When three traits make a line: evolution of phenotypic plasticity and genetic assimilation through linear reaction norms in stochastic environments

T. ERGON* & R. ERGON†

*Department of Biosciences, Centre for Ecological and Evolutionary Synthesis, University of Oslo, Oslo, Norway
†University College of Southeast Norway, Porsgrunn, Norway

Keywords:
climate effects; constraints; cue perception and reliability; environmental change; genetic covariance/correlation; life history theory; optimality models; uncertainty/imperfect cues; value of information.

Abstract

Genetic assimilation emerges from selection on phenotypic plasticity. Yet, commonly used quantitative genetics models of linear reaction norms considering intercept and slope as traits do not mimic the full process of genetic assimilation. We argue that intercept–slope reaction norm models are insufficient representations of genetic effects on linear reaction norms and that considering reaction norm intercept as a trait is unfortunate because the definition of this trait relates to a specific environmental value (zero) and confounds genetic effects on reaction norm elevation with genetic effects on environmental perception. Instead, we suggest a model with three traits representing genetic effects that, respectively, (i) are independent of the environment, (ii) alter the sensitivity of the phenotype to the environment and (iii) determine how the organism perceives the environment. The model predicts that, given sufficient additive genetic variation in environmental perception, the environmental value at which reaction norms tend to cross will respond rapidly to selection after an abrupt environmental change, and eventually becomes equal to the new mean environment. This readjustment of the zone of canalization becomes completed without changes in genetic correlations, genetic drift or imposing any fitness costs of maintaining plasticity. The asymptotic evolutionary outcome of this three-trait linear reaction norm generally entails a lower degree of phenotypic plasticity than the two-trait model, and maximum expected fitness does not occur at the mean trait values in the population.

Introduction

All natural populations evolve in environments that are to some degree variable. Biologists have long realized that the phenotypic expression of different genotypes may respond differently to the same environmental change and that such phenotypic plasticity may be heritable (DeWitt & Scheiner, 2004; Pigliucci, 2005). Depending on the effect this phenotypic plasticity has on selection (fitness), evolution may thus bring about mechanisms that either buffer the phenotypic expression against environmental variation (i.e. environmental canalization) or modify the responses to some environmental influence in an adaptive manner (Nijhout, 2003). Phenotypic plasticity involves developmental, physiological and/or behavioural phenotypic responses to some component(s) of the environment (DeWitt & Scheiner, 2004; Pigliucci, 2005; Pigliucci et al., 2006). These environmental components, often referred to as environmental ‘cues’ (DeWitt & Scheiner, 2004), are often just correlated with, but not identical to, the environmental variables affecting fitness (e.g. McNamara et al., 2011; Svennungsen et al., 2011; Gienapp et al., 2014). Hence, cues do not provide perfect information about the optimal phenotypic expression, and it is usually...
adaptive to respond more conservatively towards information-poor cues than more informative ones (Yoccoz et al., 1993; Ergon, 2007; McNamara et al., 2011). The phenotypic expression of a particular genotype as a function of an environmental cue is called a reaction norm (Woltereck, 1909; Pigliucci, 2005). There has been considerable interest in evolutionary processes governing reaction norms as this is crucial for our understanding of how populations may respond to environmental change and introduction to novel environments (e.g. Lande, 2009; Reed et al., 2010; McNamara et al., 2011; Gienapp et al., 2014).

Waddington (1953, 1961) originally used the term ‘genetic assimilation’ to describe experimental results where qualitative phenotypes (such as lack of cross-veins in Drosophila wings) that are initially only expressed in response to a particular environmental stimulus (such as heat shock during a particular stage of development) become constitutively produced (i.e., become expressed independently of the environmental stimuli) after continued selection. However, ‘genetic assimilation’ is also used to describe similar phenomena in evolution of the mean of quantitative phenotypes that may remain plastic at equilibrium in a stochastic environment after an environmental change (Pigliucci & Murren, 2003; Lande, 2009). In such cases, the new equilibrium phenotypes will not be independent of the environment unless the reaction norm slope is zero.

We here use the term ‘genetic assimilation’ essentially as in Pigliucci et al. (2006) and Lande (2009) to describe the evolutionary scenarios where, after an abrupt environmental change, there is an initial increase in phenotypic plasticity, after which mean plasticity is reduced and the zone of canalization (i.e., the environment range, or value, where phenotypic variance is at minimum; Dworkin, 2005; Lande, 2009) moves towards the current mean environment (Fig. 1). Although the exact definition of ‘genetic assimilation’ and proposed mechanisms are somewhat contentious (Scharloo, 1991; Pigliucci et al., 2006), there is substantial evidence from both laboratory experiments and field studies that such processes commonly take place (Pigliucci & Murren, 2003; Braendle & Flatt, 2006; Pigliucci et al., 2006). In our treatment, we regard the process of genetic assimilation as complete in a stationary environment when phenotypic variance is minimized in the mean environment (but both mean reaction norm slope and phenotypic variance in the mean environment may remain nonzero). Population-level phenotypic variation in a fluctuating environment depends on both the degree of environmental canalization, or ‘buffering’, of individual plasticity (represented by the genotypic reaction norm slopes; Dworkin, 2005) and the variation among genotypes in the reaction norm elevation around the mean environment. Considering linear reaction norms, phenotypic variance in the population is always minimized in the environment where the correlation between reaction norm slope and the phenotypic expression is zero (i.e. where reaction norms ‘tend to cross’; Lande (2009)).

The final stage of the genetic assimilation process where the zone of canalization moves to the new mean environment is perhaps the least understood; it has been suggested that genetic drift or fitness costs of maintaining plasticity plays a part (West-Eberhard, 2003; Pigliucci et al., 2006; Lande, 2009; Bateson & Gluckman, 2011), and changes in the genetic variances, covariances and genetic architecture of reaction norm components may be involved (Wagner et al., 1997; Steppan et al., 2002; Le Rouzic et al., 2013).

One approach to quantitative genetics analysis of phenotypic plasticity (Via et al., 1995; Rice, 2004) is to consider the intercept and slope of linear reaction norms as two quantitative traits in their own right (de Jong, 1990; Gavrilets & Scheiner, 1993a; de Jong & Gavrilets, 2000; Tufto, 2000; Lande, 2009). More generally, reaction norms have been modelled by considering polynomial coefficients as traits (Gavrilets & Scheiner, 1993b; Scheiner, 1993). In these models, the intercept trait is defined as the value of the plastic phenotype at a reference cue designated as zero by the researcher. Lande (2009) analysed the evolution of such a linear reaction norm, assuming a stochastic environment undergoing a sudden change in both the mean environmental cue and the phenotypic value where fitness is maximum. In his model, the population responded

Fig. 1 Genetic assimilation of a quantitative character. In a stationary fluctuating environment (indicated by red and blue normal distributions), phenotypic variation (indicated by lighter shaded areas) will evolve to be minimized at the mean environmental cue value. Mean reaction norm slope (thick solid lines) will depend on the correlation between the cue (\(U\)) and the phenotypic value that maximize fitness (\(\Theta\)), see Fig. 3 and eqn (1). Five individual reaction norms in each of the environments are indicated with thin coloured lines. After a sudden environmental change (from red to blue or blue to red), mean reaction norm slope will first increase towards the stippled line representing \(E(\Theta|U)\) and then decline as the zone of canalization (the narrowest parts of the shaded areas) moves to the new mean cue value. Figure is adapted from Fig. 2 in Pigliucci et al. (2006) and Fig. 1 in Pigliucci & Murren (2003).
by a rapid increase in mean reaction norm slope (plasticity), followed by a slow increase in reaction norm intercept with a concomitant decrease in plasticity. However, the genetic assimilation was not completed, as the zone of canalization could never move away from the reference cue because the covariance between reaction norm slope and intercept was assumed to remain constant. Lande (2009) argued that further reduction in phenotypic variance would take place (e.g. due to fitness costs of maintaining plasticity), but did not include any such mechanisms in his modelling.

In this study, we argue that the two-trait model is an insufficient representation of genetic effects on linear reaction norms and hence fails to predict critical aspects of the evolution of phenotypic plasticity and genetic assimilation. Instead, we suggest modelling linear reaction norms as being composed of three traits based on the most fundamental ways that gene products may alter linear reaction norms in such a way that they remain linear, specifically distinguishing between genetic effects on reaction norm elevation and genetic effects on cue perception (Fig. 2). Reanalysing the scenarios for extreme environmental change considered by Lande (2009), we show that, under the three-trait reaction norm model, genetic assimilation in the new stochastic environment becomes complete (as defined above) without changes in genetic correlations among the defined traits, genetic drift or imposing any fitness costs on maintaining plasticity. Further, we show that the evolutionary equilibrium of this three-trait linear reaction norm under random mating entails (with certain exceptions) a shallower mean reaction norm slope than the slope of the optimal individual reaction norm and the equilibrium slope of the two-trait model. Hence, maximum individual fitness does not occur at the mean trait values in the population.

We start by deriving an expression for optimal linear reaction norms as a function of environmental cues in stationary stochastic environments. We then derive our three-trait linear reaction norm model, and finally, we analyse the evolutionary dynamics of this model in a quantitative genetics framework and compare it to the dynamics of the two-trait reaction norm model analysed by Lande (2009).

Models

Optimal linear reaction norms in temporally variable environments

Models for optimal adaptations in variable environments have traditionally assumed either that individuals have no information about the relevant environmental variables, or that individuals have exact information about the state of the environment (Yoshimura & Clark, 1991; Roff, 2002). Whenever the phenotype yielding highest fitness is not known exactly (i.e., the individuals do not have full information about the present and future environment), the long-term success of a genotype depends not only on the expectation of fitness, but it is also adaptive to reduce the variance in mean fitness across generations (Yoshimura & Clark, 1991; Starrfelt & Kokko, 2012). Models that assume that individuals have no information about the environment have been used to explain risk-avoidance and bet-hedging strategies (den Boer, 1968; Hopper et al., 2003; Starrfelt & Kokko, 2012). On the other side of the spectrum, models that predict optimal trait values as a function of environmental variables often assume that these variables are known to the individuals without error (e.g. Stearns, 1992; Roff, 2002).

![Fig. 2](image-url) Genetic effects on reaction norms to interval-scaled environmental cues. Genetic effects affecting the organisms cue ‘perception’ will shift the reaction norm along the cue-axis (indicated by blue horizontal arrows and stippled lines), whereas genetic effects that are independent of the cue value will shift the reaction norm along the phenotype-axis (indicated by red vertical arrows and stippled lines). In a linear reaction norm model (panel a), a shift along the cue-axis may have the same effect on the reaction norm as a shift along the phenotype-axis. This is not the case for a nonlinear reaction norm (panel b). The slope of linear reaction norms may also be altered by genetic effects on cue sensitivity (indicated by the stippled black line in panel a).
The concept that phenotypic expressions are functions of more or less informative environmental cues is well established in evolutionary ecology (Tollrian & Harvell, 1999; DeWitt & Scheiner, 2004; Stephens et al., 2007; McNamara et al., 2011; Gienapp et al., 2014). For example, seasonal reproduction in many organisms must take place within a rather narrow time window which often varies largely between years (Durant et al., 2007; Gienapp et al., 2014). As such phenological events must often be prepared a long time in advance (due to acquiring resources, physiological developments and migration), seasonal reproduction may be influenced by rather information-poor cues such as temperature and food constituents weeks before reproductive success is determined (Berger et al., 1987; Lindstrom, 1988; Negus & Berger, 1998; Nussey et al., 2005). Examples of such obviously adaptive phenotypic plasticity to more or less informative environmental cues are ubiquitous in nature (Pigliucci, 2005; Sultan, 2010; Landry & Aubin-Horth, 2014).

To derive an optimal norm of reaction to an imperfect cue, we may view the cue $U$ and the phenotypic expression that maximizes fitness, $\Theta$, as having a joint distribution with given means, $\mu_U$ and $\mu_\Theta$, variances, $\sigma_U^2$ and $\sigma_\Theta^2$, and a correlation, $\rho = \frac{\sigma_{\Theta U}}{\sigma_\Theta \sigma_U}$ (Fig. 3). Note that we here define the cue $(U)$ in a general sense as the environmental component that affects the phenotype, not how this component is perceived by the individuals (as in, e.g., Tufto (2000)). Also note that $U$ must not necessarily be interpreted as a proxy for another environmental component that affects fitness (e.g. Miehls et al., 2013), although this may be the case (see caption of Fig. 3). Hence, following McNamara et al. (2011), we focus on the information content in the cue $(U)$ about the optimal phenotypic expression $(\Theta)$ in the given environment.

Under the assumption of no density or frequency dependence, the optimal phenotypic trait values are those that maximize the geometric mean of fitness across generations (Dempster, 1955; Caswell, 2001). This is equivalent to maximizing the expected logarithm of fitness. Hence, if fitness, $W$, is a Gaussian function (with constant width and peak value) of the phenotype value, $y$, such that $\ln(W(y))$ is a quadratic function, the optimal linear reaction norm as a function of cue value $u$ is

$$y_{opt}(u) = \mu_\Theta + \frac{\sigma_\Theta}{\sigma_U} (u - \mu_U)$$

(Appendix S1). Note that, due to the quadratic fitness function $\ln(W(y))$, this is the same as the least squares prediction line of $\Theta$ as a function of cue value $u$ (Battacharyya & Johnson, 1977).

This optimal individual reaction norm under imperfect information (eqn 1) may be seen as a weighted average of the optimal phenotype under no information $(\mu_\Theta)$ and the optimal phenotype under perfect information $(\mu_\Theta + \frac{\sigma_\Theta}{\sigma_U} (u - \mu_U))$, with the weight being $|\rho|$ (Fig. 3). Given that $W$ is a Gaussian function of $y$, this linear reaction norm is the optimal reaction norm (i.e. a nonlinear reaction norm would not perform better) as long as $E[\Theta | U = u]$ is a linear function of $u$, which is the case when $U$ and $\Theta$ are binormally distributed (chap. 7.8 Johnson & Wichern, 2007).

Optimality models of this kind have been central in the development of evolutionary ecology (Parker & Maynard Smith, 1990; Sutherland, 2005; Roff, 2010). McNamara et al. (2011) analysed the general optimal linear reaction norm given by eqn (1) in terms of optimal phenology under environmental change. Ergon (2007) used a similar approach to analyse optimal trade-offs between prebreeding survival, onset of seasonal reproduction and reproductive success in populations of multivoltine species with fluctuating densities.

Quantitative genetics models for linear reaction norms – two vs. three traits

The optimal linear reaction norm given by eqn (1) says nothing about the selection process and does not consider genetic constraints. In the following, we will consider a quantitative genetics model for linear reaction norms, assuming phenotypic responses to an interval-scaled cue with an arbitrary zero point (Houle et al., 2011).

In quantitative genetics models for the evolution of phenotypic plasticity, it is common to consider the intercept ($x$) and slope ($\beta$) of the reaction norm as two traits (e.g. de Jong, 1990; Gavrilets & Scheiner, 1993a; de Jong & Gavrilets, 2000; Tufto, 2000; Lande, 2009; Scheiner, 2013). That is, the plastic phenotype is modelled as a function of an environmental cue $u$ in the form

$$y(u) = x + \beta u.$$  

(2)

In this two-trait model, the intercept trait $x$ is the phenotypic expression for the cue value designated as zero. Lande (2009) assumed that minimum phenotypic variation occurred in the mean environment that the population had been adapted to, and hence defined the cue to have its zero point in this reference environment. He then used this reaction norm model (eqn 2) in a quantitative genetics analysis of adaptations to a sudden extreme change in the mean environment when the reference environment remained unchanged.

We will here analyse a more general linear reaction norm model based on the three most fundamental ways that genetic effects can alter a linear reaction norm in such a way that it remains linear: (i) a change along the plastic phenotype-axis, (ii) a change in slope (cue sensitivity), and (iii) a change in the reaction
norm along the cue-axis (Fig. 2). This leads us to consider a linear reaction model in the form

\[ y(u) = z_a + z_b \frac{u}{C_0} z_c \]  

(3)

where \( z_a, z_b \) and \( z_c \) are considered as (latent) traits. A particular genetic effect may of course affect more than one of these traits, but any genetic effect on a linear reaction norm can be decomposed into these three components. Obviously, shifting a linear reaction norm along the cue-axis (a change in \( z_c \)) may have exactly the same effect on the reaction norm as shifting it along the \( y \)-axis (a change in \( z_a \)) (Fig. 2). By rearranging the reaction norm model (3) as \( y(u) = x + z_b \frac{u}{C_0} z_c \), we see that increasing \( z_a \) by one unit has the same effect on \( y(u) \) as decreasing \( z_c \) by \( 1/z_b \) units.

However, traits \( z_a \) and \( z_c \) still represent very different genetic effects within the organisms. Trait \( z_c \) may be thought of as representing genetic effects on ‘perception’ of the environmental cue in a general sense. For example, variation in \( z_c \) may represent genetic effects affecting the sensory apparatus in such a way that different genotypes perceive the same environmental cue as different, but cue perception may not necessarily involve a sensory apparatus (see Discussion). Note that in Lande’s (2009) notation, \( e_t \) corresponds to a random value of \( E \) in generation \( t \), and \( e_t/C_0 \) corresponds to a random \( U \) in the same generation.

Fig. 3 Conceptual overview of optimal linear reaction norms in stochastic environments. The environmental component \( U \) (cue) that determines the mean phenotype and the environmental component \( E \) determining the phenotypic expression that maximize fitness (\( \Theta \)) have a bivariate distribution with correlation \( \rho \) (central 95% of a binormal distribution with \( \rho = 0.5 \) is indicated by the ellipses in the lower right panel). This leads to a bivariate distribution of \( U \) and \( \Theta \) with means \( \mu_U \) and \( \mu_\Theta \), variances \( \sigma_U^2 \) and \( \sigma_\Theta^2 \), and a correlation \( \rho = \sigma_{U\Theta}/(\sigma_U \sigma_\Theta) \) (top right panel). The shaded areas show the conditional probability distributions of \( E \) and \( \Theta \) given a cue value \( u \) (with \( \rho = 0.5 \)). If fitness, \( W \), is a Gaussian function of the plastic phenotype value \( y(u) \), the optimal reaction norm as a function of cue value \( u \) is the same as the least squares prediction of \( \Theta \) given \( u \) and \( y_{opt}(u) = \mu_\Theta + \rho \frac{\sigma_\Theta}{\sigma_U} (u - \mu_U) \), Appendix S1. Some authors refer to \( U \) in this context as a ‘proxy cue’ of environmental component \( E \). However, it is sufficient to only consider \( U \) and \( \Theta \) as two correlated components of a temporally varying environment. Blue line represents the optimal reaction norm under perfect information (\( \rho = 1 \)) (when the ellipses collapse to a line), and green line represents the optimal reaction norm when \( U \) and \( \Theta \) are uncorrelated (\( \rho = 0 \)). Solid red line represents the optimal reaction norm when \( \rho = 0.5 \) (corresponding to the drawn ellipses). Thick stippled red line is referred to in the Analysis section. Note that in Lande’s (2009) notation, \( e_t \) corresponds to a random value of \( E \) in generation \( t \), and \( e_t/C_0 \) corresponds to a random \( U \) in the same generation.
the production of these gene products and their effect on $y(u)$ are independent of the cue. Finally, trait $\zeta_0$ (reaction norm slope) represents variation in gene products that affect the sensitivity of the plastic phenotype $y(u)$ to the cue. With this reaction norm model (eqn 3), $\zeta_0$ may be referred to as a ‘cue reference trait’ although we do not suggest that there is necessarily a ‘template’ of a specific environment that is stored genetically in the organisms; what is essential is the types of genetic variation that is represented by the three traits in the model. Note that it is only when assuming a linear reaction norm that genetic effects on cue ‘perception’ can lead to the same change in the reaction norm as genetic effects on the environment independent component of the plastic phenotype ($\zeta_0$); this will not be the case in a nonlinear reaction norm model (Fig. 2b).

The two-trait model (eqn 2) is a special case of the more general three-trait model (eqn 3) where $\zeta_0$ is fixed to zero. Reaction norm slope is considered as a trait in both models (i.e. $\beta = \zeta_0$), but for clarity we have used separate notations in the two models.

### Analysis

#### Basic properties of the reaction norm models

As already noted, an obvious difference between the two-trait (eqn 2) and the three-trait (eqn 3) reaction norm models is that the two-trait model implies a one-to-one correspondence between genotypes and reaction norms, whereas the three-trait model implies that one reaction norm can represent many genotypes. As we will see below, linear reaction norms in a population will evolve very differently and reach different equilibria when we consider the reaction norm to result from three traits rather than two traits.

An essential difference between the two-trait and the three-trait reaction norm models relates to constraints in the evolution of the covariance between reaction norm intercept and slope in the population. To see this, it is elucidating to consider a particular representation of this covariance, $u_0$, defined as the cue value for which phenotypic variance is at a minimum and where the covariance between the reaction norm intercept and slope is zero (the ‘zone of canalization’ at the population level) is centred around $u_0$. Given a phenotypic covariance between intercept and slope ($P_{ab}$) and a variance in reaction norm slope ($P_{bb}$), this cue value is

$$u_0 = - \frac{P_{ab}}{P_{bb}}$$

(4)

(Appendix S2).

From eqn (4) we see that in the two-trait model (2), where reaction norm intercept ($\alpha$) and slope ($\beta$) are considered as traits, $u_0$ is independent of the trait means, and directional selection on any of the traits will not affect $u_0$ unless the selection also changes the variance of the slope or covariance of the traits. In the three-trait model (3), however, the covariance between intercept and slope depends on the mean traits $\zeta_0$ and $\zeta_{bc}$. Under the assumption of normal traits, $u_0$ then becomes

$$u_0 = \zeta_0 + \frac{\zeta_{bc}P_{bc} - P_{ab}}{P_{bb}}$$

(5)

where $P_{bc}$, $P_{ab}$ and $P_{bb}$ are the elements of the phenotypic variance–covariance matrix indicated by the subscripts (Appendix S2). Thus, under the three-trait model (3), $u_0$ may respond directly to directional selection on both trait $\zeta_0$ (if $P_{bc} \neq 0$) and trait $\zeta_{bc}$. If trait $\zeta_0$ is independent of trait $\zeta_{bc}$ and $\zeta_0$ (i.e. $P_{bc} = P_{ab} = 0$), $u_0$ becomes $\zeta_0$. Note also that $u_0$ is independent of $P_{bc}$.

Lande (2009) defined the cue $u$ ($u_{ref}$ in his model) to have its zero point at $u_0$, referred to as a ‘reference environment’. Hence, one could define the two-trait model analysed by Lande (2009) for any arbitrary interval-scaled cue variable as $y(u) = \alpha + \beta(u - u_0)$ where the genetic correlation between the traits $\alpha'$ and $\beta$ is by necessity zero as $u_0$ is defined by $\text{cov}(y(u_0), \beta) = \text{cov}(\alpha', \beta) = 0$ (Appendix S2; see also last paragraph on page 1438 in Lande (2009)). This model is structurally similar to our three-trait model except that the ‘reference environment’ in our model is considered as an individual trait, $\zeta_0$ (reflecting individual variation in cue ‘perception’), which is exposed to selection. Unlike in Lande’s (2009) model, where the definition of trait $\alpha'$ depends on $u_0$, there are no constraints on the phenotypic or genotypic covariances in our three-trait model (other than the covariance matrix being positive-definite). The two-trait model of Lande (2009) can only evolve in the same way as the three-trait model if $u_0$ is treated as the mean of an individual trait with variance different from zero. Hence, the three-trait quantitative genetics model and Lande’s (2009) two-trait model are not alternative parameterizations of the same model. Lande’s (2009) two-trait model is a constrained version (i.e. a special case) of our more general three-trait model with the trait $\zeta_0$ fixed to $u_0$, which requires that $P_{bc} = P_{ab} = P_{bb} = 0$ as well as $P_{ab} = 0$ ($P_{bb} = 0$ is only required to maintain the same definition of $\zeta_0$ and $\alpha'$ to give $\zeta_0 = u_0$). We will later show that expected $u_0$ at equilibrium in the three-trait model always becomes $\mu_U$.

### Evolution of linear reaction norms

Environmental change may lead to changes in any of the parameters of the joint distribution of the cue ($U$) and the best possible phenotype ($\Theta$) (c.f., eqn 1 and Fig. 3). Any such change will impose directional selection on the individual traits defining the reaction norm, and the evolutionary response to this selection will depend on the additive genetic variances and
covariances of these traits. We will here compare the dynamics of the three-trait model (eqn 3) to the dynamics of the more constrained two-trait version (eqn 2), the intercept–slope model analysed in detail by Lande (2009). Specifically, we will analyse the transient and asymptotic evolution of the reaction norm distribution after a sudden and extreme concomitant change in both $\mu_I$ and $\mu_\Theta$ while $\sigma_{zt}^2$, $\sigma_{ct}^2$ and $\sigma_{ct}^2$ remain unchanged. We assume that all individuals in each generation experience the same environment and that the environments in subsequent generations are independent (as also in Lande’s (2009) analysis). Following Lande (2009), we also assume that trait variances and covariances remain constant under selection. Although this may be a particularly unrealistic assumption (Steppan et al., 2002), it serves the purpose of examining how reaction norms can evolve through changes in trait means only.

**Quantitative genetics – modelling**

Assuming that the individual traits of the reaction norm (3) have a multivariate normal distribution with a constant variance–covariance matrix in a population with discrete generations, the change in the population mean of the traits from a generation $t$ to the next,

$$
\begin{bmatrix}
\bar{z}_a^t \\
\bar{z}_b^t \\
\bar{z}_c^t
\end{bmatrix}_{t+1} =
\begin{bmatrix}
\bar{z}_a^t \\
\bar{z}_b^t \\
\bar{z}_c^t
\end{bmatrix}_t +
\begin{bmatrix}
G_{aa} & G_{ab} & G_{ac} \\
G_{ab} & G_{bb} & G_{bc} \\
G_{ac} & G_{bc} & G_{cc}
\end{bmatrix}_t
\begin{bmatrix}
\bar{\phi}_a_t \\
\bar{\phi}_b_t \\
\bar{\phi}_c_t
\end{bmatrix}_t,
$$

is the product of the additive genetic variance–covariance matrix for the traits, $G$, and the selection gradient $\bar{\phi}_t$. Here, $\bar{\phi}_t$ is the sensitivity of the logarithm of population mean fitness to changes in each of the mean trait values (Lande, 1979; Lande & Arnold, 1983).

$$
\bar{\phi}_t = \begin{bmatrix}
\partial W_r / \partial z_a \\
\partial W_r / \partial z_b \\
\partial W_r / \partial z_c
\end{bmatrix}
\ln(W_r).
$$

We will assume a Gaussian fitness function with width $\omega$ and peak value $W_{\text{max}}$, and that all individuals experience the same environment in any generation.

A random individual in generation $t$ has phenotype $y_t(u_t) = z_{a,t} + z_{b,t}(u_t - z_{c,t})$, where the traits $[z_{a,t}, z_{b,t}, z_{c,t}]$ are drawn from a multivariate normal distribution with mean $[\bar{z}_a, \bar{z}_b, \bar{z}_c]$ and phenotypic covariance matrix $P$. When the phenotypic expression that maximizes fitness in that generation is $\theta_t$, this individual will have fitness

$$
W_t = W(y_t(u_t), \theta_t) = W_{\text{max}} \exp \left( \frac{(y_t(u_t) - \theta_t)^2}{2\omega^2} \right).
$$

To find an analytical expression of the selection gradient (7), a common approach (Lande & Arnold, 1983; Lande, 2009) would be to first find the population mean fitness by integrating over the phenotype distribution, $p(y_t(u_t))$,

$$
W_t = \int_{-\infty}^{\infty} W(y_t(u_t), \theta_t)p(y_t(u_t))dy.
$$

However, because $p(y_t(u_t))$ is not normal as it involves the product of the two normally distributed traits $z_{b,t}$ and $z_{c,t}$, it is not straightforward to solve this integral analytically. Indeed, it seems that an exact analytical expression for the selection gradient (7) does not exist. We therefore initially based our analysis on simulations of the evolutionary process (6), where the selection gradient (7) is computed numerically by simulating a population of 10 000 individuals at each generation (see Appendix S5 for R code). These simulations are accompanied by (and compared to) mathematical analyses presented in Appendix S3 and Appendix S4.

In the simulation results presented in Fig. 4, we used the same parameter values as in Lande’s (2009) analysis of the two-trait model except that we, for convenience, used a somewhat less extreme sudden change in the environment, with a change in $\mu_I$ and $\mu_\Theta$ of 3 (instead of 5) standard deviations of the background fluctuations ($\sigma_I$ and $\sigma_\Theta$ of eqn 1). As Lande (2009), we used a diagonal $G$ matrix and sat $G_{ct} = 0$ to half the cue variance (three-trait model) or zero (two-trait model). For simplicity, in the simulations we also assumed that only trait $z_a$ had a nonadditive residual component with variance $\sigma_{zt}^2$, such that $P_{aa} = G_{aa} + \sigma_{zt}^2$, $P_{bb} = G_{bb}$, $P_{cc} = G_{cc}$, and $P_{ab} = P_{ac} = P_{bc} = 0$. The two-trait model is obtained simply by setting also $P_{ac} = 0$ and $z_c = 0$.

**Quantitative genetics – results**

The simulations show that immediately after the sudden environmental change, there is a rapid increase in reaction norm slope (Fig. 4b), while $z_a$ (Fig. 4c) swings back in the opposite direction of the change in mean cue $\mu_I$ (i.e. away from the new optimum). This phase of the adaptation may be characterized as a ‘stage of alarm’, where exaggerated perception of the environmental change becomes adaptive. As $z_a$ moves towards the new optimum (Fig. 4a), the reaction norm slope $z_b$ is reduced and $z_c$ turns towards the new optimum. Eventually, $z_a$ stabilizes around $\mu_I$ and $z_b$ stabilizes around $\mu_\Theta$ (Fig. 4d), in accordance with the theoretical results in Appendix S3 (see Appendix S4 for detailed numerical results). Note that with $P_{ab} = P_{bc} = 0$ (as in the simulations), the theoretical equilibrium mean values $z_{a,e} = \mu_\Theta$ and $z_{c,e} = \mu_I$ are independent of the variances and covariance of $U$ and $\Theta$. In Appendix S4, we conjecture that the equilibrium mean traits $z_{a,e}$ and $z_{c,e}$ in general (for $P_{ab} \neq 0$ and $P_{bc} \neq 0$) are affected by $\sigma_{I,\Theta}^2$, $\sigma_{I,\Theta}^2$ and $\sigma_{\Theta,\Theta}$, but only indirectly through $z_{c,e}$.

As we used a diagonal phenotypic variance–covariance matrix ($P$) in the simulations, the cue value $u_0$
In contrast, in the two-trait model, the mean environment regardless of what this mean is. (Appendix S4), this property (simulations (Figs S1–S5 show simulation results for a scenario where the phenotypic variance–covariance matrix here is diagonal (see eqn 5)). Solid blue lines represent the three-trait model (3) and the stippled red lines represent the two-trait model (2). The trajectories were calculated as the mean of 1000 independent simulations. Grey lines show the realization of a single simulation. Solid green lines show μu (panel a), the optimal slope when reaction norm slope and intercept can be tuned independently, σ2/σ2 (eqn 1) (panel b), and μl (panel c). In panel a, the dotted blue line is the mean intercept (uz − uz − Pz) in the three-trait model for comparison with the intercept trait in the two-trait model (stippled red line). In panel b, stippled green line shows the approximate equilibrium mean slope, uz ≈ σuz/(σz + Pz). Parameter values in the initial environment were μu = 0, μl = 0, σz = 2, σl = 4, and ρ = σl/σz = 0.25. At generation 5000, μu jumps to 6 and μl jumps to 12 while the other parameters remain unchanged. Diagonal G and P matrices were used with gaa = 0.5, Paa = Gaa + 0.5, Pbb = Gbb + 0.045, and Pzz = Gzz = 2 (three-trait model) or Pzz = Gzz = 0 (two-trait model). Initial mean trait values were uz = 0, zb = ρσz/σz = 0.5, and uz = 0.

Fig. 4 Evolution of linear reaction norms after a sudden environmental change. Panels a–c: Trajectories of the population mean trait values with a sudden environmental change at generation 5000 (see text). Panel d: Phase plane diagram showing uz plotted against zb through all generations (this is the point in the cue phenotype plane where reaction norms ‘tend to cross’ (see Figs 1 and 5), as the phenotypic variance can only be minimized when the mean environment equals that yields minimum phenotypic variance (eqn 5) equals uz, which stabilizes around the theoretical equilibrium μu (Fig. 4c; Appendix S3). Hence, in this case, equilibrium uz becomes uz = μu. As shown both by simulations (Figs S1–S3) and theoretical considerations (Appendix S4), this property (uz = μu) holds also when P is not diagonal – that is, at equilibrium, phenotypic variance is always minimum in the mean environment. As a result, the three-trait model leads to complete genetic assimilation in the sense that the population-level zone of canalization (represented by uz) evolves to the mean environment regardless of what this mean is. In contrast, in the two-trait model, uz does not evolve in response to changes in the trait means and the phenotypic variance can only be minimized when the mean environment equals −Pz/Pbb (see eqn 4). This contrast in the asymptotic state of the systems obtained from the two alternative reaction norm models is illustrated in Fig. 5, whereas Fig. 6 shows the trajectories of phenotypic variation and difference between uz and μu in the simulated scenario presented in Fig. 4. Figures S4 and S5 show simulation results for a scenario where there is no environmental variation before and after the sudden environmental change (more similar to classic examples of genetic assimilation).

Interestingly, as seen in Fig. 4b, the mean reaction norm slope zb in the three-trait model stabilizes at a lower level than the optimal slope yielding the highest expected fitness of an individual, σ2/σ2 (see eqn 1), which is also the equilibrium mean slope in the two-trait model (Gavrilets & Scheiner, 1993a; Lande, 2009). Intuitively, this is because the optimal value of trait zb...
of an individual depends on the value of trait $z_c$ that this individual possesses, which is stochastic. Under the assumption that $P_{ab} = P_{bc} = 0$, an approximate mean slope value is found as $\bar{\beta}_z \approx (\sigma_{y\theta} + P_{ac})/\sigma_{y}^2$ (Appendix S4 and eqn 10 below), which is close to the stationary mean in the simulations (Fig. 4). For comparison, the equilibrium mean traits in the two-trait model become $\bar{\beta} = \sigma_{y\theta}/\sigma_{y}^2$ and $\bar{\mu} = \mu_0 - \bar{\beta}\mu_U$ (Gavrilets & Scheiner, 1993a; Lande, 2009). Note that the denominator in the approximate expression for $\bar{\beta}_z$ is the variance of $(U - z_c)$, and not the variance of the cue $U$ alone as in the expression for $\bar{\beta}^*_{\mu}$ in the two-trait model; that is, genetic variance in the perception trait $z_c$ inflates the variance of the perceived cue $(U - z_c)$. Hence, if $P_{ac} = 0$, $\bar{\beta}_z$ is always lower than the optimal slope in eqn (1) unless $P_{ac} = 0$ (which gives the two-trait reaction norm model). This is indicated by a stippled reaction norm in Fig. 3.

![Fig. 5](image1.png) Reaction norm distribution when the populations have reached a stationary dynamics in the two-trait model (a) and the three-trait model (b) under the scenario presented in Fig. 4. The distribution of the environmental cue ($U$) in the new environment is indicated by the shaded areas on the x-axes, and the central 95% of the joint distribution of $U$ and $\Theta$ is shown with the ellipses with an ‘x’ at the mean. For each model, 50 random reaction norms (genotypes) are plotted. In the two-trait model, the cue value $u_0$ where phenotypic variation is minimal will always be at zero when reaction norm slope and intercept are independent (indicated with a white, crossed, symbol plotted at the mean plastic phenotype for this cue value). In contrast, in the three-trait model genetic assimilation becomes complete and $u_0$ moves to $\mu_U$ with a mean plastic phenotype at $\mu_0$.

![Fig. 6](image2.png) Phenotypic standard deviation, SD($y$) (a), and the distance between the mean environment and the zone of canalization, $\mu_U - u_0$ (b), in the simulations presented in Fig. 4. Blue solid lines represent the three-trait model, whereas the red stippled lines represent the two-trait model. Horizontal grey lines are drawn at the mean values of the last 3000 generations prior to the sudden environmental change at generation 5000. Lines show the mean of 1000 independent simulations plotted at every 100th generation.
As seen in Fig. 4b, the asymptotic mean \( \bar{z}_b \) in the simulations (where \( P_{ac} = 0 \)) is close to but somewhat larger than the approximation \( \bar{z}_b \approx \bar{z}_b/(\sigma_b^2 + P_{ac}) \). This discrepancy is further analysed in Appendix S4. As shown there, the equilibrium mean reaction norm slope \( \bar{z}_b \) can be approximated analytically if we assume that the plastic phenotype \( y(u) \) has a normal distribution, which is very nearly the case with the parameter values in our simulations in Fig. 4. The integral (9) then has an analytical solution, and as a result, an approximate equilibrium slope \( \bar{z}_b \) can be found numerically from the equation (assuming \( P_{ab} = P_{bc} = 0 \))

\[
\bar{z}_b \approx \frac{\sigma_{u\theta} + P_{ac}}{\sigma_{b}^2 + P_{ac}} + \frac{\sigma_{b}^2 + \sigma_{u\theta}^2 \sigma_{b}^2}{\sigma_{b}^2 + P_{ac}} - \frac{2\sigma_{b}^2 \sigma_{u\theta} + P_{ac} \sigma_{u\theta}^2}{\sigma_{b}^2 + P_{ac}} \left( P_{ac} + \frac{\sigma_{ac}^2}{\sigma_{c}^2} P_{ac} \right).
\]

\[(10)\]

where the large values of \( \sigma_{a}^2 \) and especially \( \sigma_{u}^2 \) used in the simulations make the second term positive but small compared with the first term (see Appendix S4 for detailed numerical results).

Another reason for the discrepancy between the asymptotic mean \( \bar{z}_b \) in the simulations and the approximation \( \bar{z}_b \approx \bar{z}_b/(\sigma_b^2 + P_{ac}) \) is that when the population under directional selection based on eqn (6) evolves towards a stationary state, the mean traits will fluctuate around the equilibrium because of the influence from the random inputs \( u_i \) and \( \theta_i \) (as seen in Fig. 4). In stationarity, this leads to \( \bar{z}_a = E[\bar{z}_a] + v_\theta, \) etc. (where \( E[\bar{z}_a] = \lim_{N \to \infty} \frac{1}{N} \sum_{i=1}^{N} \bar{z}_{a,i} \) and \( E[v_\theta] = 0 \) etc.) and, as shown in Appendix S4, the variances and covariances of \( v_{u}, v_{\theta} \) and \( v_{c} \) then enter into eqn (10). Note that we assume that \( u_i \) and \( \theta_i \) have zero autocorrelation, such that the covariances between the mean reaction norm parameters and the environment, caused by adaptive tracking (Tufto, 2015), are zero.

Because the equilibrium reaction norm slope \( \bar{z}_b \) is influenced by the phenotypic variance of the cue reference trait \( \bar{z}_c \) (and its covariance with the other traits; eqn 10), and hence deviates from the slope that maximizes fitness (eqn 1), the expected fitness at equilibrium will be lower than the expected fitness of the optimal individual reaction norm in eqn (1) (Fig. 7, lower right panel). As a consequence, a proportion of the population will have a higher expected fitness than an individual with mean trait values. Nevertheless, mean fitness in the population after the environmental change stabilizes around a higher level in the three-trait model than in the two-trait model (Fig. 7, left panels), despite a lower expected fitness at mean trait values (right panels). The reason for this is that the three-trait model gives a lower phenotypic variance in the new environment (Fig. 6a). Mean fitness in the two-trait model thus stabilizes around the optimum only when the mean cue is zero because phenotypic variance will not be minimized in other environments (Fig. 7, left panels).

**Discussion**

Quantitative genetics models are theoretical models for the joint evolution of population means of quantitative individual phenotypic traits, where the researchers define traits that they find most meaningful in the context they are studied. In quantitative genetics models of reaction norms where a plastic phenotype is modelled as a linear function of an interval-scaled environmental cue, the reaction norm intercept and slope are often considered as individual traits subjected to selection (Gavrilets & Scheiner, 1993b; Scheiner, 1993, 2013; de Jong & Gavrilets, 2000; Tufto, 2000, 2015; Lande, 2009). The intercept of such a reaction norm (i.e. the reaction norm value at cue value zero) is often not very biologically meaningful because this trait, as well as its variance and covariance with other traits, depends on the defined zero point, or ‘reference cue’, of the (arbitrary) interval-scaled cue variable. One may, however, as in Lande (2009), define the zero point of the cue to be the mean cue value which the population is adapted to. This ensures that the variance of the plastic phenotype is minimized in the mean environment, which is theoretically plausible (Bürger, 2000; Lande, 2009; Le Rouzic et al., 2013), but it is not clear how this ‘reference cue’ may evolve (in Lande’s (2009) analysis it is assumed to remain constant; see however de Jong & Gavrilets, 2000).

We have here suggested that the ‘reference cue’ can be considered as an individual trait that reflects genetic variation in cue ‘perception’ in a general sense, and hence considered a linear reaction norm in the form \( y(u) = z_u + z_b(u - \bar{z}_c) \). In this model, the biological meaning of all the traits, and their variances and covariances, is not modified when redefining the zero point of the cue variable \( u \) (which is not the case for the intercept \( z = z_u + z_b(\bar{z}_c - \bar{z}_c) \)). The three traits in this model reflect three fundamentally different genetic effects on linear reaction norms. Whereas \( z_b \) represents genetic effects on cue sensitivity, \( \bar{z}_c \) reflects genetic effects on cue ‘perception’ (in the general sense discussed below) and has the same scale as the environmental cue, and \( z_u \) represents genetic effects that are both independent of the cue value and invariant to its defined zero point (the latter is not the case for the intercept). These structural differences in the reaction norm models matter for the equilibrium mean reaction norms (and distributions), because the traits do not have independent effects on the plastic phenotype \( y(u) \) (note the product \( z_b \bar{z}_c \) in the three-trait model).

In our analysis of the three-trait model, we have shown that the cue value where variance of the plastic phenotype is minimized (where reaction norms ‘tend to
cross; $u_0$) always evolves to equal the mean environment at equilibrium. This occurs without assuming any cost of maintaining plasticity (DeWitt et al., 1998; West-Eberhard, 2003; Pigliucci et al., 2006; Lande, 2009; Bateson & Gluckman, 2011; Svennungsen et al., 2011), or any change in the variances or covariances of our defined traits (de Jong & Gavrilets, 2000). Even though $u_0$ may be interpreted as $\frac{\text{cov}(\text{intercept, slope})}{\text{var}(\text{slope})}$, $u_0$ is biologically more meaningful than the covariance between reaction norm slope and a somewhat arbitrarily defined intercept trait. Note that $u_0$ is a population-level parameter that does not depend on any quantitative genetics model for the linear reaction norm, and which can easily be estimated (as discussed below). Further, our analysis also demonstrate that the equilibrium mean reaction norm slope in the three-trait model will deviate from the optimal slope yielding the highest expected fitness of a hypothetical individual that can tune reaction norm intercept and slope accurately and independently (eqn 1), which is also the equilibrium mean slope of the two-trait model (Gavrilets & Scheiner, 1993a; Lande, 2009). At least when there is weak correlation between $z_b$ and $z_c$ (i.e. $P_{bc}$ is sufficiently small), the equilibrium mean slope will be lower than the optimal individual slope. Intuitively, this is because the optimal slope is lower when the cue reference trait of a random individual, in addition to the environmental cue, is stochastic due to random mating.

As a consequence, maximum expected fitness does not occur at the mean trait values in the population.

In the three-trait model, phenotypic variance in a given environment increases with both $z_b$ and the distance between $z_c$ and the environmental cue ($u$), at least when the traits are independent (see eqn S4-3 in Appendix S4), whereas in the two-trait model, phenotypic variance is independent of the trait means (Fig. 6). In our simulations, after the sudden environmental change, there is a rapid initial increase in both $z_b$ and the distance between $z_c$ and the new mean cue value (i.e. $z_c$ initially evolves rapidly in the opposite direction of the change in the environmental cue, such that the perception of the environmental change is exaggerated). Hence, due to the positively interacting effects of $z_b$ and $z_c$ on the plastic phenotype $y(u)$, this efficiently increases phenotypic variance in the new environment which enhances the evolvability of the plastic phenotypic character and acts to restore population mean fitness (see Figs 4 and 7). The subsequent process of assimilation whereby reaction norm slope $z_b$ is reduced, $z_c$ moves towards the mean cue value, and $z_a$ evolves towards mean $\Theta$, is a much slower process.

**Genetic effects on linear reaction norms**

Although a shift in the reaction norm along the cue-axis (through trait $z_c$) can have exactly the same effect
on the individual linear reaction norm as a shift along the phenotype-axis (through trait $z_c$), the genetic bases for these effects are fundamentally different, and, as explained above, changes in the means of these two traits have different effects on the population. It also seems obvious that there will often be genetic variation on both these traits. Phenotypic plasticity involves complex pathways, at both organismal and cell levels, from perception of environmental cues and physiological transduction to phenotypic expression (reviewed in Sultan & Sterans, 2005). Depending on the type of organism and the nature of the phenotypic characters and the environmental cues, these pathways may, to varying degrees, involve sensory systems, neuroendocrine and metabolic systems, cellular reception, gene regulation networks, and other developmental, physiological and behavioural processes. Environmental conditions may directly affect any of these systems and processes, not just the sensory systems (e.g. temperature may directly affect metabolism and gene regulation in ectothermic organisms (Gil-loody et al., 2002; Ellers et al., 2008), and various processes may be affected by food constituents (Sanders et al., 1981; Meek et al., 1995; Krol et al., 2012) and nutritional state (Lölmus & Sundström, 2004; Rui, 2013; Mueller et al., 2015)). Genetic variation in upstream (i.e. close to the cue perception) regulatory processes, which may involve cue activation thresholds for transduction elements, may affect the way the environment is 'perceived' (in a general sense) by the organism, and hence the cue reference trait (trait $z_c$) in our model. Genetic variation in downstream processes close to the phenotypic expression of quantitative characters, on the other hand, may affect the degree of up/down-regulation in response to given levels (and types) of transduction elements and hence the slope of linear reaction norms (trait $z_b$ in our model). Finally, some genetic variation may have the same additive effect on the phenotypic expression of the environmental cue (trait $z_a$ in our model). The importance of differentiating between these three traits may be better appreciated when considering the effects of the mean traits on the population; A change in $z_c$ will change the cue value at which different genotypic reaction norms tend to cross ($u_0$), whereas a change $z_b$ will not. Although there is ample evidence for widespread genetic variation for reaction norms in natural populations (Falconer & Mackay, 1996; Sultan & Sterans, 2005; Sengupta et al., 2016), there are not many examples where the full pathway of phenotypic plasticity from cue perception to phenotype expression is known in great detail (Sultan, 2010; Morris & Rogers, 2014), and even less is known about the genetic variation of the different elements of these pathways. It seems, however, obvious that there may be substantial genotypic variation in perception of environmental cues (i.e. variation in trait $z_c$ in our model). Examples indicating genetic variation in environmental perception include substantial among-population variation in the signal transduction pathway of induced plant defence in Arabidopsis thaliana (Kliebenstein et al., 2002), and individual variation in systemic stress responses has likely components of individual variation in what is perceived as stressful (Hoffmann & Parsons, 1991; Badyaev, 2005; Dingemanse et al., 2010). There is also considerable variation and ‘fine-tuning’ in light (and shading) perception systems involving phytochromes that are sensitive to different wavelengths in plants (Smith, 1990, 1995; Schlütting & Smith, 2002).

**Predictions and empirical evaluations**

Parameters in a reaction norm function considered as quantitative traits are always latent in the sense that one cannot measure their phenotypic value by a single measurement of an individual (except for traits that are defined for a particular environment, such as an intercept). Although one may estimate reaction norm intercept and slope from multiple measurement of the same genotype or related individuals with known genealogy (Nussey et al., 2007; Martin et al., 2011), such data alone does not provide enough information to separate the traits $z_c$ and $z_b$ (from a statistical point of view, the three-trait model fitted to such data is overparameterized, which may be one of the reasons it has not previously been considered). Nevertheless, if one have a detailed understanding of the physiological (or developmental) mechanisms of the plastic response, one may still be able to estimate meaningful reaction norm traits beyond a phenomenological ‘intercept’ and ‘slope’, including traits associated with cue perception (trait $z_c$). Time-series data from selection experiments may also provide information about the genetic architecture of the reaction norms (Fuller et al., 2005).

The cue value that gives minimum phenotypic variation in the population ($u_0$) may be estimated by fitting data on genotype-specific phenotypic measurements to mixed-effects linear models with random individual slopes and intercepts (Martin et al., 2011; Bates et al., 2015), or from a random regression ‘animal model’ building on a known relatedness among individuals (Nussey et al., 2007). Our three-trait quantitative genetics model gives certain predictions about the evolution of $u_0$ under environmental change. Our analysis shows that the mean cue reference trait ($z_c$), and hence $u_0$ (eqn 5), will respond rapidly to changes in the mean environment (provided sufficient additive genetic variation). Whenever there is selection for increased plasticity (i.e. selection for higher $z_b$), exaggerated perception of the environmental change also becomes adaptive, and one may observe that $u_0$ swings away in the opposite direction of the change in the mean cue during a ‘stage of alarm’ after large and fast changes in the environment (see Fig. 4). Later, $u_0$ will move
towards, and eventually fluctuate around, the new cue value. In contrast, under the two-trait model \( u_0 \) will not change in response to changes in the mean cue value.

**Future directions**

In this paper, we have made a number of simplistic, but quite standard, assumptions, including interval-scaled cues and phenotypes, Gaussian fitness with constant width and peak value, lack of density and frequency dependence, random mating, discrete generations where all individuals are exposed to the same environment (e.g. no spatial heterogeneity), and uncorrelated environments from one generation to the next. These assumptions may be modified or relaxed in future developments. In particular, the two-trait model has been used in theoretical studies involving within-generation heterogeneity (de Jong & Gavrilets, 2000; Tufto, 2000, 2015; Scheiner, 2013). We suggest that these studies may be developed by including a cue reference trait in the linear reaction norms (our three-trait model). The models may also be modified by incorporating different reaction norm shapes. Notably, de Jong & Gavrilets (2000) allowed the genetic covariance between reaction norm intercept and slope, as well as their variances, to evolve through selection on allelic pleiotropy. It would be interesting to repeat their approach on our three-trait model to investigate the relative contributions (and synergies) of the evolution of trait means and trait variances and covariances.

Several authors have assumed flexible polynomial reaction norms with the polynomial coefficients considered as traits (Gavrilets & Scheiner, 1993a,b; Scheiner, 1993; Via et al., 1995). We suggest that such rather phenomenological nonlinear reaction norm models may be modified by considering the slope and perception traits of the three-trait model as themselves dependent on the environment, which may result in a polynomial of \( (u - z_c) \); considering trait \( z_b \) as a linear function of \( (u - z_c) \) results in a reaction norm that is a second-order polynomial of \( (u - z_c) \), etc. Note that in nonlinear reaction norms, unlike linear ones, a change in the perception trait(s) will never have the same effect on the genotypic reaction norm as a change in elevation trait (the component of the plastic phenotype independent of the environment) (see Fig. 2b).

Regardless of the reaction norm shape, we argue that it is essential to distinguish genetic variation in how the environmental cues are perceived from other genetic variation affecting the reaction norm distribution in the population. We suggest that future developmental and behavioural studies pay more attention to genetic variation in environment perception and transduction, and that the contributions of such genetic variation to phenotypic variation in natural environments are evaluated.

**Data archiving**

No data used. The R code used for simulations is provided in Appendix S5 in the Supporting Information.

**Acknowledgments**

We thank Arnaud Le Rouzic, Richard Gomulkiewicz, Samuel M. Scheiner, Thomas F. Hansen, Øistein H. Holen and two anonymous reviewers for comments on earlier versions of the manuscript; we greatly appreciate their input and advice but may still disagree on some issues. This work made use of the Abel computing cluster, owned by the University of Oslo and the Norwegian meta-centre for High Performance Computing (NOTUR). We are thankful for technical support from the Research Computing Services group at USIT, University of Oslo.

**References**


Dworkin, I. 2005. Canalization, cryptic variation, and developmental buffering: a critical examination and analytical


Supporting information

Additional Supporting Information may be found online in the supporting information tab for this article.
Appendix S1 Optimal reaction norms.
Appendix S2 Cue value when phenotypic variance is minimized and covariance between reaction norm slope and phenotype is zero.
Appendix S3 Equilibrium mean traits $\tilde{z}_a$ and $\tilde{z}_c$ and equilibrium $\mu_e$ when $P_{ab} = P_{bc} = 0$.
Appendix S4 Further mathematical analyses and comparisons with simulation results.
Appendix S5 R code for simulations.
Figure S1 Simulation results with non-diagonal variance-covariance matrices $G$ and $P$.
Figure S2 Histogram and qq-plot showing the equilibrium phenotypic distribution in the simulations presented in Figure S1.
Figure S3 Phenotypic standard deviation and the distance between the mean environment and the zone of canalization, $\mu_U - \mu_O$, in the simulations represented in Figure S1.
Figure S4 Simulation results for a scenario where there is no environmental variation before and after the sudden environmental change and the traits are independent (diagonal $P$).
Figure S5 Phenotypic standard deviation and the distance between the mean environment and the zone of canalization, $\mu_U - \mu_O$, in the simulations represented in Figure S4.

Received 19 March 2016; accepted 17 October 2016