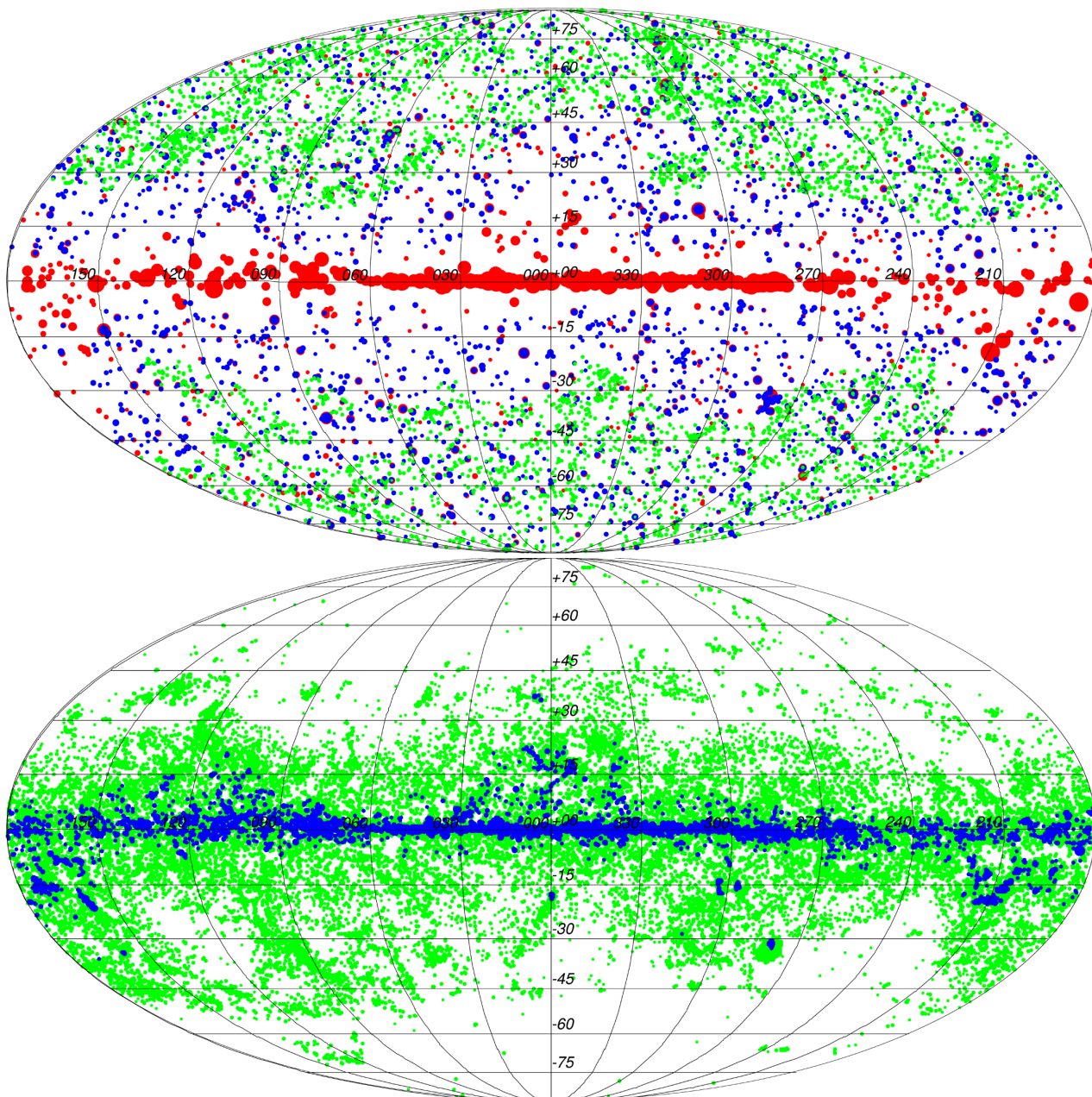
**Notes.** Two FWHM values are given: one from an elliptical Gaussian fit to the beam, and another that is the FWHM of a Gaussian with the same solid angle as the main beam,  $\Omega_{\text{beam}}$ . The FWHM found from the main beam solid angle is used to evaluate  $\Omega_{\text{beam}_1}$  and  $\Omega_{\text{beam}_2}$ , which are the beam solid angles within a radius equal to this FWHM and twice this FWHM, respectively.

The differences between the implementations are described in Planck Collaboration XXVIII (2014), and are due to the different characteristics of the maps at LFI and HFI frequencies, requiring alternative methods to reduce the numbers of spurious detections. Both implementations project the full-sky maps onto square patches where the filtering and detection is performed. The sizes of the patches and the overlap between patches have been chosen in such a way that the full sky is effectively covered. Sources above a fixed signal-to-noise ratio (S/N) threshold are selected and their positions are translated from patch to spherical sky coordinates. Because the patches overlap, multiple detections of the same object can occur; these must be found and removed, keeping the detection with the highest S/N for inclusion in the catalogue.

### 2.3. Defining the PCCS2 and PCCS2E

For reasons explained in Sect. 1, for this release we provide two subcatalogues for some frequency channels, which we call PCCS2 and PCCS2E. We also provide a new parameter for each source that gives the highest reliability catalogue to which the source belongs. However, it is not possible to evaluate this parameter for every source. It is this consideration which separates the sources into the PCCS2 and the PCCS2E; those sources without this field are placed in the PCCS2E. Figure 2 shows the distribution of the PCCS2 and PCCS2E sources across the sky for three of the *Planck* frequency channels (30, 143, and 857 GHz).

LFI: One measure of the reliability of the sources detected in the three LFI channels is based on a comparison with existing catalogues of radio sources. First, each single-frequency catalogue is compared with the appropriate external radio catalogues. Next, all the remaining unidentified sources outside a  $|b| > 20^\circ$  Galactic cut are examined on a source-by-source basis by performing a manual search in archival repositories such as the NASA/IPAC Extragalactic Database (NED). Second, a multifrequency analysis is used to assess whether or not a source is present in more than one *Planck* channel between 30 and 100 GHz. All sources with plausible identifications in external catalogues are assigned to the PCCS2 with a high degree of reliability. Additionally, all



**Fig. 2.** *Top:* distribution of the validated sources from the PCCS2. Red, blue, and green circles show sources from the 30, 143, and 857 GHz catalogues, respectively. *Bottom:* locations of the sources in the 143 and 857 PCCS2E, shown by blue and green circles, respectively. The figure is a full-sky Mollweide projection with the Galactic equator horizontal; longitude increases to the left with the Galactic centre in the centre of the map. The size of the filled circles gives an idea of the relative flux densities of the sources per frequency, where the larger circles correspond to larger flux densities. Note that a different size range for each channel was necessary for visualization purposes.

sources that are detected in two or more *Planck* channels in the multifrequency analysis are also placed in the PCCS2, albeit with a lower degree of reliability. Given the small number of remaining sources, we do not create a PCCS2E for the LFI bands; instead, we flag the least reliable sources. Further details can be found in Sect. 3.2.1, which describes our assessment of the reliability of the PCCS2 at the lower frequency channels.

HFI: There are no external full-sky catalogues at HFI frequencies; hence the reliability cannot be evaluated following the same procedure as for LFI. Instead, we follow a similar procedure to the one used for the PCCS as described in [Planck Collaboration XXVIII \(2014\)](#). In that paper, we used two

measures of reliability for the HFI catalogues. The first measure, which we called *simulation reliability*, is determined from source injection into simulated maps and is defined as the fraction of detected sources that matched the positions of injected sources. If the simulations are accurate, such that the spurious and real detection number counts mirror the real catalogue, this reliability is exact. The second measure, which we called *injection reliability*, is determined from source injection into the real maps, and in this case we are only simulating the real source component. The total source counts are composed of real and spurious components. In order to understand the reliability, we need to understand the spurious component. However, if we have a knowledge of the real component we can infer the spurious component from the total source counts. This is the motivation

for this second approach, where injection reliability is defined as the fraction of total extracted sources that correspond to injected sources recovered by PCCS2 detection methods. This method therefore provides an approximate assessment of the reliability. Naturally, the first method is preferred over the second, but the second approach becomes necessary when the simulations are not a sufficiently accurate representation of the sky signal. In order to establish whether the simulations are of sufficient quality, we require that the simulated catalogues pass two internal consistency tests: that they have the same injected source completeness as the real catalogues; and that they have total detected number counts, as a function of S/N, that are consistent with those in the real data. (The intrinsic number counts are assumed to be power law functions of flux density and are fitted to the detection counts at higher flux densities, where the catalogues are reliable and complete, and extrapolated to lower flux densities). In order to achieve this internal consistency we need to exclude the Galactic plane region from the analysis, due to discrepancies arising from deficiencies in the simulation of diffuse dust emission near the beam scale (e.g. Galactic cirrus) and uncertainties in defining an input source model for the Galactic sources. The region excluded increases with frequency and is not a simple Galactic latitude cut, but is based on the level of the dust emission. The Galactic masks used at each of the six HFI frequencies are described in Sect. 3.2. In addition to these Galactic plane regions, for the highest four frequency channels we also exclude the region of sky inside a “filament mask” from the reliability assessment. Note that there is a different filament mask for each of these channels. These filament masks describe the areas of the sky in which residual structures, not related to sources, are present in the MHW2 filtered maps. The creation of these masks is explained further in Sect. 3.2.2. The union of the filament mask and the Galactic plane region then defines the area of the sky in which sources are assigned to the PCCS2E. Thus, whether a source is assigned to the PCCS2 or PCCS2E is determined solely by its location on the sky. The HFI reliability assessment for the PCCS2 is described further in Sect. 3.2.3 (recall there is no reliability assessment for the PCCS2E).

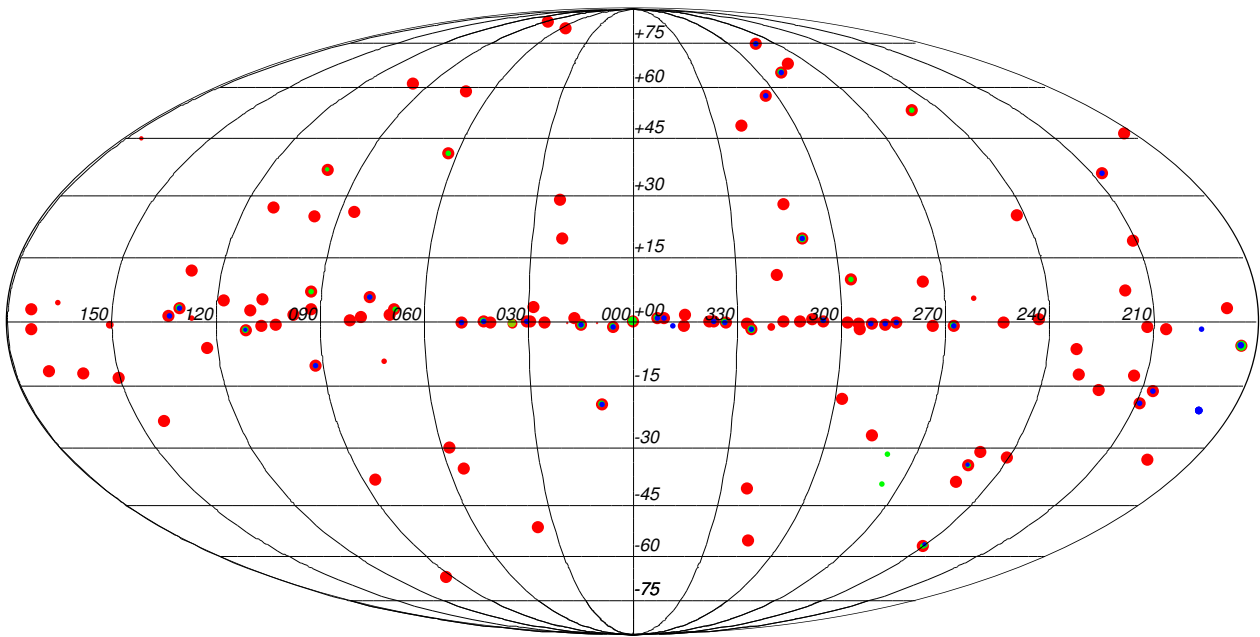
## 2.4. Photometry

As in the PCCS, we provide four different measures of the flux density for each source. They are determined by the source detection algorithm (DETFLUX), aperture photometry (APERFLUX), point spread function fitting (PSFFLUX), and Gaussian fitting (GAUFLUX). Only the first is obtained from the filtered maps; the other measures are estimated from the full-sky maps at the positions of the sources. The source detection algorithm photometry, the aperture photometry, and the point spread function (PSF) fitting use the *Planck* band-average effective beams, calculated with FEBeCoP (Fast Effective Beam Convolution in Pixel space; Mitra et al. 2011; Planck Collaboration IV 2016; Planck Collaboration VII 2016). Note that only the PSF fitting algorithm takes into account the variation of the PSF with position on the sky. The PCCS2 has been produced from the *Planck* full-mission maps (eight sky surveys in the LFI and five sky surveys in the HFI), and therefore supersedes the previous catalogues (for the PCCS only 1.5 surveys were analysed). It also includes the latest calibration and beam information, and we have improved some of the algorithms used to measure the photometry of the sources. In order to assess the differences between the photometry in the PCCS and PCCS2 we have compared both sets of catalogues at all *Planck* bands.

A major change is in the Gaussian fitting photometry. We have implemented a new version of the algorithm that produces more robust measures, particularly for extended objects where the difference between the flux densities in the PCCS and PCCS2 can be as large as 100%. In the previous version of the algorithm, for some sources the fitting code was not converging properly and this issue has been addressed by using a new fitting approach; see Appendix B for a description of the method and its validation. In addition, the photometry from the detection pipeline has changed at some frequencies by several percent, because it now takes into account the latest information about the effective beam FWHM and corrects for the biases listed in Table 6, which range from 1% to 12%, depending on the frequency. The other two techniques, aperture photometry and PSF fitting, produce similar results in both catalogues. In the first case, the algorithm has not changed, while in the second, although the algorithm has been changed to improve the positional accuracy, this does not affect our measurements because we use the coordinates from the detection pipeline as the reference for all photometric measures. In both cases the differences are always at the percent level. Moreover, flux densities extracted from the publicly released *Planck* maps at 30, 44, and 70 GHz require a small correction for beam efficiency, since a small amount of power lies outside the main beam (Planck Collaboration II 2016). These small multiplicative corrections are 1.00808, 1.00117, and 1.00646 at 30, 44, and 70 GHz, respectively. The flux densities provided for sources in the PCCS2 catalogues have been corrected accordingly. Uncertainties are provided for all four flux-density measures. In Table 13 we show the uncertainties associated with the flux densities of the faintest sources in the extragalactic zone of each catalogue, after excluding the faintest 10% of sources as obtained with the source detection algorithm. These uncertainties range from 90 to 130 mJy for the 30–70 GHz catalogues, and from 30 to 270 mJy for the 100–857 GHz catalogues. This gives an idea of the sensitivity of the catalogue and the associated uncertainties. However, the uncertainties depend not only on the flux density of the sources but also on their position in the sky, so we provide noise maps that can be used to estimate the expected uncertainty in the flux density of a source at any position in the sky.

Detection pipeline photometry (DETFLUX). The detection pipelines assume that sources are point-like. The amplitude of a detected source is converted to flux density using the solid angle of the effective beam (from Table 2), and the conversion from map units into intensity units. The uncertainty in the flux density for each source is measured as the local noise in an annulus around the source in the MHW2-filtered map, where bright pixels belonging to other compact sources in the vicinity, if any, are excluded from the calculation. If a source is resolved by *Planck* its flux density will be underestimated. In this case it may be better to use the GAUFLUX estimation. The estimation of the flux density provided by the HFI detection pipeline has been improved since the PCCS release, by removing a bias that lowered the recovered flux densities in the higher frequency channels (see Planck Collaboration XXVIII 2014). The photometric performance of the PCCS2 detection pipeline is assessed in Sect. 3.4.

Aperture photometry (APERFLUX). The flux density is estimated by integrating the data in a circular aperture centred at the position of the source. An annulus around the aperture is used to evaluate the level of the background. The annulus is also



**Fig. 3.** Distribution of the polarized sources in the lowest channels of the PCCS2. Red, green, and blue circles show sources from the 30, 44, and 70 GHz catalogues, respectively. As in Fig. 2, the size of the circle gives a qualitative idea of the relative polarized flux density of the source.

used to make a local estimate of the noise to calculate the uncertainty in the flux density. The flux density is corrected for the fraction of the beam solid angle falling outside the aperture and for the fraction of the beam solid angle falling in the annulus. The aperture photometry was computed using an aperture with a radius equal to the average FWHM of the effective beam (the effective FWHM in Table 2), and an annulus with an inner radius of 1 FWHM and an outer radius of 2 FWHM. The effective beams, also given in Table 2, were used to compute the beam solid angle corrections. For details see the PCCS paper (Planck Collaboration XXVIII 2014).

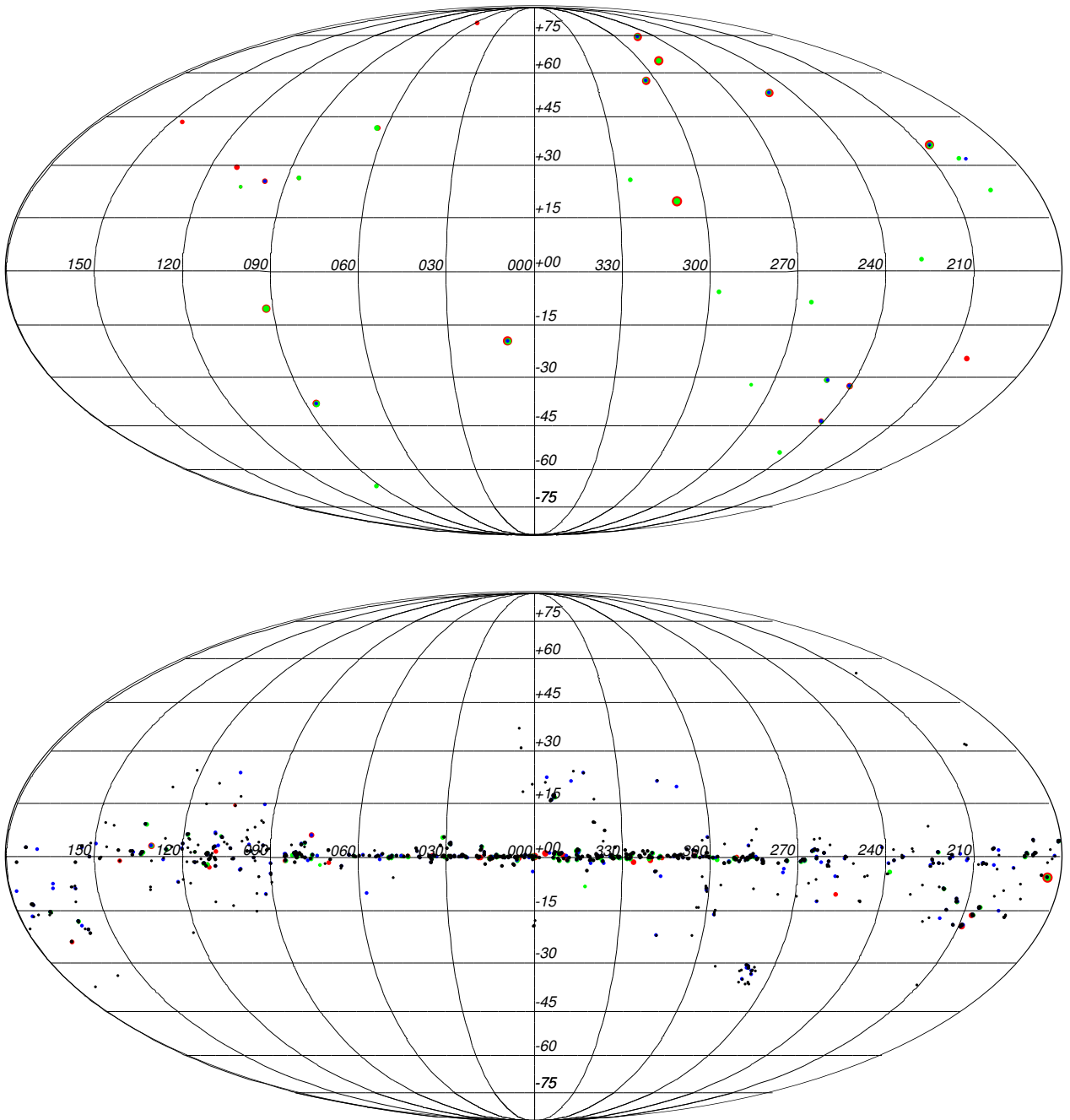
**PSF fit photometry (PSFFLUX).** The flux density and its uncertainty are obtained by fitting a model of the PSF at the position of the source. The model has four free parameters: the amplitude of the source; a background offset; and two coordinates for the location of the source. The PSF is obtained from the effective beam by means of a bicubic spline interpolation for source positions that are different from the centre of a pixel. Note that the PSF fitting now includes subpixel positioning, which is a new feature introduced after the production of the PCCS. For details see Appendix A.

**Gaussian fit photometry (GAUFLUX).** The approach to Gaussian fitting has been completely revised since the PCCS. The algorithm now allows the position of the source to vary as the best fit is found. The same parameters are returned for each source: its flux density; the major and minor semi-axes; and an orientation angle. Additionally, as in the PCCS, the semi-axis values are used in the construction of the flag for extended sources. The new method uses a downhill simplex method in multidimensions, the Nelder-Mead method, to find the best-fit values in the full parameter space of position, flux density, and elliptical Gaussian parameters. The method has been shown to be robust and stable (Press et al. 1992). Optimization is based on the reduced

log-likelihood with prior regularization for the size of the source defined by the effective beam at each frequency. The downhill simplex methods does not produce estimates of the flux density uncertainties. For this purpose a Markov Chain Monte Carlo has been used. For details see Appendix B.

## 2.5. Polarization

In the *Planck* polarization maps, the polarized sources are embedded in a background that is the combination of instrumental noise and diffuse emission. The nature of the diffuse emission depends on the observation frequency; for example, polarized synchrotron emission in the lower frequency channels and infrared emission in the higher frequency channels. In both regimes the polarization fraction of the compact sources (the ratio between their polarized flux densities and total intensity) is typically lower than 1–2%. This presents a challenge in terms of disentangling the true polarized flux density of a source from the background. In order to tackle this problem, a two-step process has been proposed (López-Cañiego et al. 2009). First, a maximum-likelihood filter is applied, reducing the noise and enhancing the S/N of the sources embedded in the  $Q$  and  $U$  maps (Argüeso et al. 2009). Second, the significance of each detection is assessed based on the statistics of the local background in the vicinity of the source. Several significance levels were investigated and we concluded that, for the typical polarization backgrounds present in the *Planck* polarization maps, a significance threshold of 99.99% successfully distinguishes the polarized emission of a compact source from a peak in the background. This approach has been used in the present catalogues to attempt to measure the polarized flux densities and uncertainties of all sources found in the temperature maps. Polarization measurements are provided for all sources where the significance of the detected polarized signal reaches or exceeds the limit of 99.99%; for the remaining sources we provide the 99% upper limit. Figures 3 and 4 show the distributions of the significantly



**Fig. 4.** Distribution of the polarized sources from the PCCS2 (*top*) and the PCCS2E (*bottom*). Red, blue, green, and black circles show sources from the 100, 143, 217, and 353 GHz catalogues, respectively. As in previous figures, the size of the filled circles gives a qualitative idea of the relative flux densities of the sources at each frequency, where the larger dots correspond to larger flux densities. Note that a different circle size range for each channel was necessary for visualization purposes.

polarized sources in the LFI and HFI polarized frequency channels. Normalized histograms of the polarization fraction for the population of significantly polarized sources in the PCCS2 catalogues are shown in Fig. 5.

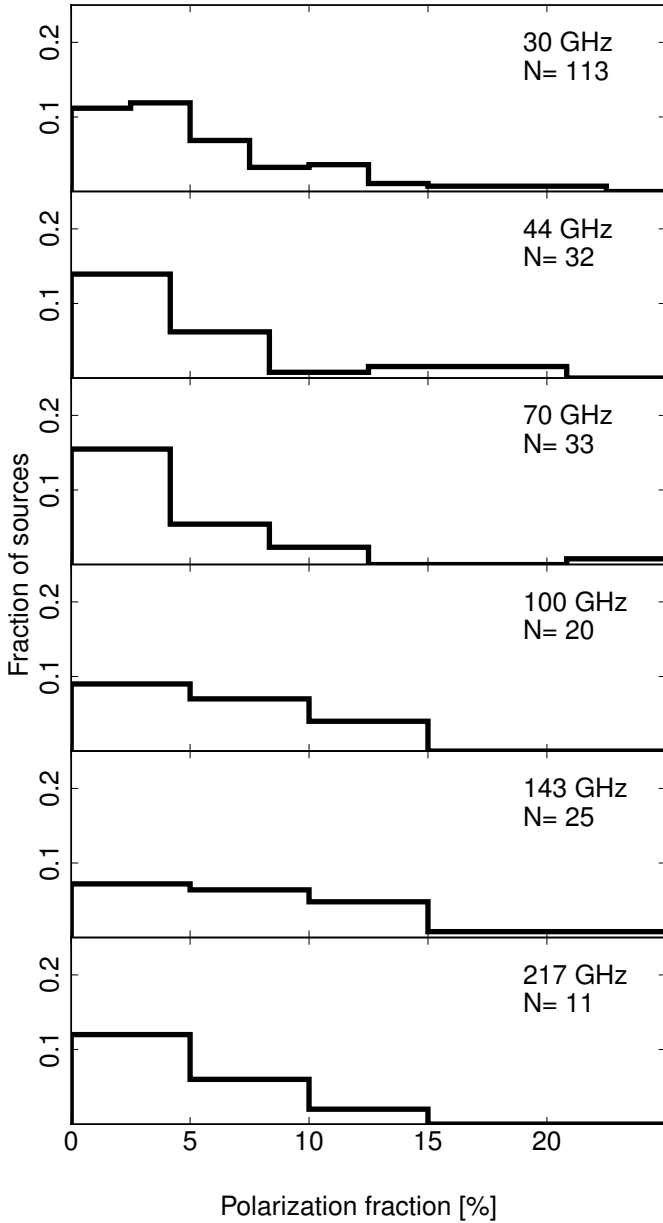
If a source is not strictly point-like, the filtering procedure used to reduce the noise will also remove signal. For this reason we also provide aperture photometry measurements for polarization, which, although noisier, do not remove as much signal from compact (but not point-like) sources as filtering. The aperture photometry package is common to both LFI and

HFI, whereas there are two different implementations of the maximum-likelihood estimator, which will allow us to assess the robustness of the methods by comparing their results in a common set of simulations. The results of the HFI and LFI polarization pipelines are compared in Sect. 3.5.

The polarized flux density of a source,  $P$ , is evaluated using

$$P = \sqrt{Q^2 + U^2}, \quad (1)$$

where  $Q$  and  $U$  are the flux densities in the Stokes  $Q$  and  $U$  maps, measured at the position of the source detected in the  $I$  map. We



**Fig. 5.** Normalized histograms of the recovered polarization fraction from the PCCS2 catalogue from 30 to 217 GHz (the 353 GHz channel is not shown because the catalogue contains only one source). The number of sources in each histogram is indicated.

follow the IAU/IEEE convention (Hamaker & Bregman 1996) for defining the angle of polarization of a source: polarization angles are taken as increasing anticlockwise (north through east). In this paper, position angle zero is taken as the direction of the north Galactic pole. The polarization angle is defined by

$$\psi = \frac{1}{2} \arctan(-U/Q). \quad (2)$$

The minus sign is necessary to correct from the HEALPix convention for position angles used in the *Planck* Stokes parameter maps, in which position angle increases clockwise. As noted in Planck Collaboration I (2016), the convention used for *Planck* polarization maps is the one usual in CMB studies and is used in WMAP papers, whereas the IAU/IEEE convention adopted here is standard for astronomical sources. Polarization angles are given in degrees in the range  $-90^\circ$  to  $90^\circ$ . The estimate of

$P$  acquired using Eq. (1) is biased, because the errors in the  $Q$  and  $U$  measurements, on average, contribute positively to the measurement of  $P$  (see, e.g. Montier et al. 2015). However, in our significance regime we can use the approximation

$$P_{\text{debiased}} = \sqrt{P^2 - \sigma_P^2} \quad (3)$$

to debias our estimate of  $P$ , where  $\sigma_P$  is the error in  $P$  and is calculated by propagating the errors in  $Q$  and  $U$ , where  $\sigma_{Q,U}$  are calculated as the local rms in an annulus around the source in the maximum-likelihood filtered  $Q$  and  $U$  maps, under the assumption of no correlation:

$$\sigma_P = \sqrt{\frac{1}{Q^2 + U^2} (Q^2 \times \sigma_Q^2 + U^2 \times \sigma_U^2)}. \quad (4)$$

The polarization angle error is obtained by propagating the errors in  $Q$  and  $U$ :

$$\sigma_\psi = \frac{1}{2(Q^2 + U^2)} \sqrt{Q^2 \times \sigma_U^2 + U^2 \times \sigma_Q^2}. \quad (5)$$

As shown in Table 14 the typical uncertainty in the polarized flux density is 45–90 mJy between 30 and 70 GHz and 30–180 mJy between 100 and 353 GHz.

### 2.5.1. Corrections for bandpass mismatch

Mismatch between the bandpass shapes of the two orthogonally-polarized detectors in each feed horn causes leakage of total intensity into the polarization signal for any emission whose spectrum differs from that of the primary calibrator, namely the CMB dipole; therefore all foreground emission including that from compact sources suffers from temperature-to-polarization leakage. Correction requires a model of the spectrum of the source, as well as a model for the spectral response of each detector or bolometer. Since the detecting elements used in the two instruments are different, LFI and HFI treated bandpass mismatch differently. The magnitude of the correction can be very different from one source to another. In the lower *Planck* frequencies, the correction can vary from a fraction of a percent up to 100%. In the higher frequency channels this correction is always below the percent level. The details are presented in Appendix C.

### 2.5.2. Evaluation of marginal polarization measurements

At four HFI frequencies (100, 143, 217, and 353 GHz) we present an additional set of polarized flux-density and polarization angle estimates for sources detected only marginally in polarization. These are derived using the Bayesian ‘‘PowellSnakes’’ algorithm (see Planck Collaboration XXVIII 2014). The aim is to disentangle the sources that have some polarized emission from those that are consistent with no polarized signal. This allows us to probe fainter polarization signals, and thus to provide deeper and more complete polarization catalogues without any loss of reliability (as we show in Sect. 3.5). The details of the method are presented in Appendix C.3.

## 3. Validation of the PCCS2

The contents of the PCCS2 and the four different flux-density estimates have been validated by simulations (internal validation)



and comparison with other astrophysical data (external validation), as was done for the PCCS (Planck Collaboration XXVIII 2014). The validation of the low-frequency sources can be performed in part by using the large number of existing catalogues. Detections identified with known sources have been flagged as such in the catalogues. In contrast, the validation of sources at higher frequencies must be done using simulations, specifically through a Monte Carlo quality assessment process in which artificial sources are injected into both real and simulated maps. In the following subsections, we discuss tests on the completeness, reliability, astrometry, and photometry of the single-frequency catalogues, as well as comparisons between different *Planck* bands. We also describe internal and external validation of the polarization measurements.

### 3.1. Completeness

#### 3.1.1. LFI

In the case of the three lowest frequencies, we compared the *Planck* compact source detections to external catalogues of radio sources. We began by constructing a band-merged catalogue based on positional coincidence and included all the sources detected above the initial  $4\sigma$  detection threshold at any of the LFI frequencies. The catalogue contained 2039 sources, many of which were detected at only one frequency. We then used this catalogue to make a position-based search for identifications with three external catalogues of radio sources using a search radius of  $1.5 \times \sigma_b$ , where  $\sigma_b = FWHM/(2\sqrt{2}\ln 2)$  can be evaluated from the fitted FWHM in Table 2. These catalogues are: (1) in the southern hemisphere, the Australia Telescope 20 GHz Survey (AT20G; Murphy et al. 2010), a catalogue of sources brighter than 40 mJy that covers the whole southern sky ( $|b| < 0^\circ$ ); (2) in the northern hemisphere, where no large-area survey at similar frequencies to AT20G is available, the 8.4 GHz Combined Radio All-sky Targeted Eight GHz Survey (CRATES; Healey et al. 2007), a compilation of flat-spectrum ( $\alpha > -0.5$ ) radio sources with nearly uniform extragalactic ( $|b| > 10^\circ$ ) coverage for sources brighter than 65 mJy at 4.8 GHz; (3) the full-sky New WMAP Point Source Catalogue (NEWPS; López-Cañiego et al. 2007; Massardi et al. 2009) covering the frequency range 23–61 GHz, that include sources brighter than 700 mJy at 23 GHz and is complete above 2 Jy. These catalogues have a similar source density, so there should not be multiple associations of AT20G, CRATES, or NEWPS sources within a *Planck* beam, and their frequencies range from 8 to 61 GHz. The NEWPS catalogue was produced by analysing the WMAP maps, and this dataset is very similar to that of *Planck* in terms of format (all-sky Healpix maps), background characteristics, and angular resolution ( $\sim 13$ – $33'$  in *Planck* LFI, vs.  $\sim 14$ – $56'$  in WMAP), which makes it a very good dataset for validation. In addition, the two catalogues, PCCS2 and NEWPS, were produced using the same source-extraction tool (the Mexican Hat wavelet). For the search radius, we use  $1.5 \times \sigma_b$ , which includes  $\sim 87\%$  of the area of the *Planck* beam, as a compromise between the arcsecond resolution of CRATES and AT20G, and the  $\sim$ degree resolution of the 23 GHz WMAP channel. In any case, given the similar source density of the catalogues, one could use a slightly larger search radius and the results would not change. As in the PCCS, the PCCS2 includes 94% of the sources in NEWPS when using a  $1.5 \times \sigma_b$  search radius, so in order to study the completeness of the catalogue deeper samples like CRATES and AT20G are needed. However, the frequencies of these two surveys, 8.4 and 20 GHz, are lower than the lowest *Planck* frequency, and variability and spectral effects

could push some of the sources below the PCCS2 detection thresholds. Thus, the completeness that we estimate by comparing the PCCS2 against these three catalogues is a lower limit. For this reason we used an alternative completeness estimate that can be derived from knowledge of the noise in the maps when the completeness is greater than 50%. If the flux density estimates  $S$  are subject to Gaussian errors with amplitude given by the noise of the filtered patches, the cumulative completeness per patch should be

$$C(S) = \frac{1}{2} + \frac{1}{2} \operatorname{erf}\left(\frac{S - q\sigma_s(\theta, \phi)}{\sigma_s(\theta, \phi)}\right), \quad (6)$$

where  $\sigma_s^2(\theta, \phi)$  is the variance of the filtered patch located at  $(\theta, \phi)$ ,  $q$  is the S/N threshold and  $\operatorname{erf}(x) = \frac{2}{\sqrt{\pi}} \int_0^x e^{-t^2} dt$  is the standard error function. The true completeness will depart from this limit when the simplifying assumptions of non-Gaussian noise and uniform Gaussian beams are broken. Using this expression, the cumulative completeness of each LFI band is derived by making use of a model of the source counts  $N(S)$  (de Zotti et al. 2005) that accounts for various source populations (flat-spectrum radio quasars, BL Lac objects, steep-spectrum sources, GPS sources, early phase gamma-ray after glows, etc.). The true completeness will depart from this limit when the simplifying assumptions of non-Gaussian noise and uniform Gaussian beams are broken.

Figure 6 demonstrates that the catalogues at 30, 44, and 70 GHz are essentially 100% complete above flux densities of 1 Jy, and for 30 and 70 GHz are still more than 95% complete down to around 0.6 Jy. The flux densities that correspond to the 90% completeness level are shown in Table 13.

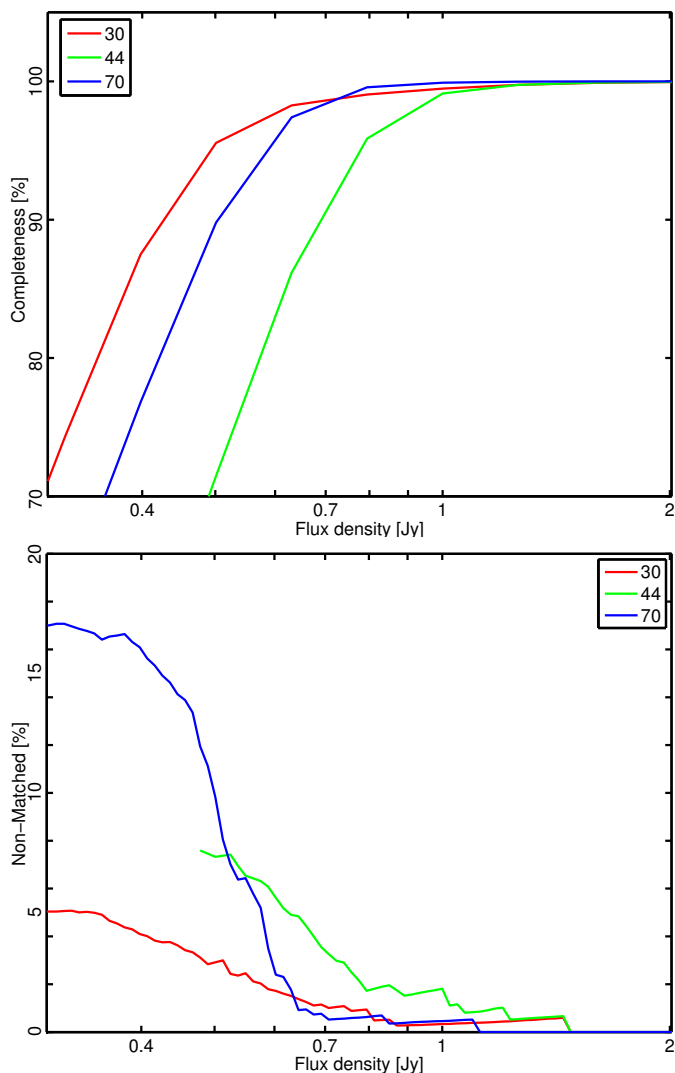
#### 3.1.2. HFI

There are no external full-sky catalogues in the HFI frequency range, so we rely on the injection of artificial sources into the *Planck* maps to establish the completeness, following the power-law models fitted to the data described in Sect. 3.2.3 and Table 4.

The completeness is determined from the injection of unresolved point sources into the real maps. Bias due to the superimposition of sources is avoided by preventing injection within an exclusion radius of  $\sigma_b$ , evaluated from the fitted FWHM in Table 2, around both existing detections in the real map and previously injected sources. We note that while superimposition of real sources will occur in the *Planck* maps, it is beyond the scope of this paper to disentangle such effects. Our definition of a point source here is a beam-shaped spike of emission, regardless of the make-up of astrophysical objects that produce the emission.

The flux from real and injected point sources contributes to the noise estimation for each patch, reducing the S/N of all detections and biasing the completeness. We prevent this effect by determining the noise properties on the maps before injecting sources, and have verified that any remaining bias on detection and parameter estimates due to injected sources is negligible. The injected sources are convolved with the effective beam computed using the FEBeCoP algorithm (Mitra et al. 2011; Planck Collaboration IV 2016; Planck Collaboration VII 2016).

We show the Monte Carlo completeness functions computed per channel in Fig. 7. We have calculated them using several cuts based on the “highest reliability catalogue” column that indicates the highest reliability catalogue to which each source belongs (see Sect. 3.2.3); as the required catalogue reliability increases, the completeness decreases. We also show the completeness for the unvalidated area of the sky containing the PCCS2E. This



**Fig. 6.** Validation of the sources in the 30, 44, and 70 GHz channels. The *top panel* shows the cumulative completeness per flux-density bin of the PCCS2 catalogue. The *lower panel* shows the number of unidentified sources per flux-density bin. These sources have no clear counterpart in any of the external catalogues used for validation. However, many of these source have been detected in more than one *Planck* channel and this implies, first, that they could be real sources and not spurious, and one can consider the number of non-matched sources presented here as an upper limit. Second, the fact that they are not in the external catalogues suggests that, if real, they could be potentially interesting objects, maybe going through a flaring phase.

area is significantly less complete than the main PCCS2 regions due to Galactic emission, where the completeness deteriorates markedly with frequency. The PCCS2 product includes noise maps at each channel, which are also shown in the middle panels of Fig. 8. These maps contain the MHW2 detection noise, defined as the standard deviation of the MHW2 filtered patches,  $\sigma_s(\theta, \phi)$ . A good approximation to the Monte Carlo completeness can be calculated for any subsection of the sky using the noise maps and the reliability threshold maps. Assuming Gaussian noise in the filtered patches, the completeness is given by Eq. (6). We compare the error function and Monte Carlo completeness estimates for the 80% reliability catalogues at each channel in Fig. 9. The effective  $\sigma_s$  that we used, and included in the data release, has been normalized across the PCCS2 region to match the effective noise from the Monte Carlo tests.

The Monte Carlo completeness drop-off is slightly wider than the error-function completeness because it includes the effects of non-Gaussian noise from the background and varying asymmetric beams. However, the discrepancy is less than 5%.

### 3.2. Reliability

The underlying philosophy of the PCCS2 was to provide a catalogue of sources with a reliability of at least 80%, which could be cut if desired by a user to generate higher reliability subsets. This has required, as explained in Sect. 2.2, the division of the HFI data into two subcatalogues, the PCCS2 and PCCS2E. The assignment to the PCCS2E is based on the position of the source on the sky. These locations are determined by the union of the Galactic region and the filament mask. Note that at 857 GHz this union represents more than half of the sky. The PCCS2E therefore contains substantially more sources than the PCCS2 in the higher frequency channels since it includes all the Galactic plane sources.

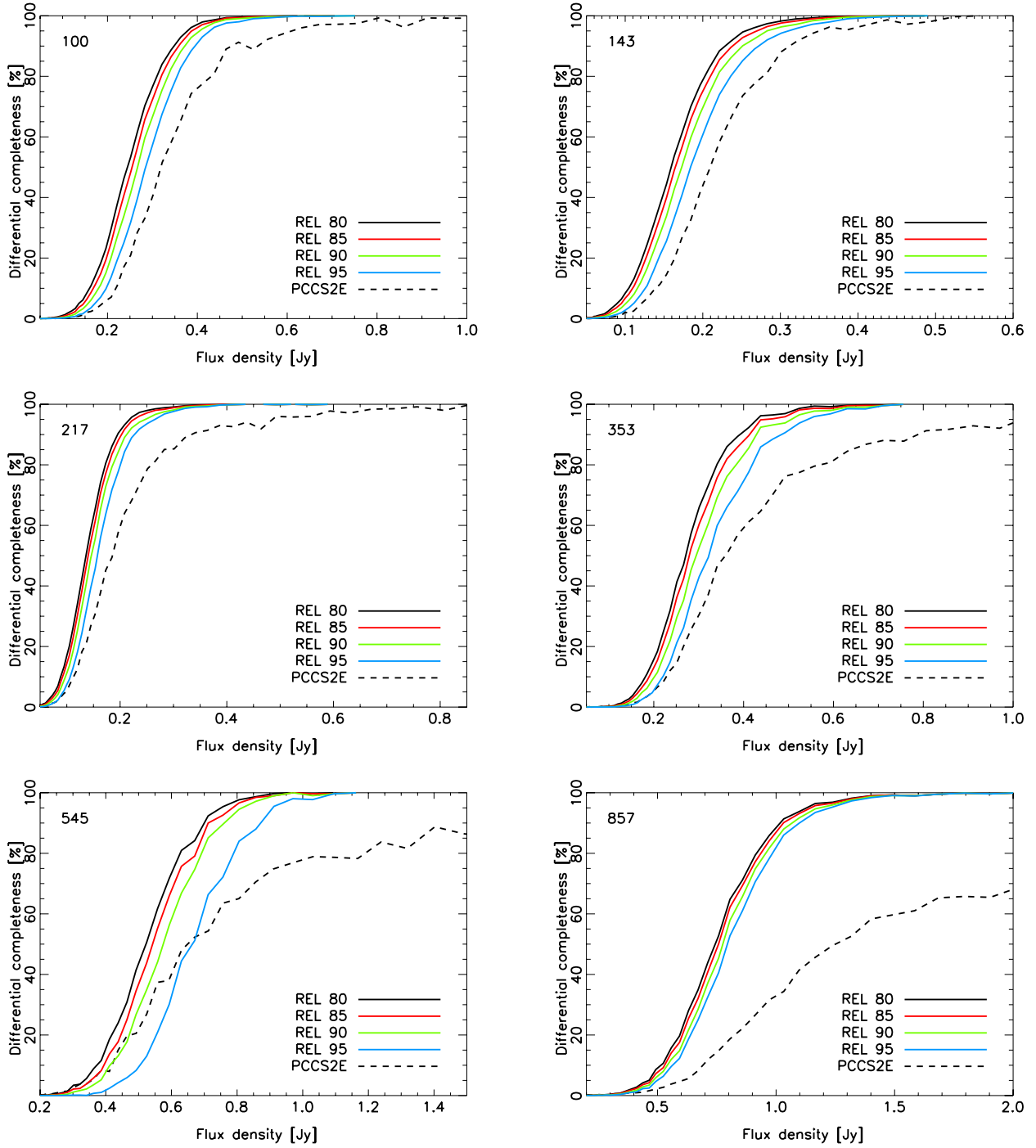
#### 3.2.1. LFI: reliability assessment

The band-merged catalogue compared with ancillary data, as described in Sect. 3.1.1, has also been used to assess the reliability of the LFI catalogues. All but 426 PCCS2 sources (out of 2039) were identified with known sources in the external radio source catalogues of CRATES, NEWPS, and AT20G. The initial estimate for the reliability, using just these external catalogues, is thus greater than 79%. The percentage of unidentified LFI sources as a function of their flux density is shown in the lower panel of Fig. 6. Associations for some of these initially unidentified sources were later found by performing a search in NED. This procedure was carried out on a source-by-source basis and some subjective judgement was required. Hence, we report a range in the possible number of sources thus identified. The sources that are positively identified by this approach are flagged as such and the associated sources are named in the PCCS2 catalogue.

Reliability at high Galactic latitudes using external catalogues: out of the 426 initially unidentified sources, 180 were at high Galactic latitudes,  $|b| \geq 20^\circ$ . More than a quarter of these were positively identified using NED, leaving 132. Given the 1161 sources detected over this latitude range, this implies a reliability of 92% for high Galactic latitude sources. It should be noted that 7–8% of the remaining 132 unidentified sources appear in multiple *Planck* bands, and are therefore likely to be real. Hence, this reliability estimate is a lower bound.

Reliability using external catalogues and taking into account multiple band detections: we also searched for identifications for all sources that appeared in two or more *Planck* bands; here we included the 100 GHz band in the analysis. Of the 426 initially unidentified sources, 133 appeared at two or more frequencies. Of these, the number that remained unidentified was 71. Given that more than half of the LFI sources (1149) appear at two or more frequencies, this implies a reliability  $>94\%$  for sources detected in two or more *Planck* bands.

Reliability using external catalogues and sources detected in a single band and with  $SNR > 5$ : we searched NED for identifications for sources detected in only a single *Planck* band with  $S/N > 5$ . Not surprisingly, the rate of identification was lower, but a few positive identifications were added. In the end we were left with 335 out of the original 426 that remained either



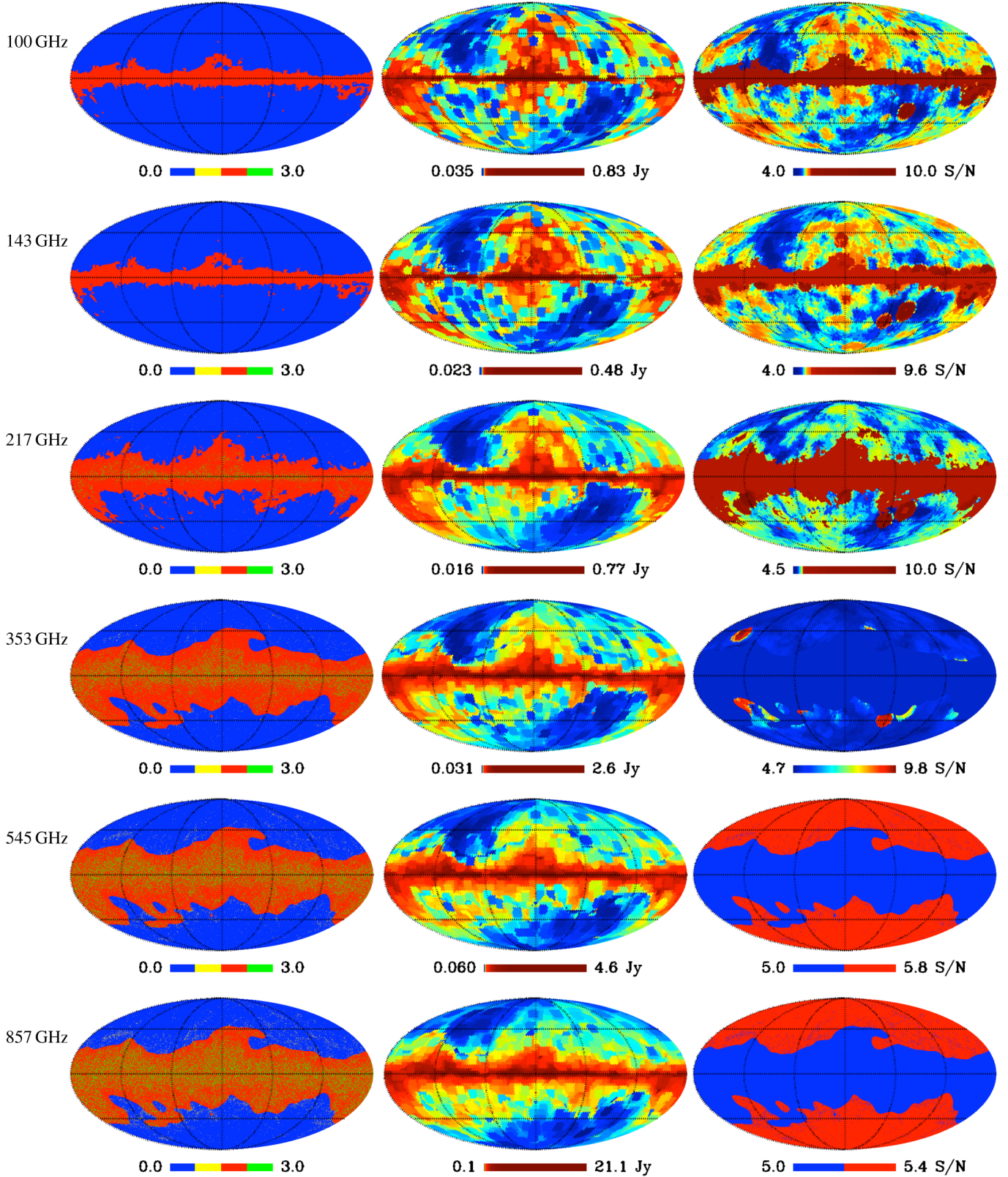
**Fig. 7.** HFI completeness results from the Monte Carlo quality assessment. Completeness is shown per channel for the 80, 85, 90, and 95% reliability catalogues, and for the PCCS2E.

unexamined or unidentified. We may therefore conclude that the overall reliability of the LFI catalogue is at least 84%.

The procedure described above was used to construct the PCCS2 for the three lowest *Planck* bands, and additionally to populate the EXT\_VAL column for them. This column summarizes the comparison with external catalogues, and is described in Sect. 5. Note that the higher-frequency bands also provide information for each source in this column, but they are not used in the reliability assessment.

### 3.2.2. HFI: filament masks

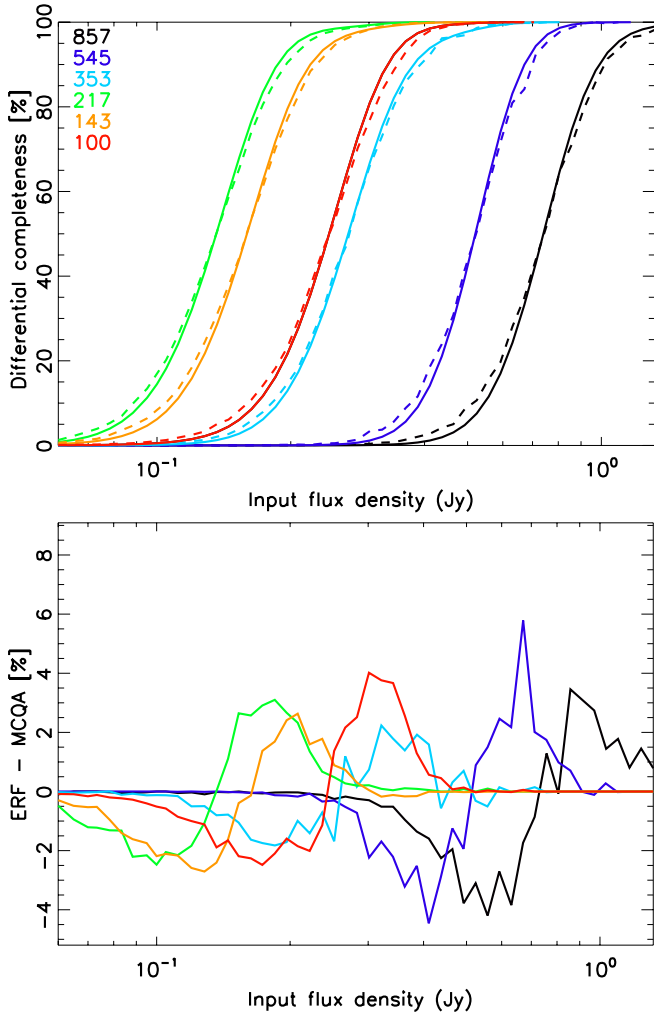
There are regions on the sky even at high Galactic latitudes in which the detection of sources cannot be trusted to high levels of reliability. The reason is that the Mexican hat wavelet algorithm used for the detection of compact sources is also efficient at edge detection. While this is ideal for point sources embedded in a Gaussian noise background, it is not optimal for a map with non-Gaussian structures where there are other edges to detect, such as dusty filaments. The impact of false detections due to these structures may in part be ameliorated by rejection criteria



**Fig. 8.** *Left:* zone masks constructed from the filament masks and the Galactic masks. The area covered by the PCCS2 is given by the zero (blue) values in the mask, and that covered by the PCCS2E is given by the non-zero values. The Galactic region is traced in red, and the filament mask is yellow outside the Galactic region and green inside it. *Centre:* rms noise level as determined by the HFI MHW2 code. *Right:* S/N thresholds applied to the raw catalogue; a flat S/N cut is applied in the region of the PCCS2E and for the PCCS2 at 545 and 857 GHz.

based on the number of connected pixels of the detection, as described in [Planck Collaboration XXVIII \(2014\)](#); however, this is not a complete solution. We wish to place source detections

occurring in these filamentary structures into the PCCS2E rather than the main PCCS2. In order to do this we need to create filament masks, which describe the regions of the sky containing



**Fig. 9.** Comparison of the error-function semi-analytic completeness derived from the  $\sigma_s$  threshold maps (Eq. (6)) and the Monte Carlo completeness estimates. *Top:* solid lines denote the error-function completeness and the dashed lines the Monte Carlo completeness. *Bottom:* difference between the two completeness estimates.

filamentary structures that pass into the wavelet filtered patches.

The obvious way to construct these masks would be to use the filtered patches themselves, after median filtering to remove the point-like objects from the patch. The difficulty with this approach is setting an appropriate threshold above which to mask. Given that these dusty structures are far from uniformly distributed across the sky, local evaluations of this threshold will not be as successful as a global one. Any practical filament mask should also be continuous; for both these reasons they cannot be created directly from the filtered patches.

A Mexican hat wavelet filtered map is very close to a difference-of-Gaussians (DOG) map if the ratio of the two FWHMs used is 2:1. The DOG map is created by smoothing the original map with two different Gaussians, creating two new maps that are then differenced<sup>5</sup>. Here the smaller of the two FWHMs used is the fitted FWHM from Table 2. A full-sky DOG map may be trivially created, and while it is not identical to the filtered patches it traces the same structures in the original map that pass into the filtered patches. In order to remove point

<sup>5</sup> This is the default approach used for finding compact sources in data from the SCUBA-2 instrument (e.g. MacKenzie et al. 2011).

**Table 3.** Fractions of sky covered by the PCCS2 catalogue, the filament mask, and the Galactic region for the HFI channels.

Channel	PCCS2 area % sky	Filament mask % sky	Galactic region % sky
100 . . . .	85.0	...	15.0
143 . . . .	85.0	...	15.0
217 . . . .	64.9	2.2	35.0
353 . . . .	47.6	7.5	52.0
545 . . . .	47.0	10.9	52.0
857 . . . .	46.3	13.9	52.0

**Notes.** No masks are required for the LFI channels, where the PCCS2 covers the entire sky. The filament mask is not required for the lowest two HFI frequency channels. Some parts of the sky are covered by *both* the filament mask and the Galactic region.

sources, the DOG map is median-filtered using a filter radius of twice the fitted FWHM (from Table 2). By thresholding this median-filtered DOG (MF-DOG) map, we can create the desired filament mask for each channel. In order to find an appropriate threshold, we select the cleanest (faintest) 25% of the sky based on the smoothed sky brightness of the 857 GHz channel map, and create a histogram of the MF-DOG map from the pixels in this region. We then fit a Gaussian to this histogram, and the filament mask is given by all the pixels in the MF-DOG map with values greater than 3 times the  $\sigma$  of this fitted Gaussian. Negative fluctuations are not masked, since they cannot lead to spurious detections. In the case of point sources in a Gaussian background, this procedure would result in an MF-DOG map that would contain solely Gaussian noise, and a mask created as above would be expected to mask 0.15% of the sky. Table 3 shows the percentage area of the filament mask for the frequency channels at which it is used; we see that the percentage area masked is well in excess of the expectation from Gaussian statistics. Additionally, we see that the area of the filament mask increases with frequency as the maps contain more and more emission from dust. Indeed, we do not need to use a filament mask for the lower two HFI frequency channels, because the dusty filamentary structures are not a problem at these frequencies.

Note that the risk of high S/N point sources located inside filamentary structures being placed inside the filament mask is limited by the fact that high S/N point sources in the DOG map are positive peaks surrounded by negative troughs. This means that once the DOG map is median-filtered the resultant level in the MF-DOG map at the location of these point sources is likely to be below the level at which thresholding occurs.

### 3.2.3. HFI: reliability assessment

As described in Sect. 2.3, we use two methods to assess the HFI reliability, the *simulation reliability* and the *injection reliability*. The simulation reliability is assessed by injecting sources into simulated maps; this simulates both the real and spurious detection components of the total counts. The injection reliability, however, involves injecting sources into the real maps; hence only the real detection component of the total counts is simulated. The real component to inject, in both cases, is evaluated using the PCCS2 above a given flux density threshold (above which we are complete) fitted to a single power-law model defined as  $N(S) \propto S^{-\alpha}$ . For each channel we provide three numbers in Table 4:  $\alpha$  is the power-law index (estimated per frequency with error in the range 0.05–0.1);  $S_{\min}$  is the minimum flux

**Table 4.** Power law model fit parameters obtained from the simulation of the source number counts in the HFI channels used in the reliability assessment.

Channel	$S_{\min}$ [Jy]	$S_{\text{taper}}$ [Jy]	$\alpha$
100 . . . .	0.3	0.1	2.54
143 . . . .	0.3	0.2	2.51
217 . . . .	0.2	0.1	2.63
353 . . . .	0.4	0.1	2.69
545 . . . .	0.7	0.1	2.59
857 . . . .	1.5	0.3	2.34

density considered when fitting the model (i.e. lower flux densities are excluded to allow for incompleteness); and  $S_{\text{taper}}$  is the flux density at which the power law was truncated for the completeness simulations to avoid dominating the injected population with unobservable faint sources. Note that there was no truncation for the reliability work (simulation or injection). Simulation reliability is preferable to injection reliability because it provides a more complete understanding of the detection properties of the catalogue, including information on how the reliability varies as a function position on the sky, as well as on S/N.

Previously, for the PCCS (as described in [Planck Collaboration XXVIII 2014](#)), the simulation reliability was used for 100–217 GHz, while injection reliability was used for 353–857 GHz. This was because the simulated maps at 353–857 GHz could not be used to produce a simulation reliability estimate. The simulated number counts and completeness were not consistent with the real data, and the discrepancies arise from deficiencies in the simulation of diffuse dust emission near the beam scale. Since then, improvements have been made in the simulations; using the FFP8 simulations ([Planck Collaboration XII 2016](#)), it is now possible to extend the use of simulation reliability to 353 GHz. These maps, however, include a leaked compact-source component from the *Planck* maps from which they were derived. As this can produce artificial, high S/N, spurious sources, we screen these from the reliability estimates by considering any detection at  $S/N > 10$  to be real. At 545 and 857 GHz, we continue to use the injection reliability estimate.

Table 3 shows the percentage area of the sky occupied by the PCCS2, for each HFI channel. This corresponds to the area in which the reliability assessment is performed. The PCCS2 covers the region of the sky not excised by the filament mask or the Galactic region. The Galactic region is determined by the area, from each channel, that must be excluded from the reliability assessment in order to achieve consistency between simulated and real catalogues. The percentage areas of the Galactic regions and filament masks are also shown in Table 3. Note that the Galactic region and the filament mask can and do overlap; their union forms the area of sky in which sources are assigned to the PCCS2E. Hence, the complement of the PCCS2 is the PCCS2E, and consequently no source can appear in both subcatalogues.

Each entry in the PCCS2 and PCCS2E catalogues contains a field, `HIGHEST_RELIABILITY_CAT`, which specifies the highest reliability subsample in which that source may be included. Hence, this field can be used to cut the catalogues to produce subsets with a reliability higher than the survey target of 80%.

For the 100–353 GHz channels we can perform the reliability assessment using simulation reliability. This allows us to define a local S/N threshold,  $q(\theta, \phi, \mathcal{P})$ , as a function of both sky

position  $(\theta, \phi)$  and target reliability,  $\mathcal{P}$ . This threshold gives a local reliability  $\mathcal{P}$  within an  $8^\circ$  radius of  $(\theta, \phi)$ . This information allows us to populate the `HIGHEST_RELIABILITY_CAT` field for all sources in the PCCS2 catalogues in these channels, and a resolution of 1% reliability. Note that, for these four channels, the option to create a higher reliability subset will also apply to spatial subsets of the original catalogue. For example, one could create a catalogue of the north ecliptic pole region to a reliability of 97%, if desired.

For the 545 and 857 GHz channels the limitations of the injection reliability mean that we are unable to define a local S/N threshold for a given reliability. Hence, we provide a global S/N threshold that will deliver the target reliability for the full catalogue. We use this approach to populate the `HIGHEST_RELIABILITY_CAT` field for these channels in steps of 5% in reliability. Since there is no local assessment, the option to create higher-reliability spatial subsets for these channels is not available, because the desired reliability will only apply to the full area covered by the catalogue. We note that the PCCS2 survey S/N threshold at 857 GHz is substantially higher than the threshold applied to build the PCCS. We have improved the modelling of the real extragalactic sources for the injection reliability estimate for the PCCS2, which results in a shallower spectral index for the input source model and fewer injected sources at low S/N. This produces a more realistic, and lower, reliability estimate at a given S/N relative to the PCCS. As the threshold has moved to higher S/N, the flux density at 90% completeness in Table 13 is now higher than for the PCCS.

The S/N threshold maps which produce the survey target of 80% integral reliability are shown in the right-hand panels of Fig. 8, for all the HFI channels. Note the flat S/N cut applied to the 545 and 857 GHz channels in the PCCS2 regions, as well as the flat  $S/N = 5$  cut applied to the PCCS2E regions. The S/N threshold HFI maps for  $\mathcal{P} = 80\%$ , 85%, 90%, and 95% are included in the data release.

### 3.2.4. HFI: comparison with H-ATLAS

As an external check on the reliability of the PCCS2 we have exploited the catalogue of submillimetre sources extracted from the full *Herschel* Astrophysical Terahertz Large Area Survey (H-ATLAS; [Eales et al. 2010](#)). The survey covers an area of about  $550 \text{ deg}^2$  at 250, 350, and  $500 \mu\text{m}$  (the two longer wavelength channels corresponding fairly closely with HFI's 857 GHz and 545 GHz). A public catalogue is available only for the H-ATLAS Science Demonstration Phase field (covering  $\approx 16 \text{ deg}^2$ ) so we have used, with permission, one that is unpublished and was released for internal use of the H-ATLAS consortium (Maddox et al., in prep.; Valiante et al., in prep.). Within the H-ATLAS fields, the PCCS2 catalogue contains 39, 44, and 121 sources at 353, 545, 857 GHz, respectively, while the PCCS2E contains two sources, both detected only at 857 GHz. We have identified, at each frequency, the PCCS2 with the H-ATLAS catalogue using a search radius equal to half the *Planck* FWHM. Increasing the search radius to one FWHM does not add any additional reliable counterparts. As expected, given the large surface density of H-ATLAS sources, at least one source is always present within the search radius. We have taken as reliable counterparts to *Planck* sources those with H-ATLAS flux densities within a factor of three of the *Planck* APERFLUX ones. Since the *Herschel* photometry does not extend to 353 GHz, to look for reliable counterparts at this frequency we have extrapolated the H-ATLAS flux densities using the spectral properties measured at higher frequencies. In the present, preliminary, version of the

**Table 5.** Positional offset between the PCCS2 and the VLA (in the sense PCCS2 – VLA) in equatorial, Galactic, and ecliptic coordinates.

Channel	Equatorial offsets		Galactic offsets		Ecliptic offsets		Positional error [arcsec]	Number of sources
	RA [arcsec]	Dec [arcsec]	longitude [arcsec]	latitude [arcsec]	longitude [arcsec]	latitude [arcsec]		
30 . . . .	$-9 \pm 6$	$-7 \pm 7$	$16 \pm 7$	$0 \pm 6$	$-1 \pm 7$	$-3 \pm 8$	78.0	66
44 . . . .	$-11 \pm 8$	$8 \pm 9$	$18 \pm 9$	$-7 \pm 8$	...	...	97.6	67
70 . . . .	$-3 \pm 5$	$-1 \pm 6$	$4 \pm 5$	$-7 \pm 6$	$-2 \pm 5$	$6 \pm 6$	58.9	70
100 . . . .	$-1 \pm 5$	$-4 \pm 5$	$7 \pm 5$	$7 \pm 5$	$9 \pm 4$	$-14 \pm 5$	53.7	70
143 . . . .	$-1 \pm 5$	$-9 \pm 4$	$-6 \pm 4$	$5 \pm 5$	$-1 \pm 5$	$-13 \pm 4$	48.8	66
217 . . . .	$5 \pm 4$	$-1 \pm 4$	$-2 \pm 4$	$3 \pm 4$	$3 \pm 4$	$-1 \pm 5$	37.5	48

**Notes.** The mean offsets in longitude and latitude (or RA and Dec) are given, together with the standard error on the mean. These offsets place strong limits on any global positional offset between *Planck* and the VLA, and hence the international celestial reference frame (ICRF). The radial positional uncertainty for an individual source, given in the positional error column, is evaluated from the standard deviations of the offset in the latitude and longitude positions, assuming no correlations between these offsets.

H-ATLAS catalogue, aperture corrections of flux densities for extended sources have been applied only for a fraction of the area. It is thus possible that a few H-ATLAS flux densities of large galaxies have been strongly underestimated and are therefore missed as reliable counterparts to *Planck* sources by the flux-density criterion. To recover them we have looked for associations of *Planck* sources with large, nearby optical galaxies. In this way we have recovered five H-ATLAS counterparts at each of the *Planck* frequencies. We find 26, 38, and 112 reliable counterparts to PCCS2 sources at 353, 545, and 857 GHz, respectively, which translates into a reliability of 26/39 (67%), 38/44 (86%), and 112/121 (93%). Neither of the two sources in the PCCS2E has a reliable H-ATLAS counterpart.

The 353 GHz channel is five identifications short of the target 80% integral reliability. Since we require consistent flux densities between *Planck* and the extrapolated values from *Herschel* for an identification, this slight deficit should not raise too much concern about the reliability of the 353 GHz catalogue.

An assessment of the expected number of matches due to chance between H-ATLAS and *Planck* sources was made using the number of *Planck* detections within the H-ATLAS area, the size of the *Planck* beams, and the number density of H-ATLAS sources with flux densities above the 90% completeness limits of the PCCS2 (scaling these limits by a factor of three, because we have taken as reliable counterparts to *Planck* sources those with H-ATLAS flux densities within a factor of three of the *Planck* APERFLUX ones). It was found that the number of random associations is  $<10^{-4}$  for all frequencies studied (353, 545, and 857 GHz).

### 3.3. Astrometry

The astrometric accuracy and positional uncertainties of the PCCS2 and PCCS2E were determined using both internal and external tests. The external validation was based on a comparison of PCCS2 source positions with those measured with the Karl G. Jansky Very Large Array (VLA), which in turn are tied to the ICRF reference frame to an accuracy well below 1". This comparison both validates the astrometric accuracy of the *Planck* catalogues and provides estimates of positional uncertainties, channel by channel. We also used simulations, in which we injected sources to test the accuracy of the positions determined by the detection algorithms.

#### 3.3.1. External tests

For the six lowest frequency channels, a direct comparison was made between the PCCS2 coordinates of bright, non-thermal radio sources and the subarcsecond precision positions determined by the VLA. Table 5 summarizes the observed offsets in position between *Planck* and VLA observations for up to 70 (depending on the frequency) compact, unconfused synchrotron sources. The positional offsets recorded in Table 5 are the averages (together with the error on the mean) of all the sources in this study; hence these results limit any *global* positional offset between the VLA and *Planck*, and do not represent the positional offset for a single source. The positional errors given in Table 5 are evaluated from the standard deviations of the offsets in latitude and longitude, and hence provide the radial error in the position of an individual source in each channel. The numbers of sources used at each channel are also given. We also examined positional offsets and uncertainties of a subset of the brightest *Planck*-VLA sources (38 sources with 70 GHz flux density  $>1.5$  Jy, 35 sources with 30 GHz flux density  $>1.9$  Jy). As expected, the positional uncertainty was reduced slightly (e.g. from 59" to 42" at 70 GHz). The offsets in equatorial and ecliptic coordinates changed by 0.5 to  $1.0\sigma$  for these bright sources. In particular the large offset in Galactic longitude at 30 GHz is reduced from 16" to 7" and the large offset in ecliptic latitude at 100 GHz is reduced from  $-14''$  to  $-7''$ .

#### 3.3.2. Internal tests

The positional accuracy of individual sources in the PCCS2 depends on the accuracy of the positions in the detection pipelines. This may be evaluated by the injection of sources into the real maps. The recovered positions are compared against the known positions of the injected sources. Table 6 shows the resulting estimates of positional accuracy. Table 7 shows the same thing, but here the population of injected sources was limited to those with  $S/N > 20$ . Note that all of the positional errors are less than the width of one HFI map pixel, which is half the width of an LFI map pixel. Also note that there is good agreement between the positional errors found from the VLA study and those found from these simulations. For the lower frequencies the position errors for sources below the 100% completeness limit must be included in the average to bring the position errors for these channels into agreement with those found from the VLA study.

**Table 6.** Native photometry (DETFLUX) bias,  $\langle\Delta_S\rangle$ , photometric recovery uncertainty, and radial position uncertainty.

Channel	DETFLUX bias [%]	stdev( $\Delta_S/\sigma_S$ )	Position error [arcsec]
30 . . . .	-2.34	0.33	50.49
44 . . . .	-4.12	1.67	59.57
70 . . . .	-12.05	3.69	44.07
100 . . . .	1.10	1.22	51.96
143 . . . .	-0.91	1.44	43.68
217 . . . .	-2.36	1.82	39.94
353 . . . .	-3.72	1.85	39.59
545 . . . .	-1.59	2.13	39.58
857 . . . .	-3.51	2.51	39.41

**Notes.** The radial position uncertainty is the 63% error radius. All were determined from source injection into the maps, using only those injected sources with input flux above the 100% completeness threshold. In the three lowest channels, the DETFLUX photometry provided in the catalogues has been corrected for this bias.

Additionally, we fitted the following functional form relating the position error,  $\sigma_r$ , to the S/N of the detection:

$$\sigma_r^2 = \left( \frac{FWHM}{d \times S/N} \right)^2 + \sigma_0^2, \quad (7)$$

where the value used for the FWHM was the fitted FWHM from Table 2, while the values of the parameters  $\sigma_0$  and  $d$  are shown in Table 8.

### 3.4. Photometry

The photometric accuracy of *Planck* is very high (see [Planck Collaboration I 2016](#); [Planck Collaboration II 2016](#); [Planck Collaboration VII 2016](#)). The consistency of the *Planck* calibration is shown in [Planck Collaboration I \(2016\)](#) to be approximately 0.2% in most *Planck* bands. The calibration of *Planck*, however, is based on the measurements of a dipole signal, and it is appropriate to ask if that accuracy extends to much smaller angular scales. The calibration depends on our knowledge of the instruments and the window functions, which in turn depends on our understanding of the beam properties in each *Planck* band. Both beam properties and calibration can also be tested by comparing, on a statistical basis, the flux densities of compact sources at different *Planck* frequencies or using different photometric methods. We refer to these tests, among others, as “internal”. We have also undertaken a direct comparison of PCCS2 flux densities with ground-based or other observations of bright sources. We refer to such comparisons as “external” tests.

#### 3.4.1. Internal consistency

**Simulations.** For the HFI channels we characterize the accuracy of source photometry by comparing the native flux-density estimates (DETFLUX) of matched sources to the known flux densities of sources injected into the real maps. The photometric accuracy is a function of S/N, and the faint detections are affected by upward bias due to noise fluctuations. In the previous PCCS, at the higher HFI frequencies, the DETFLUX estimates were found to be biased low ([Planck Collaboration XXVIII 2014](#)). This has been corrected in the construction of the PCCS2. Tables 6 and 7 show the DETFLUX bias per channel as well as

**Table 7.** As Table 6, but for all detections with  $S/N > 20$ .

Channel	DETFLUX bias [%]	stdev( $\Delta_S/\sigma_S$ )	Position error [arcsec]
30 . . . .	-2.35	1.16	37.88
44 . . . .	-3.15	1.98	44.35
70 . . . .	-13.75	11.39	39.69
100 . . . .	0.58	1.45	45.80
143 . . . .	-1.18	1.76	39.53
217 . . . .	-2.06	2.15	38.33
353 . . . .	-3.24	2.14	38.57
545 . . . .	-0.81	2.54	37.85
857 . . . .	-2.27	2.79	37.99

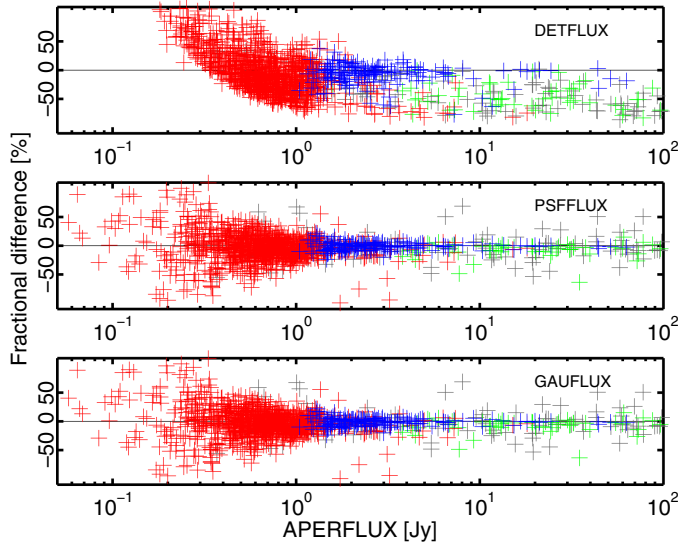
**Table 8.** Parameters  $\sigma_0$  and  $d$  determined by fitting Eq. (7), relating the position error,  $\sigma_r$ , from the simulations to the S/N of the detection.

Channel	$\sigma_0$ [arcmin]	$d$
30 . . . .	$0.267 \pm 0.001$	$2.14 \pm 0.44$
44 . . . .	$0.217 \pm 0.001$	$1.74 \pm 0.59$
70 . . . .	$0.538 \pm 0.001$	$1.68 \pm 0.23$
100 . . . .	$0.685 \pm 0.001$	$1.61 \pm 0.01$
143 . . . .	$0.615 \pm 0.001$	$1.60 \pm 0.01$
217 . . . .	$0.580 \pm 0.002$	$1.38 \pm 0.02$
353 . . . .	$0.578 \pm 0.002$	$1.43 \pm 0.03$
545 . . . .	$0.539 \pm 0.002$	$1.48 \pm 0.04$
857 . . . .	$0.546 \pm 0.0004$	$1.46 \pm 0.02$

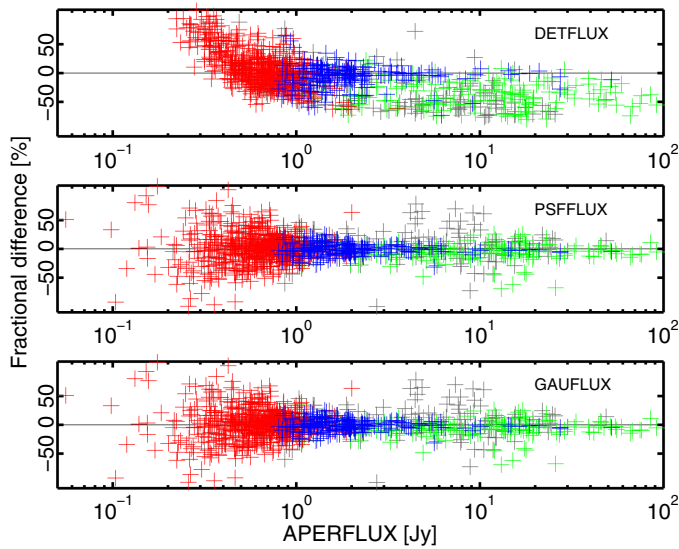
the standard deviation of  $\Delta_S/\sigma_S$ , the difference between the input and recovered flux densities normalized by the uncertainty on the flux density, which would be unity for Gaussian noise.

Comparisons of the four different flux-density estimates. We next compare values derived from the four different methods of assessing flux densities. Figures 10–13 show the results for four *Planck* channels. These comparisons are made against APERFLUX. This flux estimation method is the simplest and makes the smallest number of assumptions about the data. However, DETFLUX has smaller uncertainties than APERFLUX, which may be seen in these figures by the upward curve towards lower APERFLUX values in the comparison with DETFLUX. This may be understood as there being a clear signal present in DETFLUX when the APERFLUX is compatible with noise. Figure 14 shows the comparison against DETFLUX for APERFLUX at 30, 70, and 143 GHz. In these plots, as expected, the curvature disappears, and we see good agreement between the methods that becomes progressively noisier towards lower values of DETFLUX. For unresolved sources in regions where there is little non-Gaussianity present in the background, DETFLUX is the flux estimation method of choice, given its greater sensitivity. However, in regions of high non-Gaussian background emission, DETFLUX is less robust. This may be seen by the lack of consistency between DETFLUX and APERFLUX, in these figures, at least for the green and grey points representing sources that lie within  $5^\circ$  of the Galactic plane. As the frequency increases so do the levels of non-Gaussian emission. In the comparison between DETFLUX and APERFLUX at 353 GHz, which only contains sources at the higher Galactic latitudes, there is a large degree of scatter. Indeed, at 353 GHz and above it is advisable to favour APERFLUX over DETFLUX.



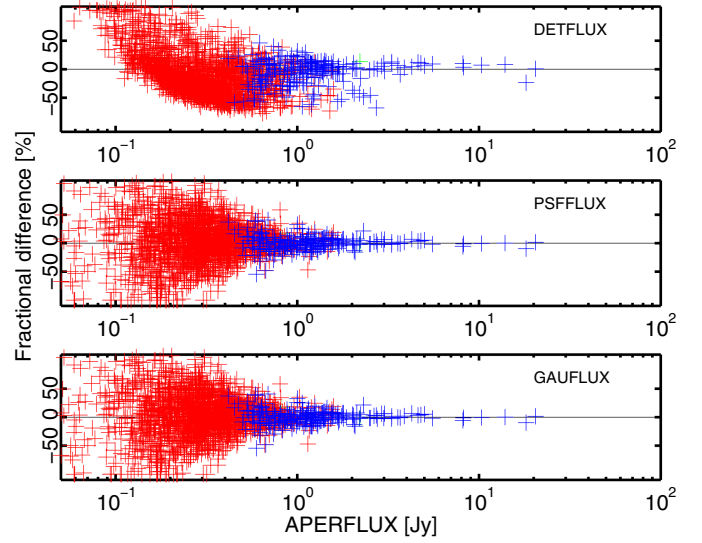


**Fig. 10.** Comparison of the DETFLUX, PSFFLUX, and GAUFLUX flux-density estimates with APERFLUX for the PCCS2 30 GHz catalogue. The fractional difference is defined as  $(S - S_{\text{APERFLUX}})/S_{\text{APERFLUX}}$ . The green and blue points correspond to sources where  $S_{\text{APERFLUX}}/S_{\text{APERFLUX\_ERR}} > 5$ . Grey and green points correspond to sources with  $|b| < 5^\circ$ , while the red and blue have  $|b| > 5^\circ$ .

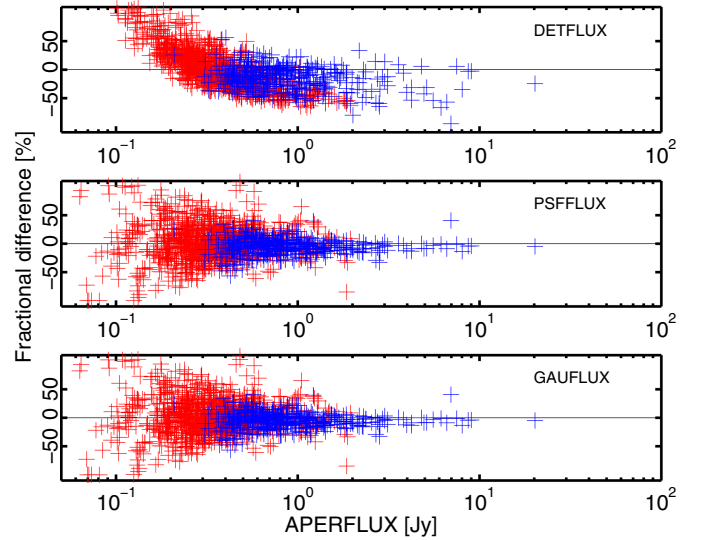


**Fig. 11.** Comparison of the DETFLUX, PSFFLUX, and GAUFLUX flux-density estimates with APERFLUX for the PCCS2 70 GHz catalogue. The fractional difference is defined as  $(S - S_{\text{APERFLUX}})/S_{\text{APERFLUX}}$ . The green and blue points correspond to sources where  $S_{\text{APERFLUX}}/S_{\text{APERFLUX\_ERR}} > 5$ . Grey and green points correspond to sources with  $|b| < 5^\circ$ , while the red and blue have  $|b| > 5^\circ$ .

**Interband comparisons.** As an additional internal test, we compared PCCS2 flux densities at one band with those in neighbouring bands. We performed this comparison for the six lowest *Planck* channels. We began by selecting all PCCS2 sources at 70 GHz with the following restrictions: flux density  $S(70) \geq 0.9$  Jy (virtually all such sources had  $S/N > 7$ ); Galactic latitude  $|b| \geq 10^\circ$ ; and no evidence of extension. We then matched these with sources in the PCCS2 at 30, 44, 100, 143, and 217 GHz. Of the 203 sources, more than 99% were detected at 30, 44, and 100 GHz as well as 70 GHz, and 97% at 143 GHz. Since virtually all the sources had synchrotron spectra, and, in general, negative



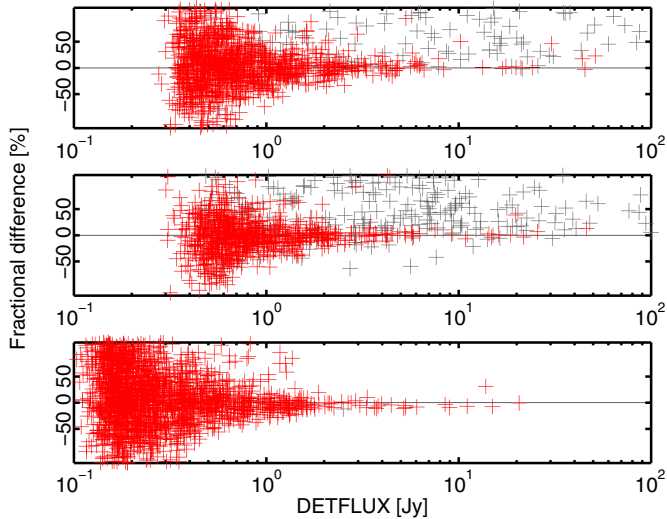
**Fig. 12.** Comparison of the DETFLUX, PSFFLUX, and GAUFLUX flux-density estimates with APERFLUX for the PCCS2 143 GHz catalogue. The fractional difference is defined as  $(S - S_{\text{APERFLUX}})/S_{\text{APERFLUX}}$ . The blue points correspond to sources where  $S_{\text{APERFLUX}}/S_{\text{APERFLUX\_ERR}} > 5$ .



**Fig. 13.** Comparison of the DETFLUX, PSFFLUX, and GAUFLUX flux-density estimates with APERFLUX for the PCCS2 353 GHz catalogue. The fractional difference is defined as  $(S - S_{\text{APERFLUX}})/S_{\text{APERFLUX}}$ . The blue points correspond to sources where  $S_{\text{APERFLUX}}/S_{\text{APERFLUX\_ERR}} > 5$ .

spectral indices, it is not surprising that only 90% of the sources could be identified at 217 GHz. We note that some of the sources not found in the PCCS2 at 217 GHz did appear in the PCCS2E; these few sources, however, were not used in this internal test.

We used this merged catalogue to calculate spectral indices for each of the 203 sources. The spectral indices were then used to make the small colour-corrections to the flux density in each band for each source. For the colour-corrections at 30 GHz we used the 30–44 spectral index, and for 353 GHz the 217–353 spectral index. For the other five bands, for band  $N$ , we used the spectral index found between bands  $N - 1$  and  $N + 1$  (e.g. for 44 GHz, we used the 30–70 spectral index). The colour-corrections we used are tabulated in [Planck Collaboration II \(2016\)](#) and [Planck Collaboration VII \(2016\)](#). The amplitude of



**Fig. 14.** Comparison of the APERFLUX flux-density estimates with DETFLUX for the PCCS2 30 GHz (top panel), 70 GHz (middle panel) and 143 GHz (bottom panel) catalogues. The fractional difference is defined as  $(S_{\text{APERFLUX}} - S_{\text{DETFLUX}})/S_{\text{DETFLUX}}$ . Grey points are sources at  $|b| < 5^\circ$ ; while red points have  $|b| > 5^\circ$ . The greater depth of the 143 GHz catalogue is clear.

**Table 9.** Slope found in the plots of predicted versus measured flux densities in five of the *Planck* bands.

Channel	Slope	Required $\Delta\alpha$
44 . . . .	$0.985 \pm 0.005$	+0.066
70 . . . .	$1.025 \pm 0.005$	-0.125
100 . . . .	$1.038 \pm 0.005$	-0.210
143 . . . .	$0.997 \pm 0.005$	+0.015
217 . . . .	$1.017 \pm 0.005$	-0.076

**Notes.** A slope  $> 1$  implies that the measured flux density exceeds the predicted value. Departures from unit slope can be explained by slight *curvature* of the spectra; we show the required change in spectral index,  $\Delta\alpha$ , to explain the departure from unity.

these corrections in a given *Planck* band ranges from around 2.5% at 70 GHz to less than 1% at 30 GHz. For a given source, the precision of the colour-corrections was typically 0.2%.

Next, we used the colour-corrected flux densities to recompute spectral indices for each source. These spectral indices were then used to predict a flux density for each source in frequency band  $N$  by assuming a constant spectral index between bands  $N - 1$  and  $N + 1$ . For instance, we interpolated between the 28.4 and 70.4 GHz flux densities to predict a 44.1 GHz flux density for each source, using the calculated spectral index for that source. These predicted values were then plotted against the actual (colour-corrected) measurements at 44.1 GHz. This operation was repeated for 70, 100, 143, and 217 GHz. If the flux-density scales of *Planck* are consistent across bands and if the spectral index is constant as assumed, we expect to see lines of unit slope. In fact, the slopes were close to unity for all five bands tested, as shown in Table 9.

We examined several different possibilities for the slight departures from unit slopes. First, we explored the possibility that CO line emission could influence the results by perturbing the flux densities. The PCCS2 flux densities used were the MHW2 estimates. The filtering removes all foreground emissions on large scales; only scales approaching the size of the beam could

affect the MHW2 flux density estimates. Thus, Galactic CO emission could introduce scatter in the 100 GHz values, but should not give significant coherent offsets. There is, however, the question of redshifted CO line emission from the sources themselves. Since the sources meeting our selection criteria are mostly bright blazars (Planck Collaboration XIV 2011), the ratio of CO line flux to continuum emission is expected to be very small.

Next, we investigated whether the statistically significant departures from unit slope in the plots of predicted versus measured flux could reasonably be explained by a breakdown in the assumption that the spectral index of the sources stays constant from band  $N - 1$  to band  $N + 1$ . For instance, the measured slope at 70 GHz is 1.0125; that is, the measured 70 GHz flux densities are about 2.55% higher than we would find by interpolating between 44 and 100 GHz, assuming no change in the spectral index between 44 and 100 GHz. If instead we allow for spectral *curvature*, the small discrepancy can be reduced or eliminated. With the simplest assumption, a sharp change of spectral index,  $\Delta\alpha$ , at 70 GHz, we find that the small excess of measured over predicted flux can be explained by  $\Delta\alpha = -0.125$  at 70 GHz. We performed similar calculations for this simple model in the other *Planck* bands (see Table 9). Spectral index changes of this magnitude are reasonable (electron ageing can account for a change in spectral index of around  $-0.5$ ); see Sect. 4 for plots of spectral index distributions for all sources in the PCCS2, not just those used in this analysis.

### 3.4.2. External consistency

The calibration of *Planck* is precise, and we have demonstrated the internal consistency of the flux densities in Sect. 3.4.1. The calibration of *Planck* is also *absolute* in the sense that it depends only on the motion of the satellite and the 0.02% accurate measurement of the CMB temperature (Fixsen 2009). Consequently, comparing *Planck* flux densities to those measured by other instruments is actually a check on the accuracy of the latter. Indeed, Butler et al. (2015) have employed *Planck* measurements to refine the centimetre-wavelength flux-density scales used at the VLA and the ATCA. Here, we summarize the results of that study and of comparisons with other CMB and submillimetre instruments and missions.

The 30 and 44 GHz channels. The comparison between *Planck* flux densities at 28.4 and 44.1 GHz and ground based observations at 22.45, 28.45, and 43.34 GHz is based on observations carried out at the ATCA and the VLA in April and May 2013. Both instruments observed a set of strong, unresolved, unconfused radio sources also scanned by *Planck* in this time interval. These observations are part of a wider effort by Perley and Stevens (in prep.) to compare the flux-density scales of the two interferometers, the VLA in the north and ATCA in the south. The *Planck* DETFLUX measurements were derived not from the PCCS2, which averages over the four years of LFI observations, but from a special map constructed using only data from 1 April to 30 June 2013. This was necessary in order to minimize the effects of source variability. Since the central frequencies of the *Planck* bands did not exactly match the frequencies employed by the ground-based instruments, we interpolated and colour-corrected the *Planck* measurements to 22.45, 28.45, and 43.34 GHz. For both purposes, we used spectral indices derived from the far more precise interferometric measurements (VLA or ATCA). A comparison of the corrected

**Table 10.** Comparison of the corrected *Planck* flux-density measurements with the ATCA, VLA, and ACT values.

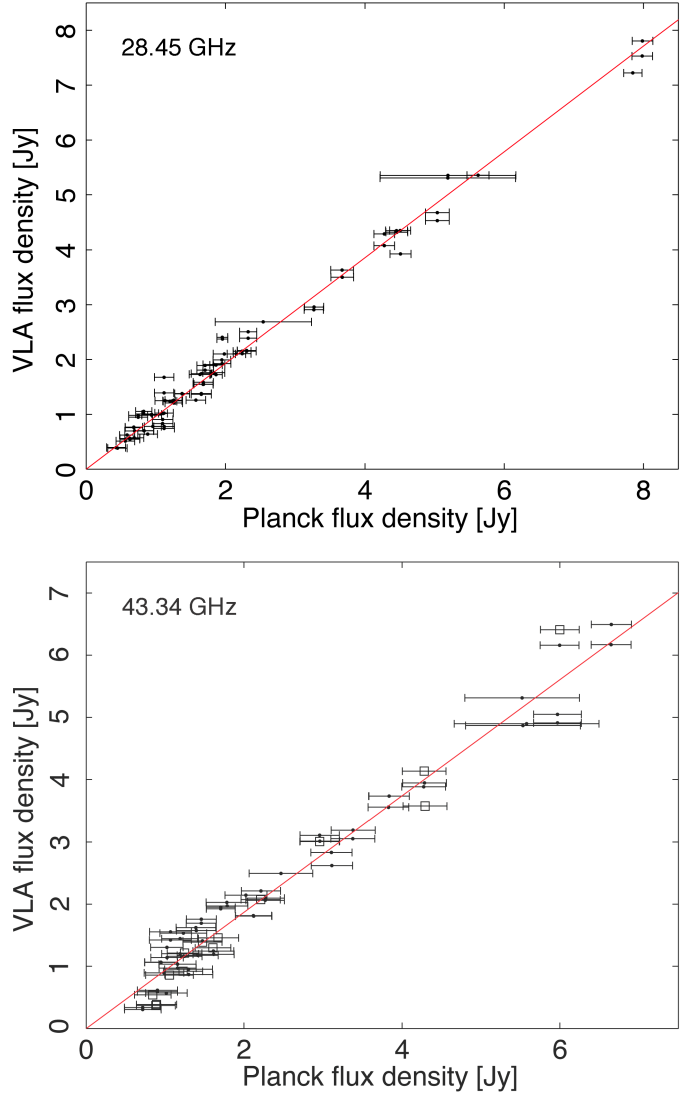
Frequency [GHz]	Flux density ratio (ground/ <i>Planck</i> )	% increment of <i>Planck</i> over ground-based measures
22.45 (ATCA) . . .	$0.99 \pm 0.017$	$1 \pm 1.7$
28.45 (VLA) . . .	$0.97 \pm 0.008$	$3 \pm 1.2$
43.34 (VLA, ATCA)	$0.94 \pm 0.013$	$6 \pm 1.7$
147.70 (ACT) . . .	$0.97 \pm 0.03$	$3 \pm 3$
217.60 (ACT) . . .	$0.96 \pm 0.03$	$4 \pm 3$

**Notes.** The error in the flux-density ratios is purely due to statistical uncertainties; the error in the % increment includes the uncertainties due to the *Planck* beams and calibration.

*Planck* measurements with the ATCA and VLA values is shown in Table 10 and Fig. 15. The *Planck* measurements are consistently slightly higher across all frequencies. These results are summarized in Butler et al. (2015), and described in greater detail in Partridge et al. (2016) where various tests of the validity of the results are presented. In particular, the effect of dropping sources found to have varied over the three-month period of the *Planck* observations is examined. The results in Table 10 are estimates derived from Butler et al. (2015). The discrepancies between the satellite and ground-based values lie close to or within the estimated error in the latter. For the flux-density scale of Perley & Butler (2013), employed at the VLA, this uncertainty is estimated to be 5%, and roughly the same level of precision may be assigned to the flux-density scale employed at ATCA. We also compared the ATCA and VLA measurements to PCCS2 30 and 44 GHz flux densities (averaged over 4 years) and found consistent results, for the same sources. As expected, source variability substantially increased the scatter. Excluding three manifestly variable sources, we find  $VLA/Planck = 0.96 \pm 0.02$  at 28.45 GHz and  $(VLA\&ATCA)/Planck = 0.93 \pm 0.03$  at 43.34 GHz. These are consistent with the more precise comparison described above. The 3% and 6% differences may be compared to the quoted 5% uncertainty in the flux density scales as given by Perley & Butler (2013).

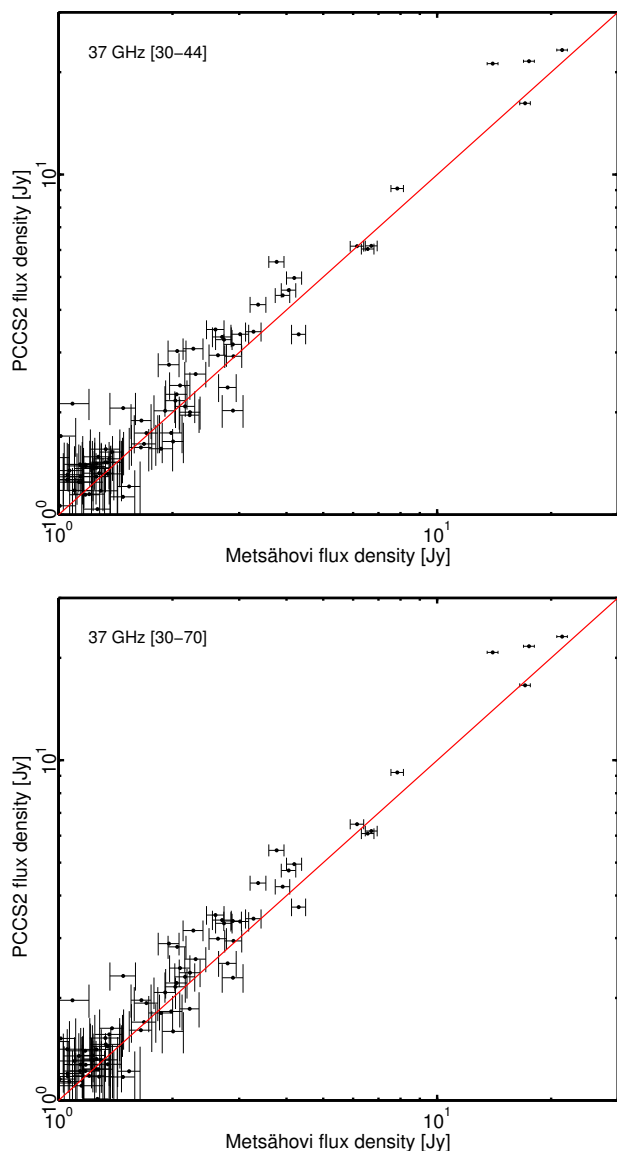
The Metsähovi Observatory is continuously monitoring bright radio sources in the northern sky at 37 GHz (Teräsanta et al. 2004). From their sample, sources brighter than 1 Jy were selected and their flux densities averaged over the period of *Planck* observations used for the PCCS2 (*Planck* Intermediate results, in prep.); note that this period corresponds to the full duration of the *Planck* mission. Hence, the uncertainties in Fig. 16 reflect the variability of the sources during the *Planck* mission. The *Planck* measurements were colour-corrected and extrapolated to the Metsähovi frequency before making the comparison. The *Planck* and Metsähovi flux densities agree at the 0.3% and 0.1% level, and an uncertainty of  $\pm 4\%$ , at 30–44 GHz and 30–70 GHz, respectively.

The 143 and 217 GHz channels. Flux densities at 143 and 217 GHz from the earlier PCCS were compared to measurements made at the Atacama Cosmology Telescope (ACT) by Louis et al. (2014). We repeated those comparisons using the new PCCS2 values, and extended the comparison to South Pole Telescope (SPT) flux densities from Mocanu et al. (2013). We employed the DETFLUX values from the PCCS2. As in Louis et al. (2014), the *Planck* flux densities were colour-corrected and extrapolated to the central frequencies of both



**Fig. 15.** Comparison of simultaneous colour-corrected flux density measurements by *Planck* and the VLA at 28.45 GHz (top) and *Planck* and the VLA (dots) or ATCA (open squares) 43.34 GHz (bottom). The best fit line is shown in red. The *Planck* 44 GHz channel is noisier than the 30 GHz channel and shows Eddington bias at low flux densities. Some sources have larger error bars than others because they lie close to the Galactic plane where the uncertainties in the measured flux densities can be large. The tiny VLA error bars have not been plotted.

ACT (147.6 and 217.6 GHz) and SPT (152.9 and 218.1 GHz), using the spectral index appropriate for each source. It is important to bear in mind that the ground-based measurements were in almost all cases far from simultaneous with those of *Planck*. Thus the variability of sources, virtually all AGN, caused significant scatter. In the case of the ACT equatorial sources, we had measurements from both the 2009 and the 2010 seasons. That allowed us to find and drop two manifestly variable sources. We also dropped two sources with thermal spectra. For SPT, Mocanu et al. (2013) present just a single flux density for each source, so in most cases we had no means of discovering and removing sources that were variable. Four sources, however, were detected by all three experiments, ACT and SPT in 2008 and *Planck* integrated over the mission. Three of these were evidently variable (and are discussed further below). For the comparison between corrected *Planck* flux densities and those of ACT at 147.6 GHz, we were left with 58 sources in common.



**Fig. 16.** Comparison between the Metsähovi and the colour-corrected PCCS2 flux densities (DETFLUX) interpolated to 37 GHz using 30 and 44 GHz (*top*) and 30 and 70 GHz (*bottom*). The multiple observations of each source have been averaged to a single flux density; the averaging was performed over the period of the full *Planck* mission, not just the epochs at which each source was observed by *Planck*. The uncertainties, therefore, reflect the variability of the sources instead of the flux-density accuracy of the measurements, which is of the order of a few mJy.

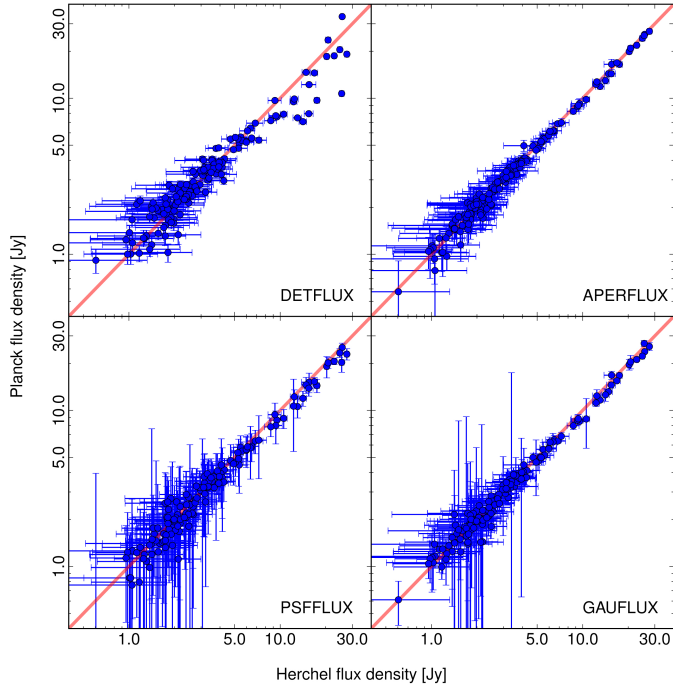
ACT flux densities were on average  $0.97 \pm 0.03$  times *Planck*'s. At 217.6 GHz, fewer ACT sources (50) were detected by *Planck*, and we find  $\text{ACT} = 0.89 \pm 0.03$  times *Planck*.

We now consider the effect on these results of sources known to be variable. First, comparison of ACT measurements made in 2009 and 2010 showed that two sources varied strongly. Dropping them changed the 147.6 GHz slope to 0.95. On the other hand, if we drop the three variable sources detected by all three experiments, the slope becomes 0.98. If we drop all five sources for which we have direct evidence of variability, the slope at 147.6 GHz settles to  $0.97 \pm 0.02$ . Since the exclusion of variable sources moves the slope both up and down in amplitude, we adopt  $0.97 \pm 0.03$  for the relation between ACT and *Planck* flux densities; ACT flux densities are about 3% lower than *Planck*'s.

At 217.6 GHz, if we remove the few sources for which we have direct evidence of variability, the slope changes to  $0.96 \pm 0.03$ .

*Planck* found fewer SPT sources than ACT sources (25 at 152.9 GHz and 30 at 218.1 GHz), and the scatter due to source variability was larger. If we include all sources, we again find the ground-based flux densities are lower than *Planck*'s:  $0.95 \pm 0.05$  at 152.9 GHz and  $0.88 \pm 0.05$  at 218.1 GHz. If we now exclude the three sources that were seen to vary between 2008 and the later *Planck* mission, the SPT results become  $0.99 \pm 0.05$  at 152.9 GHz and  $0.97 \pm 0.05$  at 218.1 GHz. We adopt these values, all lying between 0.96 and 0.99, as evidence of good agreement between the ground-based and *Planck* flux density scales at 143 and 217 GHz. The small differences between the *Planck* flux density scales at these frequencies and those measured from the ground can be compared to the following uncertainties quoted for the ground based experiments: SPT, 1.6% and 2.4% calibration uncertainty in the maps at 150 and 220 GHz, respectively (Mocanu et al. 2013); and ACT, 6% uncertainty in the flux density scale at 148 GHz (Louis et al. 2014).

The 857 GHz channel. At this frequency, there are no other all-sky surveys available matching in frequency against which the PCCS2 fluxes can be compared. However, the  $350 \mu\text{m}$  channel of the SPIRE instrument (Griffin et al. 2010) on *Herschel* (Pilbratt et al. 2010) is a close match to the 857 GHz passband of *Planck*. Pointed observations of compact extragalactic targets obtained with SPIRE can thus be used to validate the flux density measurements made in the PCCS2. The most useful set of observations from SPIRE for our purposes are those from the *Herschel* Reference Survey (HRS) (Boselli et al. 2010), a survey of the far-infrared and submillimetre properties of local bright galaxies. The published SPIRE photometry for this sample (Ciesla et al. 2012) uses either PSF fitting for sources unresolved by *Herschel* or apertures matched to the observed sizes of the sources in the *Herschel* maps. In both these cases the apertures used will be much smaller than the *Planck* beam. Since several of the HRS galaxies have nearby bright companions, and since other sources might be included in the large *Planck* beam, new flux density values were extracted for the HRS sources using apertures matched to the size of the *Planck* beams (Eales et al., priv. comm.). This allows a direct comparison of the SPIRE  $350 \mu\text{m}$  flux densities to the *Planck* 857 GHz fluxes for the same 141 objects. It should be noted that only three of these objects have not been flagged as EXTENDED by *Planck*. We should, therefore, not be surprised if the flux extraction methods (that assume a single point-like source) will be biased low. In Fig. 17 and Table 11 we show the results of this comparison for the four different flux extraction methods used in the PCCS2; namely DETFLUX, APERFLUX, PSFFLUX, and GAUFLUX. The best performing *Planck* flux-density extraction method is, perhaps not surprisingly, the method that most closely resembles the flux-density extraction method applied to the *Herschel* maps, namely APERFLUX, which shows good agreement between *Herschel* and *Planck* fluxes over the full range of source brightness. The worst performing method, in contrast, is DETFLUX, which shows an increased scatter, and an overall bias to lower *Planck* values for the brighter sources. This bias is expected if the sources are not truly point-like. For a population of slightly extended sources we expect a noticeable downward bias for the brighter sources, which disappears into the noise for fainter objects. This pattern of bias for the brighter sources which disappears once these sources are excluded is also seen for PSFFLUX. The increased scatter seen for the brighter sources with



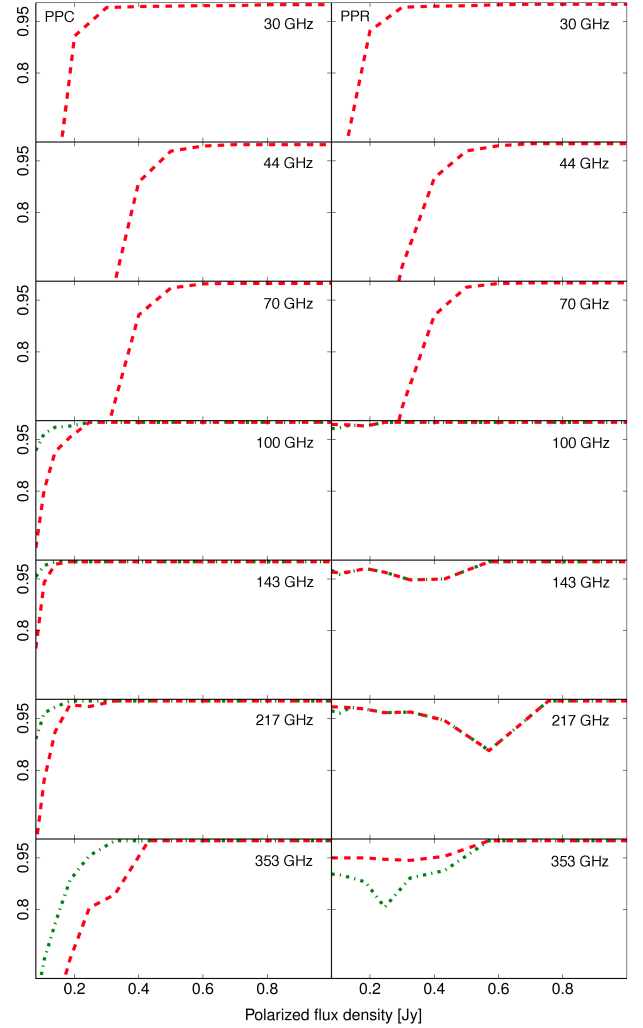
**Fig. 17.** Comparison of flux densities from *Planck* and *Herschel* at  $350\ \mu\text{m}$  (857 GHz) using the *Herschel* Reference Survey. The one-to-one lines are shown in red.

**Table 11.** Comparison of flux-density measurements from *Planck* and *Herschel* at 857 GHz ( $350\ \mu\text{m}$ ).

Extraction method	Flux density ratio ( <i>Herschel</i> / <i>Planck</i> )	
	All 141 HRS sources	Discarding $S_{\text{HRS}} > 10\ \text{Jy}$
DETFLUX . . . . .	$1.045 \pm 0.010$	$0.982 \pm 0.019$
APERFLUX . . . . .	$1.019 \pm 0.011$	$1.009 \pm 0.021$
PSFFLUX . . . . .	$1.065 \pm 0.022$	$1.016 \pm 0.038$
GAUFLUX . . . . .	$1.056 \pm 0.013$	$1.024 \pm 0.024$

**Notes.** The *Planck* measurements for all flux-extraction methods are lower than the *Herschel* results. If, however, the 17 sources in the HRS sample with flux densities greater than 10 Jy are excluded from the analysis, then the flux-density ratios for all flux-extraction methods are within  $1\sigma$  of unity.

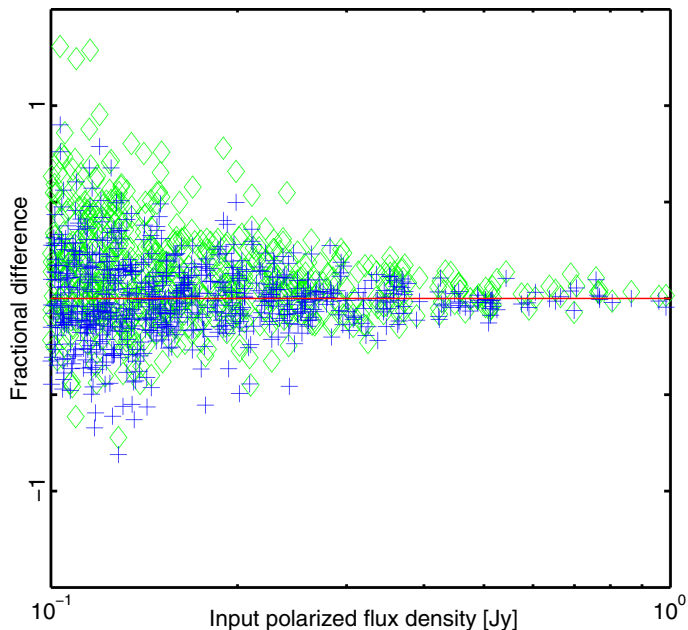
DETFLUX probably arises from errors in the recovered position. This is due to the relationship between the scale of the wavelet used and the pixel size in the maps. For this channel (857 GHz) the small beam size and the increased level of foregrounds in the map mean that the optimum scale for the wavelet is very narrow with respect to the map pixels. This makes the flux-density estimate extremely sensitive to errors in the recovered position of the source. This effect is most pronounced at this channel and for the brighter sources. A similar bias seen in GAUFLUX is a little more difficult to explain, but again may result from the assumption that sources are single and point-like. A double source, for instance, may pose difficulties in the flux-density estimation resulting in a bias low. We conclude that there is a good match between the PCCS2 flux densities at 857 GHz and *Herschel* flux densities in the matching  $350\ \mu\text{m}$  SPIRE band. We also conclude that, for most purposes concerned with the flux-density measurement of compact sources like the galaxies discussed here, APERFLUX is the most appropriate flux-density measure to use for the higher frequency channels.



**Fig. 18.** *Left:* polarized photometric completeness (PPC). *Right:* polarized photometric reliability (PPR). Red dashed lines: derived with the common method applied to both LFI and HFI. Green dot-dashed lines: including the marginal polarization data (HFI only). From *top to bottom*, 30–353 GHz. The plots were constructed using the PCCS2 catalogue only.

### 3.5. Polarization measures

To validate the polarization measurements in the PCCS2 and PCCS2E catalogues, we rely on simulations based on the injection of sources with known properties into the *Planck* polarization maps between 30 and 70 GHz and the FFP8 simulated maps (Planck Collaboration XII 2016) between 100 and 353 GHz. It should be noted that the injection of sources into the real maps has the advantage that many thousands of sources can be used to test the analysis; however this procedure does not simulate the leakage due to the bandpass mismatch. The FFP8 maps do contain this effect, although there are only hundreds rather than thousands of polarized sources. Both approaches, however, allow us to test the fidelity of the polarized flux densities and polarization angles produced by our analysis pipelines. They also allow us to compute measures for the completeness and reliability of recovered polarization measurements. Since the extraction of these measurements is non-blind, based on the positions provided by the analysis of the temperature maps, these terms for the polarization pipelines only have any meaning given that the source is real.



**Fig. 19.** Comparison between the LFI and HFI implementations of the maximum-likelihood estimator code to measure polarized flux densities. The comparison was performed using the 100 GHz FFP8 maps, and the locations of the point sources included in the simulation, because the polarization pipelines perform non-blind extractions. The recovered fractional difference of the polarized flux densities of the two methods, defined as  $(\text{recovered} - \text{true})/\text{true}$ , is plotted against the true polarized flux density, as simulated in the FFP8 maps. The results from the LFI pipeline, IFCAPOL, are shown by the green diamonds, and the results from the HFI pipeline, PwSPOL, are shown by the blue crosses.

We define the “polarization photometric completeness” (PPC) as the percentage of polarized sources correctly identified as polarized above a given true polarized flux density, and “polarization photometric reliability” (PPR) as the percentage of polarized sources whose polarized flux density is contained in the interval defined by the best-fit value and  $\pm 3\sigma$  errors. Figure 18 shows the PPC and PPR as a function of the true and estimated polarized flux density, respectively, for the PCCS2 for all the polarized channels. The red dashed lines show the results for the subsets of significantly polarized sources, whose measurements are provided for both LFI and HFI, while the green dot-dashed lines show the results when marginally polarized sources are also included in the analysis. Here we see that the inclusion of the marginal data increases the completeness with only a minimal decrease in the 353 GHz channel reliability. The negative “kinks” in the reliability curves of the 217 and 353 GHz channels are caused by the same single source. This source was detected in the intensity maps with  $S/N = 151.5$  (217 GHz) and the recovered flux density was underestimated by around  $23\sigma$ , where  $\sigma$  is the estimated error on the flux density. The dramatic underestimation of the flux density was caused by the recovered position of the source being offset from the true position by 1.27 arcmin. In this  $S/N$  regime such an offset is sufficient to explain the failure of the PPR criterion, as the polarized flux density will be underestimated by more than  $3\sigma$ .

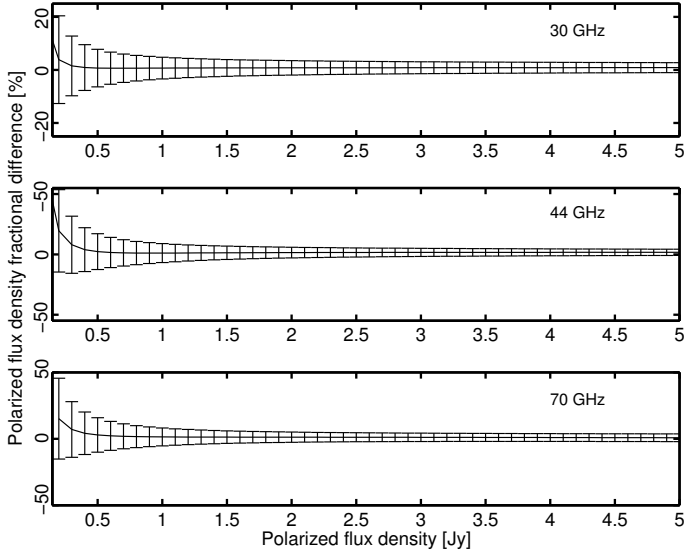
A comparison between the LFI and HFI implementations of the common procedure for extracting the polarization measurements for the significantly polarized sources was performed. Figure 19 shows a comparison of the recovered polarized flux densities (for each implementation), and the true polarized flux density. We have assessed the performance of each method, and

find that above 250 mJy, where we are complete, the average recovered polarized flux density is within 1% of the true value for IFCAPOL and within 0.8% for PwSPOL, and that they are within 0.2% of each other.

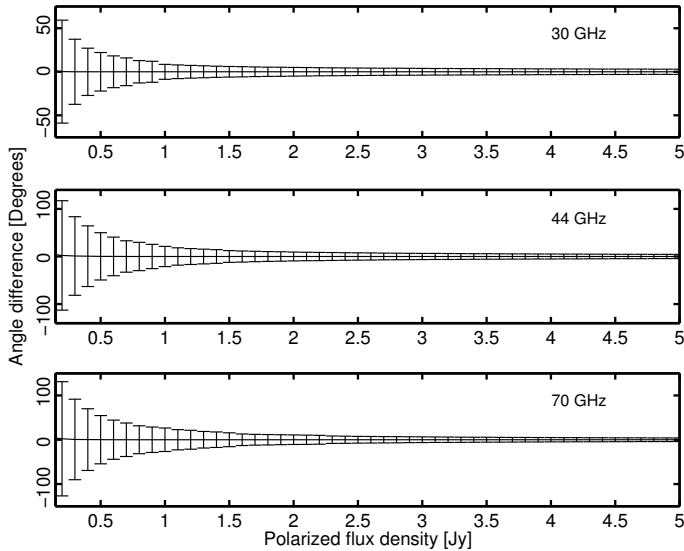
### 3.5.1. Internal consistency

30–70 GHz. In order to assess the performance of the maximum likelihood estimator used to provide the polarization measurements in the three lowest *Planck* channels (IFCAPOL), we used Monte Carlo simulations. Point sources were simulated and convolved with the appropriate Gaussian effective beam from Table 2 for each channel, and were injected into HEALPix  $N_{\text{side}} = 4096$  maps. These maps were then downgraded to  $N_{\text{side}} = 1024$  to match the pixelization of the LFI maps, and the source maps were added to the *Planck* 2015 (PR2)  $Q$  and  $U$  maps. The sources were injected away from known bright radio sources. In all, 37 000 sources, in 50 flux-density bins, were injected into the  $Q$  and  $U$  maps. The pipelines were run given the positions of these simulated sources, producing polarized flux density and polarization angle measurements. The results of the Monte Carlo simulations on the recovery of the polarized flux densities are shown in Fig. 20. We can see that the polarized flux densities are recovered in an unbiased way for strongly polarized sources, and that the faintest ones suffer from Eddington-type bias. Figure 21 shows the equivalent plot for the polarization angle and here we can see that the angle is recovered successfully for all channels, where the uncertainties increase towards fainter polarized flux densities. Based on these simulations, we computed the polarization photometric completeness and reliability, shown in Fig. 18. In the simulations we injected sources at all Galactic latitudes, and we did not apply any Galactic cut. We find that our catalogues are complete at the 90% level at 200 mJy (polarized flux density) at 30 GHz, and at 400 mJy at 44 and 70 GHz. At the 600–700 mJy level the three catalogues are complete. A summary of these results can be found in Table 14 (Sect. 4).

100–353 GHz. The recovery of the polarized flux densities from the FFP8 simulations, using the method common to both LFI and HFI, is shown in Fig. 22 for the PCCS2 and the PCCS2E. The PCCS2 polarized flux density estimates are reliable across the full range of flux densities and considerably more reliable than the PCCS2E. Given that the PCCS2E catalogue covers the Galactic plane region this is hardly unexpected. The polarized flux densities are unbiased over the range of values where the survey is complete, but for the fainter sources a positive bias is present, as expected from Eddington-type bias. Figure 23 shows the recovery of the polarization angle, which is unbiased over the full polarized flux-density range, although the errors in its recovery increase as the polarized flux density of the source decreases. This behaviour is exactly what is expected if our assumptions made in Sect. C.2 hold; namely that  $\sigma_Q \approx \sigma_U$ , and that they are uncorrelated. Consider sources with a given polarization angle in the range of polarized flux densities which suffer from Eddington bias: the required upward noise fluctuations could come from  $Q$  or  $U$  or both. Once the polarization angle is evaluated, if our assumptions hold, then the average value found for the angle will be unbiased but its dispersion will be much larger than for the brighter sources. In Fig. 23 we also see that the measurements in the PCCS2E are again less reliable than the PCCS2.



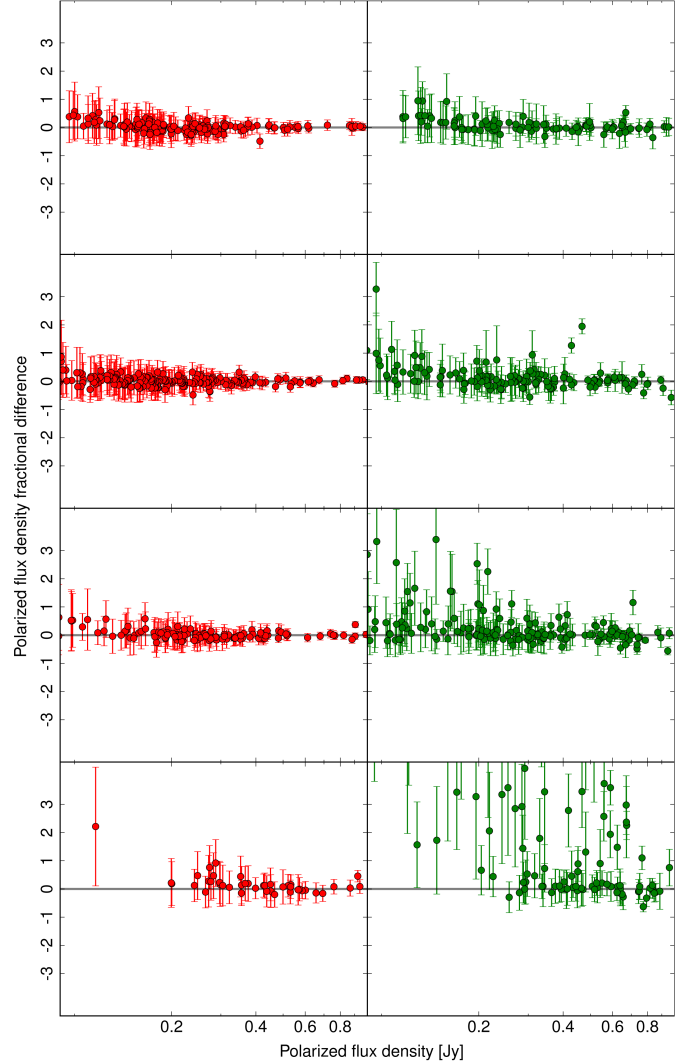
**Fig. 20.** Internal validation using Monte Carlo simulations to assess the recovery of the polarized flux density for the 30, 44, and 70 GHz channels. In these simulations, point sources were injected into the  $Q$  and  $U$  maps with 50 different polarized flux density values, starting at 0.2 Jy and increasing with a step size of 0.1 Jy. The fractional difference, defined as  $(\text{recovered} - \text{true})/\text{true}$ , is plotted against the true polarized flux density. The recovered polarized flux densities are unbiased, except for the faintest sources, where the effect of Eddington-type bias is seen.



**Fig. 21.** Internal validation using Monte Carlo simulations to assess the recovery of the polarization angle of the 30, 44, and 70 GHz channels. In these simulations, point sources spanning the full range of polarization angles were injected into the  $Q$  and  $U$  maps with 50 different polarized flux density values, starting at 0.2 Jy and increasing with a step size of 0.1 Jy. The difference between the recovered and true angles is plotted against the true polarized flux density. Here we see there are no biases in the recovery of the polarization angle, although obviously the uncertainty increases for fainter sources.

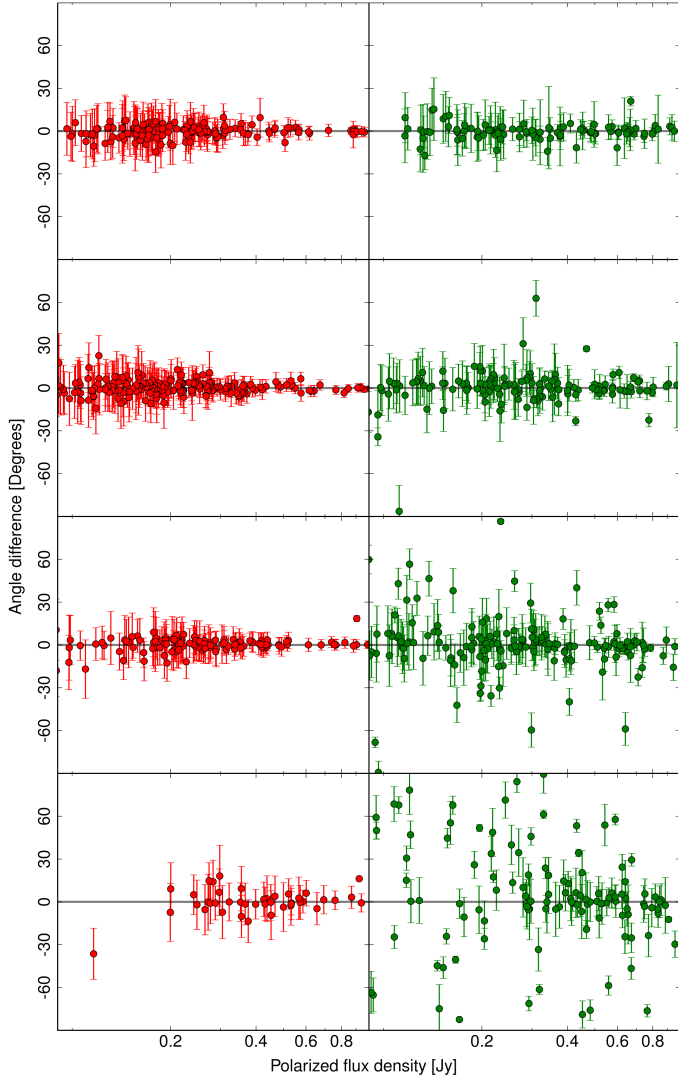
### 3.5.2. External consistency

The limited number of polarimetric millimetre surveys, the small number of bright *Planck* sources with a high significance in polarization, and the fact that the majority of polarized sources are variable, makes it difficult to validate the *Planck* polarized flux densities with external datasets.



**Fig. 22.** Fractional difference between the true and recovered polarized flux densities, *from top to bottom*, for the 100–353 GHz FFP8 simulations. *Left* (red): PCCS2. *Right* (green): PCCS2E. Here the fractional difference is defined as  $(\text{recovered} - \text{true})/\text{true}$ . These are the significantly polarized sources, as found by the common method, and the uncertainties associated with the best-fit estimates are  $\pm 3\sigma$  error bars. Eddington-type bias is seen at lower polarized flux densities.

One of the objects from the catalogue that we have studied in detail is Tau A, also known as M1 or the Crab Nebula. This object is resolved in the higher frequency *Planck* channels and may not be the best source for validation at these frequencies; nevertheless it is the brightest compact source in polarization in *Planck* and has been thoroughly studied in other experiments. In Table 12 we compare the total intensity and polarized flux densities, polarization fraction, and polarization position angle for Tau A with measurements from WMAP (Weiland et al. 2011) and the IRAM 30 m telescope at 89 GHz (Aumont et al. 2010). In general, it is assumed that the polarization position angle of Tau A is constant across the frequency range of interest, up to at least 353 GHz. In Table 12 one can see that the *Planck* polarization position angles (as measured by the maximum likelihood filtering method and by aperture photometry) are significantly different from those of WMAP and IRAM at some frequencies. We have investigated these discrepancies and found that there



**Fig. 23.** Difference between the recovered and true polarization angles, from top to bottom, for the 100–353 GHz FFP8 simulations. *Left* (red): PCCS2. *Right* (green): PCCS2E. These are the significantly polarized sources, as found by the common method, and the uncertainties associated with the best-fit estimates are  $\pm 3\sigma$  error bars.

are multiple factors in LFI and HFI affecting our measurements of the position angles of Tau A that deserve further attention.

First, at the position of Tau A in the Stokes  $U$  maps one can see a small spurious signal that is affecting the angle measurements. For this object, most of the polarized signal is in the Stokes  $Q$  map, and  $U$  makes very little contribution to the total polarized flux density (quadrature sum of  $Q$  and  $U$ ). However, as shown in Table 12, when we calculate the polarization position angle with either method, the contribution from the spurious signal has the effect of changing the position angles by up to  $5^\circ$  from the  $-88.2$  measured at IRAM (Aumont et al. 2010). This spurious signal has been introduced by the complex cross-terms in the polarized beams, which are normally expected to be very small and below the map noise level, but show up here because Tau A is so bright. In an attempt to remove this effect, we have produced maps where we have deconvolved the beam and fitted for spurious signals. Results for LFI frequencies, from the ArtDeco map-making pipeline at the LFI DPC, are shown in Col. 7 of Table 12. These new measures of position angle agree with the expected value from IRAM and WMAP. However, we

caution that these new maps are under development and the measurements should be used with caution. There is an ongoing effort, not yet completed, to generate a similar set of maps for the HFI frequencies, in order to understand whether similar spurious signals affect the HFI polarization angle measurements. The tests that we have carried out with the new LFI maps indicate that the polarized flux densities and angles of the other sources in the catalogue are mostly unchanged, but some sources with high polarized flux density may be marginally affected.

Second, the angular size of Tau A measured with IRAM at 89 GHz (Aumont et al. 2010) shows that it will be slightly resolved by *Planck* in the HFI channels. This could have an impact on the flux densities and polarization position angles measured with both the filtering method and with aperture photometry. In particular, the filtering method assumes that the sources are unresolved, so the flux densities derived with this method should be regarded as lower limits if the source is extended. In the case of aperture photometry, the integration radius that we use in HFI is too small for a source as large as Tau A. We have therefore increased the aperture radii to  $2 \times (FWHM^2 + \theta_{\text{Tau A}}^2)^{1/2}$ , where  $\theta_{\text{Tau A}} = 4'$  as measured by IRAM, and recomputed the angles for the four HFI channels with polarization capabilities. This improves the agreement between the HFI position-angle measurements and those from WMAP and IRAM, except at 353 GHz. The results are shown in Col. 7 of Table 12.

Third, as shown in Planck Collaboration VI (2016) and Planck Collaboration VIII (2016), different methods have been used in LFI and HFI for correcting the frequency maps for a global leakage signal from total intensity into polarization due to the bandpass mismatch. In practice, this means that the LFI frequency maps have not been corrected, whereas the HFI ones have. The global bandpass corrections applied to the maps are not the same as the local corrections that we apply in this paper for point sources, which depend on the spectrum of each source (see Appendix C). However, even though our techniques to extract the flux densities of the sources in the  $Q$  and  $U$  maps will remove most (if not all) of the global correction if the sources are point-like, this may not be true for extended sources. To test this, we have extracted the polarization position angles from HFI maps where the global bandpass correction had not been applied. The results are shown in Table 12 and in Fig. 24, where we compare the polarization position angles from WMAP and IRAM with the new measurements from *Planck*. The recovered angles between 100 and 217 GHz are very similar to the case where the global bandpass mismatch had been applied, except at 353 GHz, where the new angle is in much better agreement with the other *Planck*, WMAP, and IRAM measurements.

These analyses show the complexity of the *Planck* maps in polarization, particularly for bright extended objects like Tau A, where we had to fit and remove the spurious signal in the LFI, increase the integration aperture radii in the HFI, and remove the global bandpass correction at 353 GHz, in order to achieve a consistency within  $2^\circ$  in polarization position angle between *Planck* and WMAP or IRAM. Tau A is the only very bright polarized source in our maps, and the limited amount of polarization information available at *Planck* frequencies for other sources limits our ability to conclude that the polarization angles of the rest of the sources in the catalogue are not affected by these issues. Therefore, as in the case of Tau A, the polarization position angles should be used with caution. In future releases of the *Planck* products we will revisit this issue.

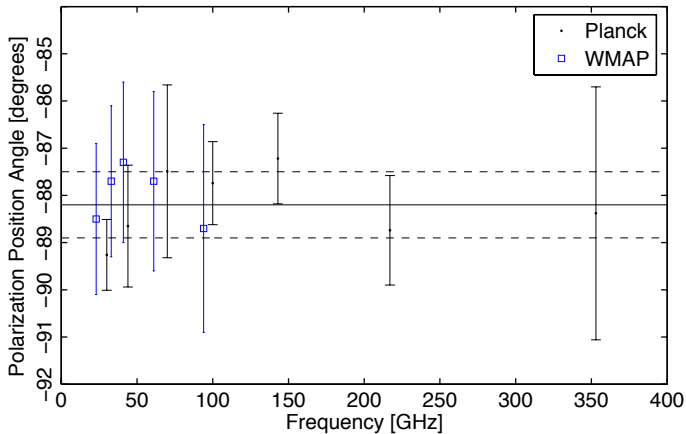
In addition, we have cross-matched the Plateau de Bure interferometer (PdBI) polarimetric survey of 86 AGN at 100 GHz (Trippe et al. 2010) with the *Planck* 70 and 100 GHz PCCS2



**Table 12.** Total intensity and polarized flux densities, polarization fraction, and polarization position angles for Tau A measured from the *Planck* full-mission maps at 30 to 353 GHz, WMAP at 23 to 94 GHz (Weiland et al. 2011), and with the IRAM 30 m telescope at 89 GHz (Aumont et al. 2010).

Freq [GHz]	$I$ [Jy]	$P$ [Jy]	$P/I$ [%]	Pol. angle <sup>a</sup> [deg]	Pol. angle <sup>b</sup> [deg]	Pol. angle <sup>c,d</sup> [deg]	Pol. angle <sup>e</sup>
30	344.23 ± 0.27	24.44 ± 1.05	7.10 ± 0.33	-84.54 ± 0.54 ± 0.50	-83.71 ± 1.40 ± 0.50	-89.26 ± 0.25 ± 0.50	...
44	292.68 ± 0.23	19.07 ± 1.10	6.51 ± 0.51	-88.34 ± 0.32 ± 0.50	-86.93 ± 0.47 ± 0.50	-88.65 ± 0.79 ± 0.50	...
70	259.99 ± 0.11	20.55 ± 0.61	7.90 ± 0.32	-84.24 ± 0.23 ± 0.50	-85.03 ± 1.32 ± 0.50	-87.49 ± 1.33 ± 0.50	...
100	215.16 ± 0.06	15.54 ± 0.14	7.22 ± 0.06	-88.53 ± 0.11 ± 0.62	-87.52 ± 0.13 ± 0.62	-87.59 ± 0.26 ± 0.62	-87.74 ± 0.26 ± 0.62
143	167.10 ± 0.04	12.02 ± 0.08	7.19 ± 0.05	-84.85 ± 0.13 ± 0.62	-85.72 ± 0.15 ± 0.62	-87.03 ± 0.35 ± 0.62	-87.22 ± 0.34 ± 0.62
217	124.21 ± 0.04	10.09 ± 0.08	8.12 ± 0.06	-87.33 ± 0.12 ± 0.62	-88.73 ± 0.18 ± 0.62	-88.84 ± 0.55 ± 0.62	-88.74 ± 0.55 ± 0.62
353	82.17 ± 0.67	9.88 ± 0.17	12.02 ± 0.23	-86.11 ± 0.37 ± 0.62	-85.15 ± 0.37 ± 0.62	-85.16 ± 1.93 ± 0.62	-88.38 ± 2.06 ± 0.62
23	383.80 ± 9.60	27.17 ± 0.68	7.08 ± 0.25	-88.50 ± 0.10 ± 1.50	...	...	...
33	342.80 ± 6.40	23.80 ± 0.44	6.94 ± 0.18	-87.70 ± 0.10 ± 1.50	...	...	...
41	317.70 ± 8.60	22.12 ± 0.60	6.97 ± 0.27	-87.30 ± 0.20 ± 1.50	...	...	...
61	276.00 ± 5.20	19.31 ± 0.36	7.00 ± 0.19	-87.70 ± 0.40 ± 1.50	...	...	...
94	232.80 ± 9.70	16.60 ± 0.73	7.13 ± 0.43	-88.70 ± 0.70 ± 1.50	...	...	...
89	195.00 ± 11.0	14.50 ± 3.20	8.80 ± 0.02	-88.20 ± 0.20 ± 0.50	...	...	...

**Notes.** <sup>(a)</sup> Position angle for *Planck* calculated using the maximum likelihood filtering method. <sup>(b)</sup> Position angle for *Planck* calculated using aperture photometry. <sup>(c)</sup> Position angle for *Planck* LFI channels (30, 44, and 70 GHz) calculated using the maximum likelihood filtering method on the special beam deconvolved maps. <sup>(d)</sup> Position angle for *Planck* HFI channels (100, 143, 217, and 353 GHz) calculated using wider aperture photometry to allow for the angular extent of Tau A. <sup>(e)</sup> Position angle for *Planck* HFI channels (100, 143, 217, and 353 GHz) calculated using wider aperture photometry, and using HFI maps for which the diffuse bandpass correction has not been applied. Note: In the *Planck* channels, the statistical error bars in the polarization position angle of Tau A do not reflect the true uncertainties of these measurements. In addition to the statistical error, a 0°5 systematic error has to be added to the LFI measurements (Planck Collaboration III 2016) and 0°62 to the HFI measurements (Planck Collaboration VIII 2016) as indicated by the second ± symbol. Similarly, the WMAP errors in the polarized position angle are statistical and a systematic error of 1°5 has been added (Weiland et al. 2011).



**Fig. 24.** Polarization position angles for Tau A from WMAP (blue squares, Weiland et al. 2011) and *Planck* (black dots). The IRAM measurement from Aumont et al. (2010) is also shown as a solid line, where a  $\pm 1\sigma$  uncertainty is shown with dashed lines.

catalogues, finding two sources in common (PKS 0851+202 and 3C 273). For these sources we see good agreement: the *Planck* polarized flux densities are  $509 \pm 106$  mJy and  $515 \pm 102$  mJy at 70 GHz, and  $566 \pm 38$  mJy and  $503 \pm 36$  mJy at 100 GHz, as compared with  $561 \pm 156$  mJy and  $418 \pm 118$  mJy measured by PdBI, for PKS 0851+202 and 3C 273, respectively.

We have also cross-matched the recent IRAM polarimetric survey from Agudo et al. (2014) at 86 GHz, again with the *Planck* 70 and 100 GHz PCCS2 catalogues. Although there are 130 and 133 sources common to both samples, if we restrict the comparison to those with measured *Planck* polarized flux densities (rather than upper limits), we are left with five and seven

sources at 70 and 100 GHz, respectively. At 70 GHz, two of the five sources (3C 273 and 3C 279) have similar polarized flux densities in both data sets, 559 and 522 mJy in IRAM, as compared with  $519 \pm 93$  and  $368 \pm 85$  in *Planck*. At 100 GHz, three of the seven sources (3C 273, 3C 279, and PKS 1055+01) have similar polarized flux densities, 522, 559 and 305 mJy in IRAM as compared with  $566 \pm 38$ ,  $430 \pm 37$ , and  $349 \pm 31$  mJy in *Planck*, respectively.

Additionally, we have compared the polarized flux densities found for 3C 273, the only bright source in polarization in the sample of sources observed simultaneously with the VLA and *Planck* in the spring of 2013. The *Planck* 30 GHz polarized flux density (colour-corrected for comparison with the VLA) was  $854 \pm 82$  mJy, while the VLA observed  $843 \pm 50$  mJy. At 44 GHz the *Planck* polarized flux density was  $567 \pm 131$  mJy, as compared with  $623 \pm 70$  mJy seen by the VLA.

### 3.6. Summary of validation

The several internal and external validation tests described in Sect. 3 allow us to assess reliability and completeness as a function of flux density in each *Planck* band. These tests also allow us to assess the accuracy of positions and flux densities tabulated in the PCCS2 and PCCS2E catalogues. With the possible exception of a 6% or  $1-1.5\sigma$  difference between *Planck* flux densities measured in the noisy 44 GHz map and those measured from the ground, no clearly significant discrepancies in any of these quantities was found. We thus conclude that both positions and flux densities in the PCCS2 are valid within the tabulated statistical errors in total intensity. Note, however, that we have no direct test of the flux densities scales at 353 and 545 GHz. Regarding the measurements in polarization, the number of external surveys

**Table 13.** PCCS2 and PCCS2E characteristics compared with those of the PCCS.

Channel	30	44	70	100	143	217	353	545	857
Freq [GHz] . . . . .	28.4	44.1	70.4	100.0	143.0	217.0	353.0	545.0	857.0
$\lambda$ [ $\mu$ m] . . . . .	10 561	6807	4260	3000	2098	1382	850	550	350
<i>Number of sources</i>									
PCCS2 . . . . .	1560	934	1296	1742	2160	2135	1344	1694	4891
PCCS2E . . . . .	...	...	...	2487	4139	16 842	22 665	31 068	43 290
Union PCCS2+PCCS2E . . . . .	...	...	...	4229	6299	18 977	24 009	32 762	48 181
PCCS <sup>a</sup> . . . . .	1256	731	939	3850	5675	16 070	13 613	16 933	24 381
<i>Number of sources</i> – in extragalactic zone <sup>b</sup>									
PCCS2 . . . . .	745	367	504	1742	2160	2135	1344	1694	4891
PCCS2E . . . . .	...	...	...	0	0	26	289	839	2097
Union PCCS2+PCCS2E . . . . .	...	...	...	1742	2160	2161	1633	2533	6988
PCCS <sup>a</sup> . . . . .	572	258	332	1483	1779	1745	1424	3566	7270
<i>Flux densities [mJy]</i> – in extragalactic zone <sup>b</sup>									
PCCS2 : minimum <sup>c</sup> . . . . .	376	603	444	232	147	127	242	535	720
: 90% completeness . . . . .	426	676	489	269	177	152	304	555	791
: uncertainty . . . . .	87	134	101	55	35	29	55	105	168
PCCS2E : minimum <sup>c</sup> . . . . .	...	...	...	...	...	189	350	597	939
: 90% completeness . . . . .	...	...	...	...	...	144	311	557	927
: uncertainty . . . . .	...	...	...	...	...	35	73	144	278
PCCS <sup>a</sup> : minimum <sup>c</sup> . . . . .	461	825	566	267	169	140	273	445	668
: 90% completeness . . . . .	575	1047	776	300	190	180	330	570	680
: uncertainty . . . . .	109	198	149	62	39	33	65	119	188

**Notes.** <sup>(a)</sup> Planck Collaboration XXVIII (2014). <sup>(b)</sup> 30–70 GHz: as in PCCS, the extragalactic zone is given by  $|b| > 30^\circ$ . 100–857 GHz: outside of Galactic region where the reliability cannot be accurately assessed. Note that for the PCCS2E the only sources that occur in this region lie in the filament mask. <sup>(c)</sup> Minimum flux density of the catalogue in the extragalactic zone after excluding the faintest 10% of sources.

available at these frequencies in polarization is very limited. In particular, we have compared the flux densities in polarization of Tau A, the Crab nebula with recent measurements of WMAP and other high resolution instruments on the ground and we have not found significant discrepancies in the polarized flux densities. However, we find a small discrepancy in the measurement of the polarization angle of Tau A in some of the *Planck* channels. For this object, one of the brightest compact sources in polarization, there is a small amount of signal in the  $U$  maps at the position of the source, where little or no signal is expected for this object. This signal, much smaller than the signal in the  $Q$  map, does not have an effect in the measurement of the total polarized flux density since the  $Q$  and  $U$  flux densities are added in quadrature (as shown in Eq. (1)), but it can explain the discrepancy in the polarization angle with respect to external measurements. Since our statistical errors do not account for this small systematic effect, when we propagate the errors in the measurements of the polarized flux density into the errors in the measurement of the polarization angle, the errors that we obtain can be underestimated.

#### 4. Characteristics of the PCCS2

In Fig. 1, we displayed the sensitivity of the PCCS2 compared with the PCCS, the ERCSC, and several other CMB projects. For the PCCS2 we define the sensitivity to be the flux density at the 90% completeness limit for each *Planck* channel. The

improvements between the PCCS2 and the PCCS are most apparent for the LFI channels. This is to be expected given the larger increase of data for LFI than for HFI in the full mission. Additionally, for the higher frequency channels the foregrounds are a significant noise source for the detection of compact sources; the reduction of the instrumental noise resulting from longer integration may therefore not increase the depth of the catalogue as much as might be expected. Finally, the estimated sensitivity of the catalogue is worse at 857 GHz (Sect. 3.2.3), owing to the improved understanding of the reliability.

Table 13 compares the characteristics of the PCCS2, the PCCS2E, and the PCCS. The total number of sources in each catalogue is given as well as the number outside the Galactic region. The numbers of sources in the extragalactic zone in general increase between the PCCS and the union of the PCCS2 and PCCS2E. For the highest three frequency channels, the union of the PCCS2 and PCCS2E catalogues contains many more sources than the PCCS due to the lower S/N threshold applied in the PCCS2E than in the Galactic region of the PCCS. In the extragalactic zone, we compare the average uncertainty on the flux density and the 90% completeness values. We can see that the PCCS2 has lower uncertainties and is consequently more complete than the PCCS, except at 857 GHz, where the completeness has dropped (see Sect. 3.2.3).

Table 14 shows the characteristics of the subset of sources with significant polarized emission, for both the PCCS2 and PCCS2E catalogues. The majority of the significantly polarized

**Table 14.** PCCS2 and PCCS2E polarization characteristics for sources with polarized emission with significance >99.99%.

Channel	30	44	70	100	143	217	353
Number of significantly polarized sources in PCCS2 . . . . .	122	30	34	20	25	11	1
Minimum polarized flux density <sup>a</sup> [mJy] . . . . .	117	181	284	138	148	166	453
Polarized flux density uncertainty [mJy] . . . . .	46	88	91	30	26	30	81
Minimum polarized flux density completeness 90% [mJy] . . . . .	199	412	397	135	100	136	347
Minimum polarized flux density completeness 95% [mJy] . . . . .	251	468	454	160	111	153	399
Minimum polarized flux density completeness 100% [mJy] . . . . .	600	700	700	250	147	257	426
Number of significantly polarized sources in PCCS2E . . . . .	...	...	...	43	111	325	666
Minimum polarized flux density <sup>a</sup> [mJy] . . . . .	...	...	...	121	87	114	348
Polarized flux density uncertainty [mJy] . . . . .	...	...	...	52	44	55	178
Minimum polarized flux density completeness 90% [mJy] . . . . .	...	...	...	410	613	270	567
Minimum polarized flux density completeness 95% [mJy] . . . . .	...	...	...	599	893	464	590
Minimum polarized flux density completeness 100% [mJy] . . . . .	...	...	...	835	893	786	958

**Notes.** <sup>(a)</sup> Minimum polarized flux density of the catalogue of significantly polarized sources after excluding the faintest 10% of sources. For the LFI channels we have not considered the sources that have been flagged as unidentified. There are nine, one, and one of these unidentified sources at 30, 44, and 70 GHz, respectively.

**Table 15.** Sources matched between neighbouring channels.

Channel	No. sources	No. matched		Fraction matched	
		Above and below	Above or below	PCCS2 and PCCS2E	(PCCS)
30 <sup>a</sup> . . .	1560	...	799	51.2%	(50.1%)
44 . . .	934	700	851	91.1%	(90.8%)
70 . . .	1296	735	1113	85.9%	(86.8%)
100 . . .	4229	1047	3049	72.1%	(71.6%)
143 . . .	6299	2734	5163	81.9%	(81.9%)
217 . . .	18 977	3837	14 928	78.7%	(66.1%)
353 . . .	24 009	12 171	20 867	86.9%	(88.7%)
545 . . .	32 762	17 003	28 423	86.8%	(85.8%)
857 <sup>b</sup> . . .	47 156	14 578	35 390	75.0%	(74.9%)

**Notes.** Given that, for the HFI channels, the sky area corresponding to the PCCS2 and PCCS2E is different for every channel, the comparison between frequency channels must necessarily be performed on the union of the PCCS2 and PCCS2E. The fraction matched from the same analysis applied to the previous PCCS is shown in brackets in the last column, for comparison purposes. Note that 217 GHz is different from other bands in the ratio of the number of above-and-below matches compared to the number of above-or-below. This is of course because of the change of spectral index at that point, as discussed in Sect. 4 and Figs. 25 and 26. <sup>(a)</sup> The 30 GHz channel is only matched with the 44 GHz channel above. <sup>(b)</sup> The 857 GHz channel is matched above with a catalogue extracted from the IRIS maps using the HFI–MHW. Both catalogues are cut with the IRIS mask prior to matching.

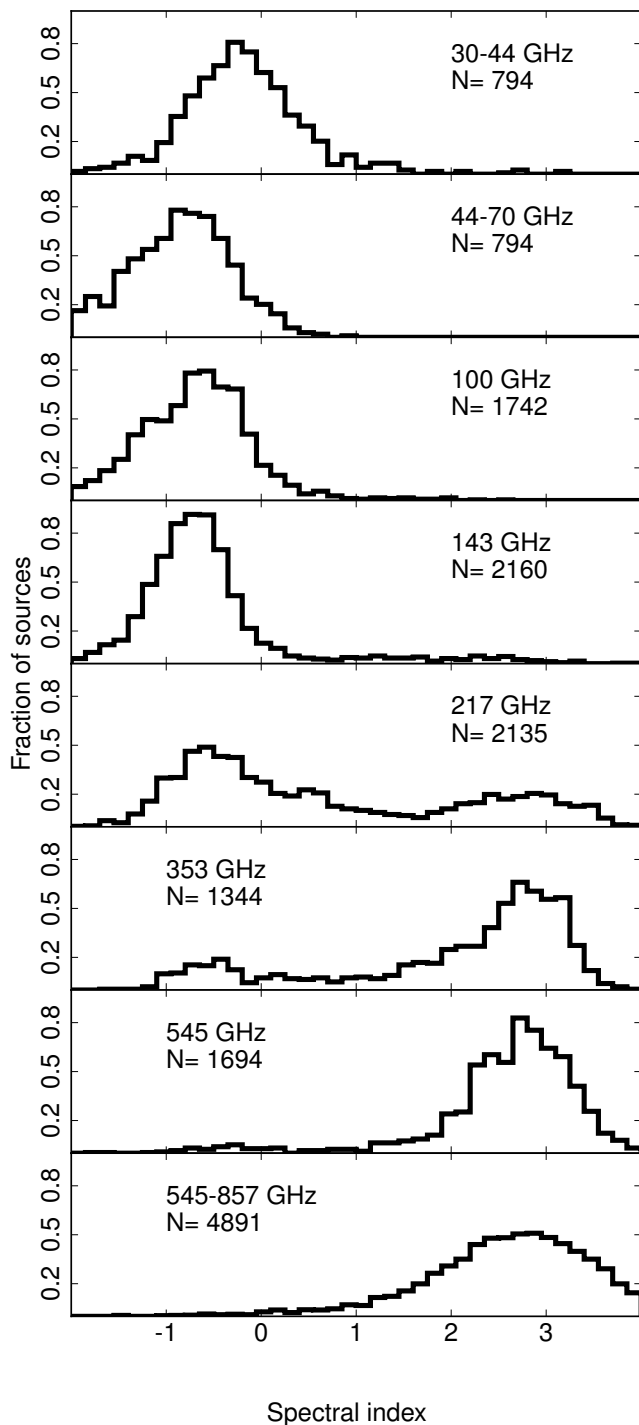
sources are in the Galactic plane region; hence for the HFI channels the majority of these sources are in the PCCS2E catalogue.

Table 15 shows the numbers of sources internally matched in adjacent frequency channels, within the union of the PCCS2 and PCCS2E. It shows the number of sources matched *both* above and below in frequency (e.g. sources at 100 GHz found in both the 70 and 143 GHz catalogues), those matched *either* above or below in frequency (a less stringent criterion), and the percentage of sources so matched. Note that sources matched by the “above or below criterion” will include as a subset those sources meeting the more stringent “above and below” criterion. A source is considered to be matched if the positions are closer than the larger FWHM of the two

channels. A catalogue was extracted from the IRIS 100  $\mu$ m map (Miville-Deschênes & Lagache 2005) using the MHW2 pipeline, and used as the neighbouring channel above 857 GHz. The IRIS mask, which removes around 2.1% of the sky, was applied to the 857 GHz catalogue before performing this comparison, and this reduces the number of sources in the union to 47 156, a decrease of about 2.1%. The number of matches given for the 857 GHz channel only includes sources outside the IRIS mask. For the 30 GHz channel, the matches were evaluated using only the channel above, 44 GHz. The low percentage of internal matches of the 30 GHz channel results from two factors: the generally negative spectral index of the sources at these frequencies; and the relatively low sensitivity of the 44 GHz receivers.

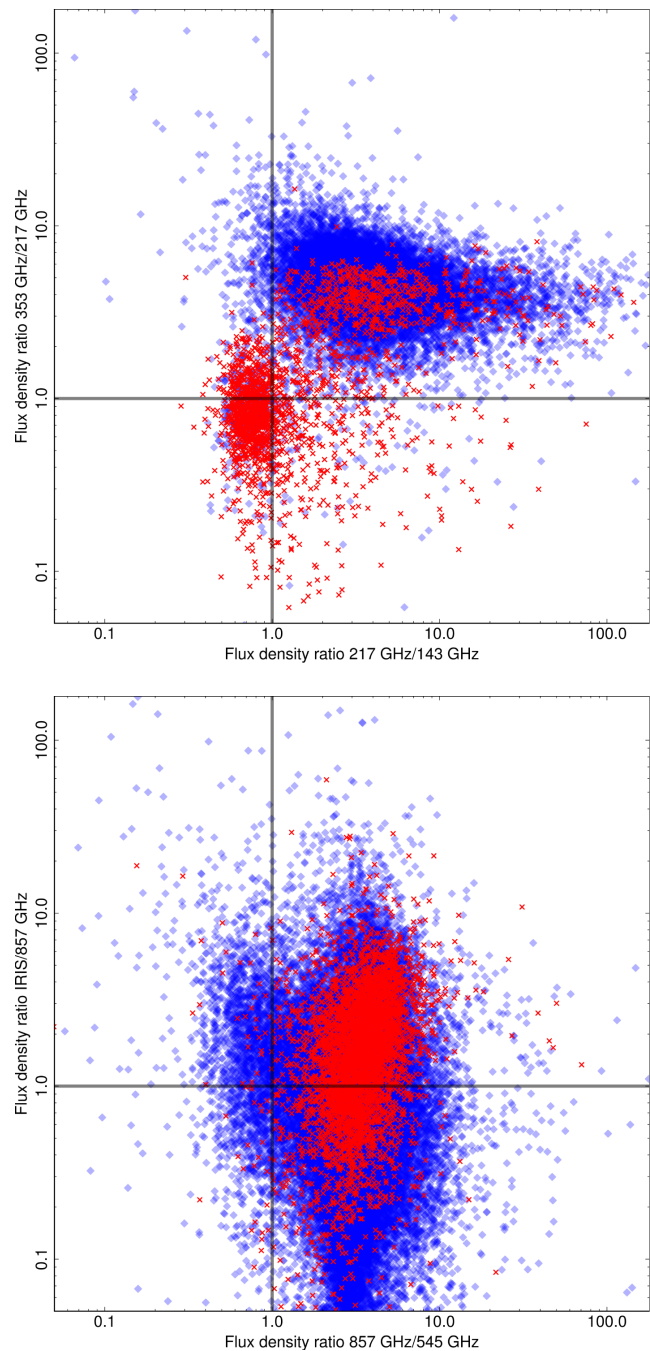
Figure 25 shows histograms of the spectral indices obtained via the non-blind flux density extraction from the neighbouring channels. As expected, the high-frequency channels (545 and 857 GHz) are dominated by dusty galaxies and the low-frequency ones are dominated by synchrotron sources, where the change in the dominant source population occurs between 217 and 353 GHz. It can also be seen that there is a shift in the peak of the histogram between the top two panels, between 30–44 GHz and 44–70 GHz and above. The reason for this is a steepening of the spectral indices of radio sources, which has been seen previously (Massardi et al. 2009; Planck Collaboration XIII 2011; Planck Collaboration XXVIII 2014).

Figure 26 shows colour–colour plots for sources from the PCCS2 and the PCCS2E. The positions in the catalogue at the common frequency in the colour–colour plot are used to perform a non-blind extraction of the flux densities from the maps at the neighbouring frequencies. These are used together with the common frequency-channel flux densities to construct the colour–colour plot. The common frequency in the top panel is 217 GHz, and here we can see the two populations, which are also seen in the spectral-index histogram (Fig. 25), for the PCCS2. Also apparent is the domination of the PCCS2E at this frequency by thermal sources, since the PCCS2E includes sources in the Galactic plane. The bottom panel uses the IRIS map and the *Planck* 545 GHz maps for the non-blind extraction of flux densities at the locations of the 857 GHz catalogues. The PCCS2 colour–colour distribution is consistent with a population of cold sources with a narrow range of temperatures (around 10–40 K) in the range



**Fig. 25.** Histograms of spectral index for sources in PCCS2. The changes in the source populations with frequency are clearly visible, the lower frequencies are dominated by synchrotron sources and the higher frequencies by dusty ones. At the intermediate frequencies both source populations are discernible. Between the *top two panels*, there is a visible shift in the peak of the histogram. This is due to a steepening of the spectral indices of the radio sources. In each panel we give  $N$ , the number of sources in the histogram.

of spectral indices is shown in Fig. 25. The larger dispersion of values in the PCCS2E by comparison, is indicative of the greater noise levels in the region of sky corresponding to the PCCS2E as well as a broader distribution of temperatures for the sources.



**Fig. 26.** Colour–colour plots. Red crosses represent sources from the PCCS2 and blue diamonds sources from the PCCS2E. *Top*: common frequency 217 GHz. We can see the non-thermal and thermal source populations of the PCCS2; the PCCS2E contains significantly more thermal sources than the PCCS2, as expected given that PCCS2E contains the Galactic plane region. *Bottom*: common frequency 857 GHz. The PCCS2 is consistent with a population of cold sources spanning a narrow range in temperature, whereas the PCCS2E shows a wider distribution of source properties.

## 5. The PCCS2: access, content and usage

The PCCS2 is available from the *Planck* Legacy Archive<sup>6</sup>. It is composed of 15 single frequency catalogue FITS files, one per LFI channel and two per HFI channel. In addition there are associated maps, again provided as FITS files, which are

<sup>6</sup> <http://www.cosmos.esa.int/web/planck/pla>

described further in Sect. 5.1. Additional information about the catalogue content and format can be found in the Explanatory Supplement<sup>7</sup>, in the FITS file headers, and in the first PCCS paper (Planck Collaboration XXVIII 2014). Here we summarize the catalogue contents, focusing on the additional features of the PCCS2 catalogues.

- Source identification: NAME (e.g. PCCS2 030 G184.54–05.78).
- Position: GLON and GLAT contain the Galactic coordinates, and RA and DEC give the same information in equatorial coordinates (J2000).
- Flux density: the four estimates of flux density (DETFLUX, APERFLUX, PSFFLUX, and GAUFLUX) in mJy, and their associated uncertainties.
- Source shape: the elliptical Gaussian fit to the source; i.e. the semi-axes, and orientation.
- Polarization measurements: the polarized flux density and polarization angle and their associated errors for significantly polarized sources; provided for all seven of the nine *Planck* channels that have polarization data (30–353 GHz). The polarization angles are defined as increasing anticlockwise (north through east) following the IAU convention; the position angle zero is the direction of the north Galactic pole.
- Marginal polarization measurements: measurements for less significantly polarized sources, as described in Sect. C.2; these are provided for the 100–353 GHz channels only.
- Source extension: the EXTENDED flag is set to 1 if a source is extended. A source is extended if the geometric mean of the elliptic Gaussian fit to the source is greater than one-and-a-half times the fitted FWHM from Table 2.
- External validation: EXT\_VAL contains a summary of the inter-channel and external validation. See the definition below.
- Positional coincidence identification with a previous *Planck* catalogue: the ERCSC and PCCS columns indicate the names of the ERCSC and PCCS counterparts, if they exist, at that channel.
- Degree of reliability: in the PCCS2 catalogue the HIGHEST\_RELIABILITY\_CAT column contains the highest reliability catalogue to which the source belongs.
- Reason for inclusion in PCCS2E: the WHICH\_ZONE flag encodes why the source has been placed in the PCCS2E.
- Cirrus indicators: a fraction of the sources detected in the upper HFI bands could be associated with Galactic interstellar medium features or cirrus. For the 217–857 GHz channels, the CIRRUS\_N and the new column, SKY\_BRIGHTNESS, may be used as cirrus indicators. The CIRRUS\_N column is defined as in PCCS, the number of sources detected at 857 GHz (using a uniform S/N threshold of 5) within a 1° radius of the source. The SKY\_BRIGHTNESS is defined as the mean 857 GHz brightness within a 2° radius of the source. See Sect. 5.2 for details.

Note that all flags are evaluated per frequency channel. Two flags require information from the 857 GHz channel for their evaluation, CIRRUS\_N and SKY\_BRIGHTNESS. These are, however, evaluated independently for each frequency channel for which they are provided. This means, for example, a source that has been observed at 545 and 857 GHz at slightly different positions in each channel (but close enough to be considered to be the same source), may have different values for the CIRRUS\_N and SKY\_BRIGHTNESS flags in each channel.

The EXT\_VAL column summarizes the cross-identification with external catalogues. Its definition has been modified slightly with respect to the PCCS. The EXT\_VAL flag now has a value of 0, 1, 2, or 3 as described below:

- 0: The source has no clear counterpart in any of the external catalogues and it has not been detected in a neighbouring *Planck* channel.
- 1: The source has no clear counterpart in any of the external catalogues, has not been detected in a neighbouring *Planck* channel, but was detected in the same channel in the PCCS.
- 2: The source has no clear counterpart in any of the external catalogues, but it has been detected in a neighbouring *Planck* channel in this release. For the HFI channels, we consider the catalogues extracted from the IRIS maps as a neighbouring *Planck* channel, given the common detection algorithm applied to both data sets.
- 3: The source has a clear counterpart in one of the radio catalogues (CRATES, Healey et al. 2007; NEWPS, López-Caniago et al. 2007; AT20G, Murphy et al. 2010), the Revised IRAS-FSC Redshift Catalogue (RIFSC; Wang et al. 2014), or the submillimetre catalogue of H-ATLAS (Eales et al. 2010).

This flag provides extra information about the reliability of individual sources: those flagged as EXT\_VAL = 3 are already known; those with EXT\_VAL = 2 (or 1) have been detected in other *Planck* channels (or maps) and are therefore potentially new sources, and those with EXT\_VAL = 0 appear in only a single channel and only in this release, and hence are more likely to be spurious.

The EXT\_VAL flag requires data from the neighbouring channels for its evaluation. It is, however, evaluated per frequency channel. If, for instance, a source is identified with an external catalogue and a source in a neighbouring channel, the source in the neighbouring channel will only be identified with the external catalogue if it also satisfies the identification criteria with the external catalogue.

It should be noted that there is no column that contains the coordinate uncertainties for each source. The errors in position are purely statistical and may be determined for each source using Eq. (7) with the parameters given in Table 8. There is also no column that contains the S/N of the detection, since this is given by DETFLUX/DETFLUX\_ERR.

### 5.1. Maps associated with the catalogues

Along with the source catalogues we provide associated maps for the HFI channels. There are three types of maps provided, which are shown in Fig. 8. These are a zone mask, a noise level map, and a S/N threshold map.

The zone map shows the areas of the sky covered by the PCCS2 and PCCS2E catalogues. The zone map takes the value of zero in the areas corresponding to the PCCS2 and is non-zero in areas corresponding to the PCCS2E. It is related to the WHICH\_ZONE flag, in that a non-zero value encodes the reason why sources in that patch of sky are placed in the PCCS2E. The value 1 corresponds to the filament mask outside of the Galactic region; 2 corresponds to the Galactic region; and 3 corresponds to the filament mask inside the Galactic region.

The noise level map corresponds to the detection noise for compact sources. This is not the same as the instrumental noise, because it includes “noise” from all signals other than compact sources.

<sup>7</sup> <http://wiki.cosmos.esa.int/planckpla2015>

The S/N threshold map contains the thresholds required at each location on the sky to produce a catalogue of the stated reliability. Threshold maps for the 80%, 85%, 90%, and 95% reliability catalogues are provided. The S/N threshold for the 80% reliability map contains the S/N cut applied to the PCCS2E in the area of the sky where the zone map is non-zero. The S/N threshold maps for higher reliabilities contain null values in this region.

In total there are, for each HFI channel, six associated maps: one zone map, one noise level map, and four S/N threshold maps. As described in Sect. 3.1.2, the completeness of the PCCS2 and PCCS2E may be evaluated using these maps. By providing the S/N threshold maps for the higher reliabilities the completenesses for the higher reliability subsets of the PCCS2 may also be evaluated. Indeed the completeness for a given reliability and region of the sky may be assessed using these data.

## 5.2. Cautionary notes on the use of catalogues

The PCCS2 supersedes previous *Planck* compact source catalogues (ERCSC and PCCS), because it has been produced using the full mission data and the latest processing and calibration pipelines. Since the three sets of catalogues have been produced from the analysis of maps that average different amounts of data, some idea of the variability of the sources could be obtained from the comparison of the three, although for this purpose it would be better to analyse the single survey maps, the time-ordered data or the user specified time interval maps that can be obtained from the *Planck* Legacy Archive.

As noted earlier, the aim of the PCCS2 is to provide as complete a list as possible of *Planck* sources with a reasonable, and user-adjustable degree of reliability. The criteria used to include or exclude candidate sources differ from channel to channel and in different parts of the sky; they also are based on different S/N levels between channels and as a function of position on the sky. These differences are consequences of our desire to make the catalogue as complete as possible, yet maintain >80% reliability; the differences have to be taken into account when using the PCCS2 for statistical studies.

We now turn to several specific cautions and comments for users of the PCCS2 and PCCS2E.

**Bandpass corrections to polarization:** for many sources in the three lowest *Planck* frequency channels, the bandpass correction of the  $Q$  and  $U$  flux densities is not negligible. Even though we have attempted to correct for this effect on a source by source basis and have propagated this uncertainty into the error bars on the polarized flux densities and polarization angles, there is still room for improvement. This can be seen in the residual leakage present at the position of Tau A in the Stokes  $U$  maps. It is anticipated that there will be future updates to the LFI catalogues once the bandpass corrections and errors have been improved.

**Variability:** at radio frequencies, up to and including 217 GHz, many of the extragalactic sources are variable. The measurements of their flux densities provided in the catalogues are, however, averages over the full *Planck* mission. It should be noted therefore that follow-up observations of these sources may show significant differences from those provided.

**Contamination from CO:** at infrared/submillimetre frequencies (100 GHz and above), the *Planck* bandpasses straddle energetically significant CO lines. The effect is the most significant at

100 GHz, where the line might contribute more than 50% of the measured flux density for some Galactic sources.

**Photometry:** each source has multiple estimates of flux density: DETFLUX, APERFLUX, GAUFLUX, and PSFFLUX, as defined above. The evaluation of APERFLUX makes the smallest number of assumptions about the data and hence is the most robust, especially in regions of high non-Gaussian background emission, but it may have larger uncertainties than the other methods. Hence, a general recommendation for which estimate to use for unresolved sources would be DETFLUX for 30 to 217 GHz and APERFLUX for 353 to 857 GHz. Note that for a specific source the nature of the local background will influence the best choice for the flux estimator. For bright *resolved* sources, GAUFLUX is recommended, taking into account that it may not be robust for sources close to the Galactic plane due to the strong backgrounds. In the PCCS2 and PCCS2E we provide polarized flux densities for two methods, one obtained from the measured flux densities in the filtered maps of  $Q$  and  $U$  and the other obtained from the measured flux densities on the unfiltered maps of  $Q$  and  $U$  using aperture photometry. Both methods agree for the brightest sources but, because the noise level is higher in the unfiltered maps, for weaker sources the polarized flux densities obtained with the filtering method are more robust. In addition, we have found that at the position of very bright sources in polarization one can see a spurious signal introduced by the complex beams in polarization. This spurious signal is small compared with the flux density of the sources, but in cases like Tau A, where most of the signal is in the  $Q$  map, this signal can have an impact on the flux density measured in the  $U$  map, which is particularly important when calculating the polarization position angle. For this reason position angles should be used with caution.

**Calibration:** the absolute calibration uncertainties of *Planck* are well below 1% for 30–353 GHz (Planck Collaboration V 2016; Planck Collaboration VIII 2016), while for 545 and 857 GHz the absolute calibration uncertainty is <7%, which is primarily due to a 5% systematic uncertainty arising from the planet models (Planck Collaboration VIII 2016). This systematic uncertainty is not included in the internal validation (not simulated) or in the comparison with *Herschel* data (which use the same planet models; Griffin et al. 2010). In addition, there is a 0°5 and 0°3 systematic uncertainty in the polarization position angles in the LFI and HFI, respectively.

**Colour-correction:** the flux-density estimates have not been colour-corrected because this implies fixing the spectral index that describes each source, and the user may want to apply a colour-correction based on a specific spectral index determined with a higher-resolution experiment. In the *Planck* Legacy Archive there is a tool to apply the colour-correction to the source flux density for a user supplied spectral index. Colour-corrections are described in Planck Collaboration II (2016) and Planck Collaboration VII (2016). Note that the term bandpass correction in this paper refers to the correction required due to the mismatch in the bandpass between orthogonally polarized detectors and not to the colour-correction of the flux density in Stokes  $I$ .

**Cirrus/ISM:** the upper bands of HFI could be contaminated by apparent sources associated with Galactic interstellar medium

features (ISM) or cirrus. The values of the parameters CIRRUS\_N and SKY\_BRIGHTNESS can be used as indicators of contamination. CIRRUS\_N can be used to flag sources that might be clustered together and thereby associated with ISM structure. In order to provide some indications of the range of values of these parameters that could indicate contamination, we compared the properties of the IRAS-identified and non-IRAS-identified sources for both the PCCS2 and the PCCS2E, outside the Galactic plane. At Galactic latitudes  $|b| > 20^\circ$ , we can use the RIFSCz (Wang et al. 2014) to provide a guide to the likely nature of sources.

We compare the PCCS2 857 GHz catalogue and the PCCS2E 857 GHz catalogue with the IRAS sources in the RIFSCz using a 3 arcmin matching radius. Of the 4891 sources in the PCCS2 857 GHz catalogue, 3094 have plausible IRAS counterparts, while 1797 do not. Examination of histograms of the CIRRUS\_N and SKY\_BRIGHTNESS parameters in the PCCS2 show that these two classes of objects behave rather differently. The IRAS-identified sources have a peak sky brightness at about  $1 \text{ MJy sr}^{-1}$ . The non-IRAS-identified sources have a bimodal distribution with a slight peak at  $1 \text{ MJy sr}^{-1}$  and a second peak at about  $2.6 \text{ MJy sr}^{-1}$ . Both distributions have a long tail, but the non-IRAS-identified tail is much longer. On this basis, sources with  $\text{SKY\_BRIGHTNESS} > 4 \text{ MJy sr}^{-1}$  should be treated with caution. In contrast non-IRAS-identified sources with  $\text{SKY\_BRIGHTNESS} < 1.4 \text{ MJy sr}^{-1}$  are likely to be reliable. Examination of their sky distribution, for example, shows that many such sources lie in the IRAS coverage gaps. The CIRRUS\_N flag tells a similar story. Both IRAS-identified and IRAS non-identified sources have a peak CIRRUS\_N value of 2, but the non-identified sources have a far longer tail. Very few IRAS-identified sources have a value  $> 8$  but many unidentified sources do. These should be treated with caution.

The PCCS2E 857 GHz catalogue contains many more sources with  $|b| > 20^\circ$  of which 1235 are identified with IRAS sources in the RIFSCz and 9235 are not. As with the PCCS2 catalogue the distributions of CIRRUS\_N and SKY\_BRIGHTNESS are different, where the differences are even more pronounced for these PCCS2E sources. Once again, few IRAS-identified sources have  $\text{SKY\_BRIGHTNESS} > 4 \text{ MJy sr}^{-1}$ , but the unidentified sources have brightnesses extending to  $> 55 \text{ MJy sr}^{-1}$ . Similarly, hardly any of the IRAS-identified sources have  $\text{CIRRUS\_N} > 8$ , but nearly half the unmatched sources do. Of the 9235 PCCS2E 857 GHz sources that are not identified with an IRAS source and that lie in the region  $|b| > 20^\circ$ , 1850 (20%) have WHICH\_ZONE = 1, 2637 (29%) have WHICH\_ZONE = 2, and 4748 (51%) have WHICH\_ZONE = 3. The PCCS2E covers 30.36% of the region  $|b| > 20^\circ$ , where 2.47% is in the filament mask, 23.15% in the Galactic region and 4.74% in both. If the 9235 unidentified detections were distributed uniformly over the region  $|b| > 20^\circ$ , we can predict the number of unidentified sources in each zone and compare this to the values we have. We find that there are 2.5 and 3.3 times more sources than expected in zones 1 and 3, showing that the filament mask is indeed a useful criterion for regarding sources detected within it as suspicious.

It should be noted that the EXTENDED flag could also be used to identify ISM features, but nearby Galactic and extragalactic sources that are extended at *Planck* spatial resolution will also meet this criterion.

## 6. Conclusions

The Second *Planck* Catalogue of Compact Sources has been produced using the *Planck* full mission data. The catalogue lists sources detected in total intensity in each of its nine frequency bands between 30 and 857 GHz and polarization measurements at the positions of these sources for seven of the frequencies between 30 and 353 GHz. Its format has changed with respect to the ERCSC and the PCCS. We have divided the catalogue into two parts, the PCCS2 and PCCS2E, based on our ability to provide a measure of the reliability of each source detected at 100 GHz and above, where the available external catalogues of compact sources are not able to fully assess the reliability of the detections. Sources located inside the defined Galactic plane masks or situated along dusty filamentary structures (as defined in the cirrus masks) are in the PCCS2E because the uncertainties in the number counts of the Galactic sources and the difficulty of simulating the diffuse dust emission near the beam scale in the higher frequency channels do not allow us to achieve the necessary consistency between the catalogues of input and detected sources in our reliability assessments.

Given the increase in the volume of data between the nominal mission and the full mission, and the improvements in the data processing and calibration of the frequency channel maps, the PCCS2 supersedes previous *Planck* catalogues. The new catalogue is more complete than the PCCS, in particular for the LFI channels, owing to the large increase in the data available, eight sky surveys compared with the two and a half sky surveys of PCCS. In addition, improvements have been made in some of the techniques used to perform the photometry analysis, and in the reliability assessment of the catalogues. The completeness of the 857 GHz channel, however, has not improved because improvements in the reliability assessment resulted in a higher S/N threshold being applied in the formation of this catalogue. It should be noted, however, that the quality of the PCCS2 catalogue at this channel is better than that of the earlier PCCS due to its greater reliability.

The division of the HFI catalogues into the PCCS2 and PCCS2E has permitted the addition of a parameter in the PCCS2 catalogue that will allow a user to define subsets of the catalogue with higher reliability levels than the target integral reliability of 80%. Associated maps are provided that will allow the user to evaluate the completeness of their chosen reliability subset, or indeed of the catalogue as a whole. This added functionality gives the users of the PCCS2 the option of extracting high-reliability subcatalogues, and, in addition, provides a much more complete full catalogue, allowing studies of more sources and to fainter flux densities. There are ongoing efforts in the *Planck* Collaboration to produce multifrequency catalogues that will complement the PCCS2; when completed, they will be available in the *Planck* Legacy Archive.

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- 67 Institut Universitaire de France, 103 Bd Saint-Michel, 75005 Paris, France
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- 74 Instituto de Astrofísica de Canarias, C/Vía Láctea s/n, La Laguna, Tenerife, Spain
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- 76 Istituto Nazionale di Fisica Nucleare, Sezione di Padova, via Marzolo 8, 35131 Padova, Italy
- 77 Jet Propulsion Laboratory, California Institute of Technology, 4800 Oak Grove Drive, Pasadena, California, USA
- 78 Jodrell Bank Centre for Astrophysics, Alan Turing Building, School of Physics and Astronomy, The University of Manchester, Oxford Road, Manchester, M13 9PL, UK
- 79 Kavli Institute for Cosmological Physics, University of Chicago, Chicago, IL 60637, USA
- 80 Kavli Institute for Cosmology Cambridge, Madingley Road, Cambridge, CB3 0HA, UK
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- 82 LAL, Université Paris-Sud, CNRS/IN2P3, 91405 Orsay, France
- 83 LERMA, CNRS, Observatoire de Paris, 61 Avenue de l’Observatoire, 75000 Paris, France
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## Appendix A: PSF photometry

The flux density is obtained by fitting a model of the PSF at the position of the source. The model has four free parameters: the amplitude of the source, a background offset, and two coordinates for the location of the source. The PSF is obtained from the effective beam (Planck Collaboration II 2014; Planck Collaboration VI 2014). The model of the source is

$$\mathbf{m} = \mathbf{A}\mathbf{P} + C, \quad (\text{A.1})$$

where  $\mathbf{P}$  is the PSF at the position of the source (the integrated response to a point-like source),  $A$  is the amplitude of the source, and  $C$  is the (constant) background. The PSF at the position of the source is obtained from the effective beam, which is defined only at the centre of each map pixel, by means of a bicubic interpolation between adjacent pixels. This step is new: in the previous version of the PCCS, the PSF was built from the effective beam at the centre of the pixel associated with the location of the source. The PSF model  $\mathbf{P}$  depends therefore on the position of the source,  $\mathbf{P} = \mathbf{P}(x_s, y_s)$ .

The best-fit values of the parameters  $\beta = (A, C, x_s, y_s)$  are found by minimizing the  $\chi^2$  between the model and the data,  $\mathbf{d}$ ,

$$\chi^2(\beta) = \sum (\mathbf{d} - \mathbf{m})^T \mathbf{N}^{-1} (\mathbf{d} - \mathbf{m}), \quad (\text{A.2})$$

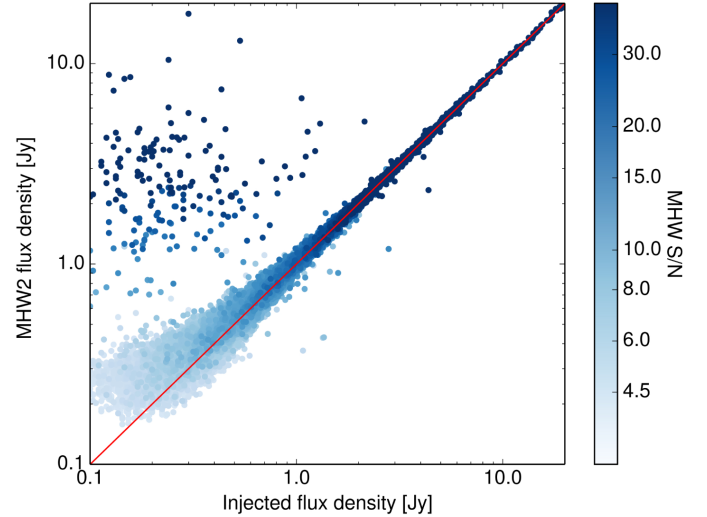
where  $\mathbf{N}$  is the covariance matrix of the noise. The noise is assumed to be uncorrelated between pixels. The overall normalization of the noise is adjusted by setting  $\chi^2 = 1$  at the best-fit value of the parameters. We also include the uncertainty of the background flux in the error of the flux density estimation. This has the effect of inflating the uncertainties to account for any mismatch between the modelled PSF and the true shape of the source and the background in the map. The uncertainties on the parameters are computed from the curvature of the  $\chi^2$ . The best-fit amplitude and its uncertainty are converted to units of flux density using the area of the PSF and the unit conversion from  $\text{K}_{\text{CMB}}$  to  $\text{MJy sr}^{-1}$  for each *Planck* channel.

## Appendix B: Gaussian fitting method

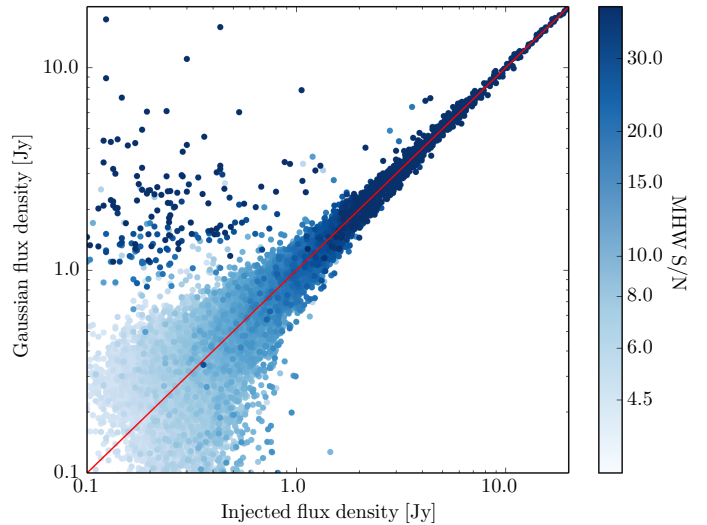
To recover the shape of the source and its orientation, and to improve on the MHW2 flux-density estimate, Gaussian fitting is used. Taking point source parameters from the MHW2 catalogue as input, a 2D Gaussian fit is performed at the location of each catalogue source. Six parameters are fitted: Galactic coordinates of the source ( $l, b$ ); the flux density; the major and minor semi-axes; and an orientation angle. The source semi-axes and orientation angle are used to flag elongated sources.

### B.1. Downhill simplex in multidimensions

The downhill simplex method in multidimensions, i.e. the Nelder–Mead or “amoeba” method (Press et al. 1992), which is useful for problems where the derivatives are not known, is used for optimization in multiparameter space. The functional to optimize is based on the reduced log-likelihood with some prior regularization for the size of the source defined by the effective beam at the given frequency. The algorithm starts optimization at the MHW2 source location, assuming initially a circular Gaussian source with the FWHM of the PSF. Optimization of all six parameters converges in a reasonable number of iterations, usually less than 1000.



**Fig. B.1.** Comparison of injected and recovered MHW2 flux densities for point sources at 100 GHz. The saturation of points is proportional to the S/N of the MHW2 detection. The outliers towards the upper left are associated with faint sources with injected flux densities  $< 1$  Jy located in areas with complicated backgrounds close to the Galactic plane. It is known that in these regions the MHW2 algorithm may give biased flux-density estimates.

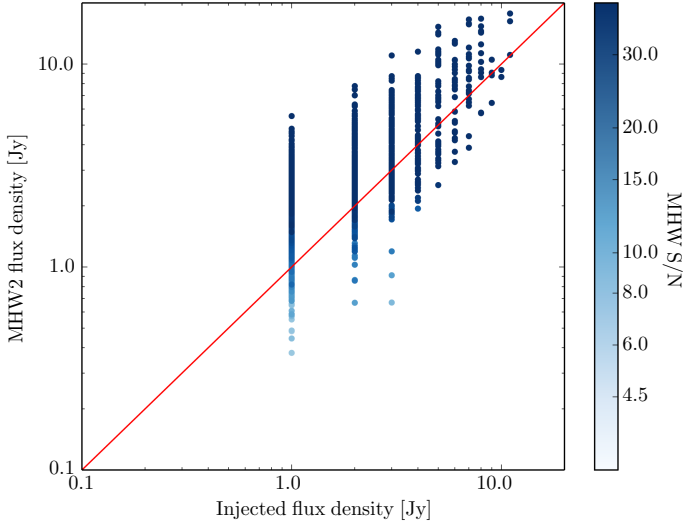


**Fig. B.2.** Comparison of injected and recovered Gaussian flux densities for point sources at 100 GHz. The saturation of points is proportional to the S/N of the MHW2 detection. Gaussian fitting improves the outlier flux densities slightly, but the flux-density estimates are still biased.

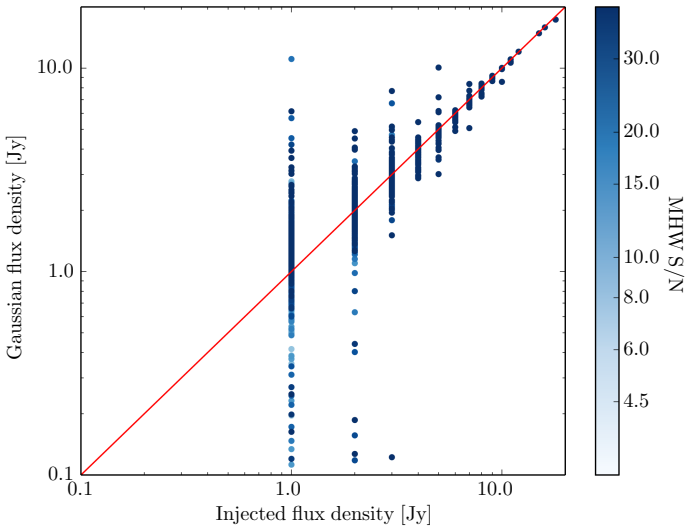
### B.2. Error estimation

The downhill simplex method does not provide any information on the uncertainties in the optimized parameters. We estimate errors using a Markov Chain Monte Carlo (MCMC) method to sample the posterior distribution. In our case, the burn-in time can be very small since to start the chain the simplex-optimized value of the parameter from the previous step can be used, and it is usually very close to the peak of the distribution. The length of the MCMC chain is set to 1000 samples by default.

To obtain the proper sampling in the MCMC chain it is necessary to define the optimal step size in the parameter space. This determination is complex since there are more than 100 000 sources in the catalogue to process; it would be



**Fig. B.3.** Comparison of injected and recovered MHW2 flux densities for cold cores at 100 GHz. The saturation of points is proportional to the S/N of the MHW2 detection. The visible digitization is because only integer values were used for the flux densities of injected sources.



**Fig. B.4.** Comparison of injected and recovered Gaussian flux densities for cold cores at 100 GHz. The saturation of points is proportional to the S/N of the MHW2 detection. The visible digitization is because only integer values were used for the flux densities of injected sources.

impossible to adjust every MCMC chain, since it would take an excessive amount of time to try several values of the sampling step using an iterative approach. Hence we decided to use an analytical approximation for the errors of most of the Gaussian profile parameters, following Hagen & Dereniak (2008). We used an analytical approximation for the separable 2D Gaussian profile model; the errors are derived for five parameters; namely position coordinates, flux density, and two non-equal width values. The calculated errors were used to find the value of the step size in the parameter space to start the MCMC sampler, which delivered the error on the tilt angle. This combined technique allowed us to avoid most of the problems related to undersampled or oversampled MCMC chains.

### B.3. Validation of the method using model data

The results of the Gaussian fit were compared with the MHW2 positions and flux densities for a test set of sources with known parameters. The PR2 100 GHz map with injected sources and cold cores was used to check the 2D Gaussian fitting algorithm. The cold cores were modelled as 2D Gaussian profiles with uniformly distributed random orientation angles. The major FWHM was in the range from 4.5 to 19', and the ellipticity parameter,  $e = FWHM_{\text{major}}/FWHM_{\text{minor}}$ , varied from 1 (circular source) to 7 (highly elliptical source). All sources were uniformly distributed across the sky.

Plots comparing the flux density values for MHW2 and Gaussian fitting for this test set are shown in Figs. B.1–B.4. Both methods give almost the same point source flux-density values (Figs. B.1 and B.2), but MHW2 gives less scatter for the fainter point sources. For the cold cores, Gaussian fitting works better and gives much less bias, especially for the bright sources (Figs. B.3 and B.4). The visible digitization of the flux densities reflects the fact that only integer values were used for the flux densities of injected sources.

The group of outliers in the upper left part of Figs. B.1 and B.2 correspond to faint point sources (<1 Jy) in regions with complicated backgrounds, near the Galactic plane. Both MHW2 and Gaussian fitting fail to recover their flux densities accurately and give biased estimates.

It is clear that Gaussian fitting is preferable for extended objects like cold cores, giving more accurate flux densities as well as recovering the actual source shape and orientation.

## Appendix C: Bandpass mismatch and polarization measures

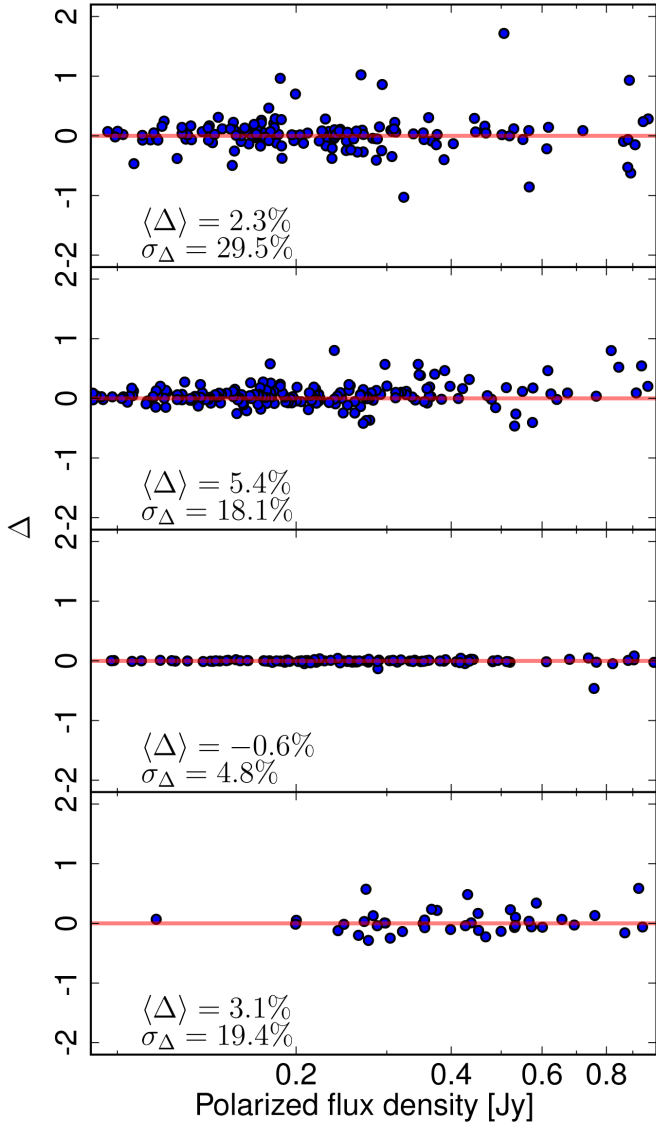
For sources with spectra differing from the CMB spectrum, bandpass mismatch causes leakage of temperature to polarization (see Sect. 2.5.1). To correct for this leakage, we require a model of the source spectrum. That requirement was handled differently by LFI and HFI.

### C.1. LFI-specific details

In the case of LFI maps corrected for bandpass-mismatch leakage, the spectral model is based on the diffuse component separation analysis (Planck Collaboration II 2016). These models are not particularly accurate for compact sources; moreover, the analysis is done at a common resolution of 1° FWHM, whereas for compact sources it is best to work at full resolution. Therefore the PCCS2 polarization measurements were evaluated by extracting the  $Q$  and  $U$  flux densities from the full-resolution uncorrected maps, and correcting for leakage at the flux density level, using

$$\begin{pmatrix} Q \\ U \end{pmatrix}_{\text{corrected}} = \begin{pmatrix} Q \\ U \end{pmatrix}_{\text{raw}} - \begin{pmatrix} P_Q \\ P_U \end{pmatrix} (\alpha - \alpha_{\text{CMB}}) I, \quad (\text{C.1})$$

where  $I$  is the total intensity,  $\alpha = \text{dln } I/\text{dln } \nu$  is the source spectral index in the relevant frequency band, and  $\alpha_{\text{CMB}}$  is the spectral index of the CMB fluctuations (1.96, 1.90, and 1.75, at 28.4, 44.1, and 70.4 GHz, respectively).  $P_{Q,U}$  is the projection factor derived in Planck Collaboration II (2016), which is evaluated at each map pixel. For the point-source correction we averaged the projection factors over the source pixels using the same weights as were used to extract the  $Q$  and  $U$  fluxes.



**Fig. C.1.** Comparison of polarized flux densities from FFP8 simulations with ( $S_{\text{bpm}}$ ) and without ( $S_{\text{nobpm}}$ ) bandpass mismatch leakage. The difference between the polarized flux densities normalized by the uncertainty on the polarized flux density,  $\Delta = (S_{\text{bpm}} - S_{\text{nobpm}})/\sigma$ , is plotted against the input polarized flux density. The errors in the polarized flux density due to leakage are always subdominant with respect to the uncertainties due to the noise.

### C.1.1. Evaluation of LFI polarization measurements

The polarized flux density  $P$  is calculated using Eq. (1), where the  $\hat{Q}$  and  $\hat{U}$  maps are obtained by applying the “filtered fusion” maximum-likelihood estimator (Argüeso et al. 2009; López-Caniego et al. 2009) to the original Stokes  $Q$  and  $U$  maps. The errors in  $P$  are calculated using Eq. (4), adding in quadrature the error estimate obtained from the Monte Carlo simulations and calculating the  $1\sigma$  asymmetric errors for a Rayleigh distribution in the intervals  $[0, 0.159]$  and  $[0.841, 1]$ . The errors in the polarization angle,  $\psi$ , are calculated using Eq. (5).

### C.2. HFI-specific details

Data from a number of bolometers are combined to make the HFI polarized frequency maps. Mismatch between the

bandpasses of the bolometers causes leakage from intensity to polarization for any source of emission which has a non-CMB spectrum. Small uncertainties in the measured transmission for each bolometer may lead to large uncertainties in the estimates of the bandpass mismatch leakage (Planck Collaboration VIII 2016), so it is difficult to make an accurate prediction of the leakage for compact sources. Instead we use the FFP8 simulations (Planck Collaboration XII 2016) to assess the effect of the leakage.

Two sets of FFP8 maps have been generated. One set was simulated with the measured bandpasses for each HFI bolometer, so it contains the bandpass mismatch leakage. The other set was generated using the average frequency channel bandpass for all bolometers in a channel. In this idealized case, there is no mismatch between the bandpasses, so no leakage is produced. We compare the polarized flux densities of sources from the two sets of maps. A suitable quantity for assessing the size of the leakage is the difference between the polarized flux density from the maps with the leakage,  $S_{\text{bpm}}$ , and that from the maps without the leakage,  $S_{\text{nobpm}}$ , normalized by the uncertainty due to the noise,  $\sigma$ ,

$$\Delta = \frac{(S_{\text{bpm}} - S_{\text{nobpm}})}{\sigma}. \quad (\text{C.2})$$

Figure C.1 shows this quantity plotted against the input polarized flux density of the source for the 100–353 GHz channels. The size of the effect depends on the differences between the individual bolometer bandpasses and the average frequency channel bandpass; they are smallest for the 217 GHz channel. For all channels the effect of the leakage is smaller than  $1\sigma$  for most sources. The mean value of  $\Delta$  gives the average bias on the polarized flux density measurements. It is smaller than  $0.06\sigma$  for all four channels. Therefore we conclude that the effect is small and can be safely ignored.

#### C.2.1. Evaluation of HFI polarization measurements

We use the  $Q$  and  $U$  maps that have been corrected for the leakage of the diffuse temperature components into polarization. This does not correct for any leakage from temperature due to the compact sources themselves. However, as shown above, this effect is subdominant when compared with the statistical uncertainty of the measurements.

The polarized flux density estimator,  $\hat{P}$ , is evaluated using Eq. (1) and the maximum-likelihood estimates,  $\hat{Q}$  and  $\hat{U}$ , are extracted from the corresponding  $Q$  and  $U$  maps by fixing the position to that found from the intensity map and strictly assuming that the source is point-like. This selection of the estimator is justified, because maximum-likelihood estimators produce minimum variance and unbiased estimates, which follow a Gaussian distribution with a variance given by

$$\frac{1}{\sigma^2} = \sum_{\eta} \tilde{\psi}^T(\eta) \mathcal{N}^{-1}(\eta) \psi(\eta), \quad (\text{C.3})$$

where  $\mathcal{N}^{-1}$  is the inverse power-spectrum of the background of the patch-map, and  $\psi(\eta)$  is the beam transfer function as function of the bidimensional spatial frequency vector,  $\eta$ . The maximum-likelihood estimator employed for the extraction of the  $Q$  and  $U$  signals was PowellSnakes (PwS; Carvalho et al. 2012, 2009). The PwS likelihood assumes the background is a realization of a homogeneous Gaussian random field, where a power-spectrum is known, which is a good assumption for small, flat patches cut from the  $Q$  and  $U$  maps.

The PwS package has been extensively tested and used inside the Planck Collaboration and is known to deliver robust and accurate estimates (Planck Collaboration VII 2011; Planck Collaboration VIII 2011; Planck Collaboration XXIX 2014). The flux densities in the  $Q$  and  $U$  maps can be either positive or negative. In order to reduce systematic effects, which could be induced by the ancillary steps of the likelihood evaluation (such as the estimation of the background power-spectrum of the patch-map), we perform the same estimation procedure on both the patch-map and its negative, and the average of the two flux-density estimates is taken. This procedure helps in stabilizing the polarization signal, especially when tackling regions with complex backgrounds. Equivalent estimates of  $\hat{Q}$  and  $\hat{U}$ , and their uncertainties, can be obtained using an aperture-photometry estimator. The aperture-photometry estimator is robust to deviations from the likelihood data model – e.g. extended sources, background deviations from Gaussianity, or variations in the beam shape – at the cost of slightly larger error bars. For both estimators the criterion for the acceptance of a putative detection was that  $\hat{P}$  had to be 99.99% significant with regard to the null-hypothesis, which is well described by a Rayleigh distribution when the assumption is made that  $\sigma_Q \approx \sigma_U$ , and that these errors are uncorrelated. In the case of acceptance, the polarization angle estimate,  $\hat{\psi}$ , is evaluated using Eq. (2). The  $\hat{Q}$  and  $\hat{U}$  uncertainties are propagated onto the  $\hat{P}$  and  $\hat{\psi}$  estimates. This is done by assuming the uncertainties are normally distributed and the error bars are small compared with the measured quantities. This approximation holds very well given the high significance threshold we have chosen. In the case where a putative detection is rejected because it does not reach the required significance, we provide the 99% upper limit.

### C.3. Methods to determine polarization properties of marginal detections

For the four polarization-sensitive HFI channels, we provide another set of polarized flux-density and polarization angle estimates for sources with marginal detections of polarization. The extraction of the polarization signal from the  $Q$  and  $U$  maps follows the same procedure described above and in Sect. 2.1. We then proceed by assessing the probability of obtaining a given measurement of polarization, given a true value of polarization  $P$ .

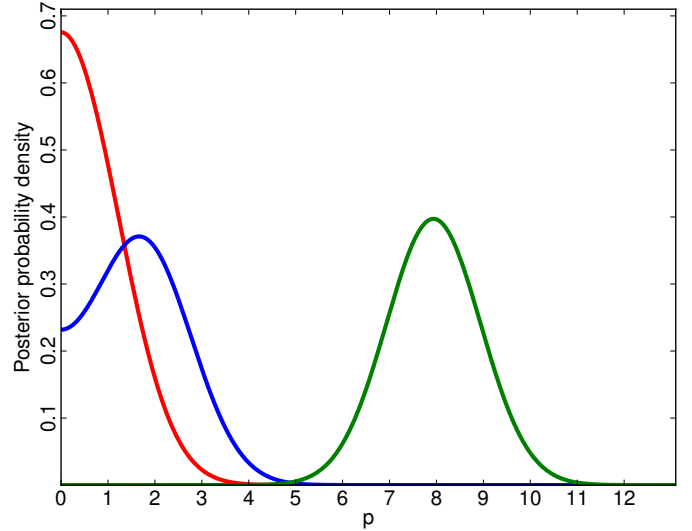
Assuming  $\sigma_Q \approx \sigma_U \approx \sigma$ , the probability of drawing  $p = \sqrt{q^2 + u^2}/\sigma$  given the true value of the polarized flux density  $p_0 = P_0/\sigma$ , is

$$\mathcal{L}(p | \sigma) \equiv \Pr(p | p_0, \sigma) = p \exp\left(-\frac{p^2 + p_0^2}{2}\right) \mathcal{I}_0(pp_0), \quad (\text{C.4})$$

where  $\mathcal{I}_0(x)$  is the zero-order modified Bessel function of the first kind (Herranz et al. 2012). Using Bayes' theorem, the posterior distribution of  $p_0$  (the true polarized flux density) given the measurement  $p$  is

$$\Pr(p_0 | p) \propto \exp\left(-\frac{p^2 + p_0^2}{2}\right) \mathcal{I}_0(pp_0) \Phi(p_0), \quad (\text{C.5})$$

where  $\Phi(p_0)$  is the Heaviside step function. We have used the Heaviside step function as a prior, since the flux-density parameter is intrinsically positive, and by taking the asymptotic form of  $\mathcal{I}_0(pp_0)$  it may be shown that  $p_0$  acts as a location parameter for large  $p$ . Examples of three different posterior distributions for the polarized flux density are shown in Fig. C.2.



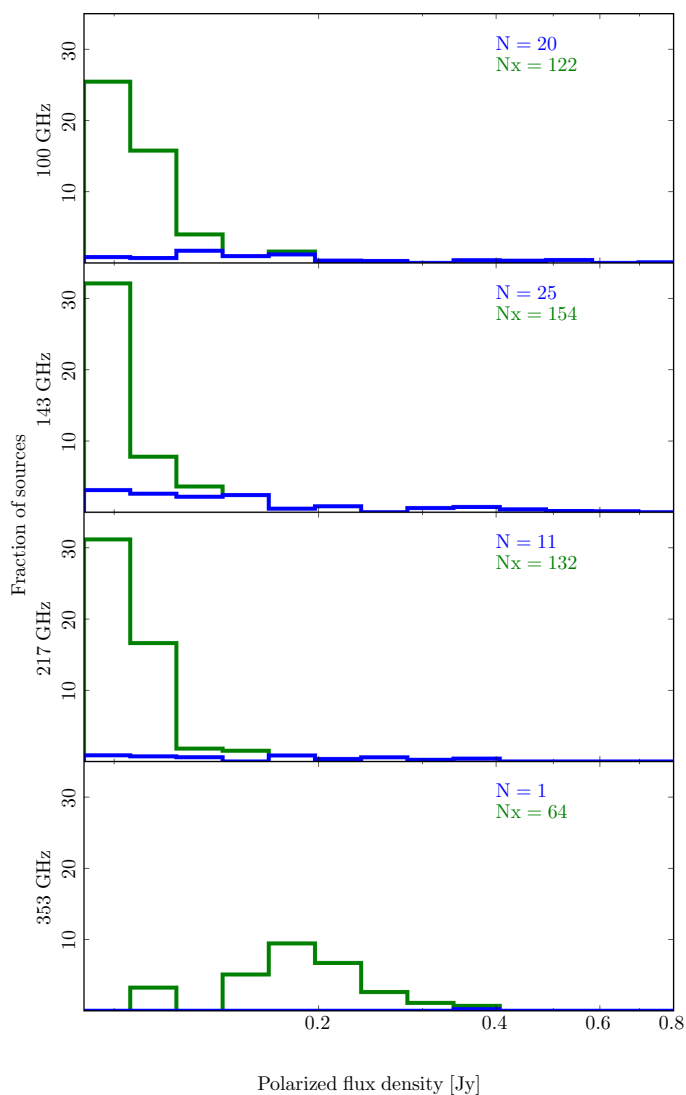
**Fig. C.2.** Three different cases of polarized flux density posterior distributions (Eq. (C.5)). The red curve shows a non-detection ( $p \lesssim 1.21$ ), the blue curve shows a marginal detection ( $1.21 \lesssim p \lesssim 3.0$ ), and the green curve shows a significant detection ( $p \gtrsim 3.0$ ).

The polarization angle distribution was derived using Eq. (2). It has been assumed that  $U$  and  $Q$  are independent Gaussian-distributed random variables with means  $\mu_U = \hat{u}$ ,  $\mu_Q = \hat{q}$ , where  $\hat{u}$ ,  $\hat{q}$  are maximum-likelihood estimates of  $U$  and  $Q$ , and  $\sigma_U$  and  $\sigma_Q$  are given by Eq. (C.3). Then using the equality for changing variables in a probability distribution  $\Pr(\theta) d\theta = \Pr(\zeta) d\zeta$ , where  $\zeta = U/Q$ , the probability distribution for  $\theta$  is

$$\Pr(\theta) = -2 \cos(2\theta)^{-2} f(-\tan(2\theta)), \quad (\text{C.6})$$

where  $f(w)$  is a function defined in Hinkley (1969, Eq. (1)). The best-fit value is the mode of the distribution and the asymmetric error-bars were computed using the 95% highest probability density (HPD) region of the posterior distribution. HPDs are discussed by Box & Tiao (1992) as a general method for compressing the information contained within a probability distribution. Each HPD is uniquely defined by the amount of probability it encloses and is constructed such that there exists no probability density value outside the HPD that is greater than any value contained within it. In other words the 95% HPD contains 95% of the total probability under the posterior distribution, such that there is no point outside of this area with a higher probability than any point inside the area. This approach allows us to provide a best-fit value and the asymmetric  $2\sigma$  error-bars for the marginal polarization entries in the catalogue.

We shall refer to this set of measurements as the Powell-Snakes marginal polarization (PwSPOL) data set. PwSPOL permits a proper statistical characterization of fainter polarization signals and is therefore able to provide a deeper and more complete catalogue without any loss of reliability, as is shown in Sect. 3.5. An additional benefit of PwSPOL is that it provides a qualitative assessment about an even fainter population of polarized sources which could be valuable as targets for follow-up observations. It does this by splitting the non-detections into two separate groups: clear non-detections, where the polarized flux density posterior peaks at no-signal, and marginal detections, where the posterior does not peak at no-signal, but this possibility is still inside the 95% HPD region of the posterior distribution. In Fig. C.3 we compare the histograms of the polarized flux-density measurements in the PCCS2 found with each approach. The distribution of polarized flux densities in



**Fig. C.3.** Normalized histograms of the polarized flux density from the PCCS2 catalogues for 100 to 353 GHz. The blue line shows the detections obtained using the common procedure used by both LFI and HFI, whereas the marginal detections, which are produced only for HFI, are shown in green. The number of sources in each group is shown in the top right of each panel.

the 353 GHz channel does not follow the same pattern as the other HFI channels. This is due to the much shallower completeness (see Sect. 3.5) of this channel as compared with the others. Although reliable, the polarized flux-density measurements of this marginal set are expected to be biased high as result of Eddington-type bias and are therefore not suitable for any statistical analysis.