Short-term flood probability density forecasting using a conceptual hydrological model with machine learning techniques

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Abstract

Making accurate and reliable probability density forecasts of flood processes is 2 fundamentally challenging for machine learning techniques, especially when prediction 3 targets are outside the range of training data. Conceptual hydrological models can reduce 4 rainfall-runoff modelling errors with efficient quasi-physical mechanisms. The Monotone 5 6 Composite Quantile Regression Neural Network (MCQRNN) is used for the first time to make probability density forecasts of flood processes and serves as a benchmark model, 7 whereas it confronts the drawbacks of overfitting and biased-prediction. Here we propose 8 an integrated model (i.e. XAJ-MCQRNN) that incorporates Xinanjiang conceptual model 9 10 (XAJ) and MCQRNN to overcome the phenomena of error propagation and accumulation 11 encountered in multi-step-ahead flood probability density forecasts. We consider flood forecasts as a function of rainfall factors and runoff data. The models are evaluated by long-12 term (2009-2015) 3-hour streamflow series of the Jianxi River catchment in China and 13 14 rainfall products of the European Centre for Medium-Range Weather Forecasts. Results 15 demonstrated that the proposed XAJ-MCQRNN model can not only outperform the MCQRNN model but also prominently enhance the accuracy and reliability of multi-step-16 17 ahead probability density forecasts of flood process. Regarding short-term forecasts in 18 testing stages at four horizons, the XAJ-MCQRNN model achieved higher Nash-Sutcliffe Efficiency but lower Root Mean Square Error values, while improving Coverage Ratio and 19 Relative Bandwidth values in comparison to the MCQRNN model. Consequently, the 20 21 improvement can benefit the mitigation of the impacts associated with uncertainties of 22 extreme flood and rainfall events as well as promote the accuracy and reliability of flood 23 forecasting and early warning.

Keywords: Short-term flood forecast; Probability density forecast; Monotone
 composite quantile regression; Conceptual model; Machine learning

26

27 **1 Introduction**

Floods are among the world's costliest disasters, and climate and anthropogenic 28 changes have made catastrophic floods much more likely happen. Over the past century, 29 floods accounted for about 30% of natural disasters, claiming more than 19% of the 30 total fatalities and more than 48% of the total number of people affected (Adikari and 31 Yoshitani, 2009; Takeuchi et al., 2018). Flood forecasting and early warning play a 32 pivotal role in geohazard mitigation, floodplain management, design and management 33 of infrastructure projects, agricultural cultivation, and human daily life (Liu et al., 2018; 34 Giuliani et al., 2019). Therefore, accurate and reliable forecasting of flood processes 35 during rainstorm events is extremely crucial and beneficial for a country or catchment, 36 whose prosperity is largely dependent on the optimum use of water resources and flood 37 level control. 38

To date, a wide variety of modelling frameworks have been introduced to model 39 the complicated nonlinear rainfall-runoff process (Sood and Smakhtin, 2015; Shen, 40 2018; Kan et al., 2020). In general, these modelling frameworks can be categorized into 41 three groups: conceptual, physically-based and machine learning models. A conceptual 42 hydrological model typically includes prior-knowledge as a necessary part of 43 conceptual components, possessing quasi-physical mechanisms (Li et al., 2020; Tarek 44 et al., 2020). There are all sorts of spatially lumped and distributed conceptual models 45 46 available with deterministic and stochastic parameter values for a given point or region. A physically-based model usually establishes a simplified catchment system and 47

expresses the internal hydrological processes through several mathematical equations 48 considering the spatial variability of rainfall and parameters (Li et al., 2019; Li and 49 50 Willems, 2020). However, physically-based models encounter a much higher challenge when trying to achieve the required prediction accuracy due to limited watershed 51 52 information. An alternative, the machine learning model, constructs a direct mapping between rainfall and runoff variables and extracts their relationship according to the 53 historical observations by machine learning algorithms, without a piece of prior 54 knowledge in relation to internal hydrological processes (Feng et al., 2020; Kao et al., 55 56 2020; Li et al., 2020; Lin et al., 2020; Nearing et al., 2020; Xiang et al., 2020).

To the best of our knowledge, the growth in machine learning for hydrological 57 sciences is tied to advances in computing power as well as the vast increase of 58 59 hydrological observations. However, machine learning models are purely data-driven and do not have any physical mechanisms, which easily lead to overfitting and biased-60 predictions, especially when prediction targets are unobserved and outside the range of 61 62 rainfall-runoff data adopted for model training (Hunter et al., 2018; Xie et al., 2021). Typically, at longer forecast horizons, the non-availability of antecedent streamflow 63 data makes it fundamentally challenging to maintain the forecast accuracy of data-64 driven models. Such weakness imposes limitations on the applicability of data-driven 65 models in rainfall-runoff studies (Schmidt et al., 2020; Zahura et al., 2020). In 66 comparison to physically-based models, conceptual models have been widely applied 67 68 in rainfall-runoff modelling owing to the practical and simple manner. Formulation of conceptual models signifies only a partial set of the real hydrological cycle processes. 69

70	This triggers several constraints like model calibration and parameter transferability
71	difficulties (Humphrey et al., 2016; Kumanlioglu and Fistikoglu, 2019), in cases where
72	forecasters and decision-makers usually require prior knowledge for calibrating and
73	running conceptual models to achieve reasonable accuracy of flood forecasts (Bandai
74	and Ghezzehei, 2020; Gu et al., 2020). Although conceptual and data-driven models
75	are derived from different philosophies, they can help remedy and enhance each other
76	with regard to their inherent limitations and strengths (Tian et al., 2018; Sun et al., 2019;
77	Chadalawada et al., 2020). Hence, a hybridization of both models is an attractive and
78	effective approach for rainfall-runoff modelling (Yong et al., 2017; Kurian et al., 2019;
79	Ghaseminejad and Uddameri, 2020). For instance, Yang et al. (2019) evaluated the
80	integration of machine learning and conceptual models for flood simulation at 1032
81	streamflow gauging stations worldwide. Farfan et al. (2020) adopted streamflow series
82	forecasts made by a conceptual model as input data of back-propagation neural
83	networks to forecast streamflow data. Hitokoto and Sakuraba (2020) integrated a
84	rainfall-runoff model and a feed-forward artificial neural network to predict real-time
85	water level processes. Hosseiny et al. (2020) integrated a two-dimensional hydraulic
86	model, a random forest classification and a multilayer perceptron for modeling flood
87	depth of the river segment of the Flaming Gorge Dam in the northeast corner of Utah
88	in the US. Konapala et al. (2020) verified hybrid models constructed by combining a
89	conceptual model with a long short-term memory neural network on their capability to
90	simulate streamflow series in hundreds of catchments across the US. The above-
91	mentioned studies explored hybrid models for flood prediction in watersheds with

diverse climate conditions by means of point forecasts. This study is the first to apply 92 conceptual models with artificial neural networks incorporating flood probability 93 94 density (FPD) forecasting for a humid subtropical climate. Exploration of conceptual and machine learning models for FPD forecasting in this study is owing to the following 95 reasons: first, conceptual models possess superior operability while machine learning 96 models possess efficient computation power; and second, physically-based models 97 usually have bottlenecks of low prediction accuracy and time-consuming due to the 98 limitation of available data or quality on the physical properties of watersheds (Liu et 99 100 al., 2018; Li et al., 2020; Cui et al., 2021; Kao et al., 2021).

Previous research regarding hybrid models mainly concentrated on point forecasts 101 or interval predictions of flood processes by integrating conceptual models with single-102 103 output artificial neural networks, whereas to date no study has involved FPD forecasting. Point forecasting, the most frequently used approach, can provide a point estimate of 104 the future flood as precisely as possible for each forecast horizon. Rather than offering 105 106 single-valued forecasts, interval prediction approaches attempt to create well-calibrated lower and upper bounds of each future prediction subject, to a prescribed confidence 107 level. Furthermore, FPD forecasting can provide flood forecasts in the form of quantile 108 point forecasts, confidence interval forecasts and probability density functions. 109 Although it needs extra efforts to calculate the probability for each possible prediction, 110 additional information gained is highly helpful to promote the full understanding of 111 112 flood predictability. FPD forecasting not only effectively quantifies the uncertainties in input datasets but also has the ability to construct the complete conditional probability 113

density curves of future flood processes. Consequently, there is a noticeable migration 114 from point forecasts and interval predictions towards FPD forecasts where modelers 115 116 seek to characterize the full probability distribution of flood events. Among machine learning techniques, the Monotone Composite Quantile Regression Neural Network 117 (MCQRNN) is a special type of multi-output artificial neural networks (ANN) that can 118 effectively estimate multiple non-crossing and nonlinear quantile functions 119 simultaneously. It is a novel and appealing approach for probability density forecasting, 120 as compared with other multi-output ANNs like support vector machine and long short-121 122 term memory (Cannon, 2018). Since MCQRNN applications do not exist in FPD forecasts, it would be important and interesting to explore in-depth conceptual 123 hydrological models to decrease the uncertainty of multi-output ANN (e.g. MCQRNN) 124 125 for FPD forecasting.

The novelty of this study relies on the integration of the Xinanjiang (XAJ) 126 conceptual model and the innovative MCQRNN with a multi-output task. Meanwhile, 127 128 this is the first application of the integrated XAJ-MCQRNN model for FPD forecasting. There are three main steps in this approach. First, the conceptual hydrological model 129 for rainfall-runoff simulation was constructed to create point forecasts of flood 130 processes and the outputs were used as inputs of the machine learning model. Second, 131 the multi-output machine learning model for FPD forecasting was built to further create 132 interval forecasts of flood processes after being supplied with point forecasts by the 133 134 conceptual model. Third, the training process of the hybrid model was optimized by an evolutionary optimization algorithm, and the predictability of the hybrid model was 135

tested by using medium-range numeric rainfall forecast products. The Jianxi Rivercatchment of China constituted the case study.

138

139 2 Methods

This study aims to integrate the XAJ and MCQRNN models for raising the accuracy and reliability of short-term FPD forecasts. Fig. 1 presents the main architectures utilized in this study: the MCQRNN (Fig. 1(a)); and the proposed XAJ-MCQRNN model that combines XAJ with MCQRNN models (Fig. 1(b)).

144 2.1 Monotone Composite Quantile Regression Neural Network (MCQRNN)

The MCQRNN has been developed to effectively estimate multiple quantile functions 145 for making probabilistic density forecasts of time series (Cannon, 2018). In comparison 146 147 to the Quantile Regression Neural Network (QRNN) (Taylor, 2000), the monotone QRNN (Cannon, 2011) and the composite QRNN (Xu et al., 2017), the merit of the 148 MCQRNN model is that it can estimate multiple non-crossing, non-linear conditional 149 quantile functions, can allow for the constraints of optional monotonicity, 150 positivity/non-negativity and generalized additive model, and can be applied to 151 estimating standard least-squares regression (Cannon, 2018). 152

The structure of the MCQRNN model is composed of input, hidden, and output layers (Fig. 1(a)). Regarding the *k*th quantile τ_k , the outputs of hidden and output layers in association with multi-input variables at horizon T are described below.

156
$$h_j(t+T) = f\left(\sum_{s=0}^T \widehat{P}(t+s) \cdot \exp\left(w_{sj}^{(h)}\right) + \sum_{m=0}^p P(t-m) \cdot \exp\left(w_{mj}^{(h)}\right) + \right)$$

157
$$\sum_{n=0}^{q} Q(t-n) \cdot w_{nj}^{(h)} + b_j^{(h)}$$
(1a)

$$\widehat{Q}_{\text{MCQRNN}}^{\tau_k}(t+T) = g\left[\sum_{j=1}^J h_j(t+T) \cdot \exp\left(w_{jk}^{(o)}\right) + b_k^{(o)}\right]$$
(1b)

159

158

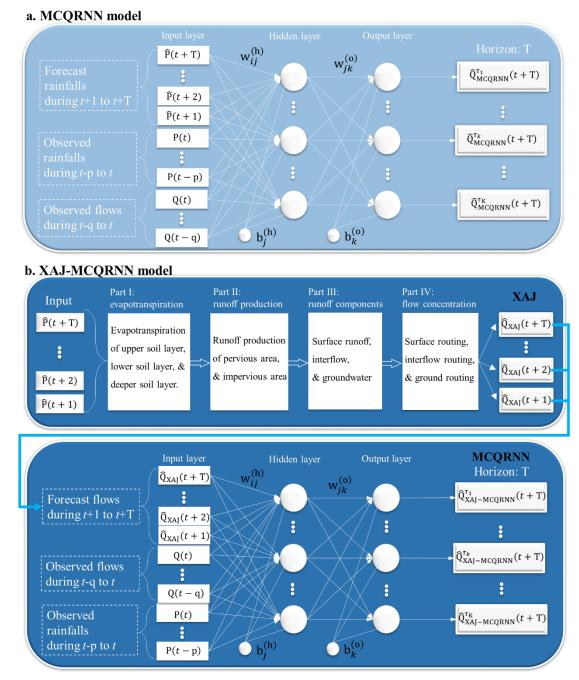


Fig. 1 Main architectures adopted in this study. a. Monotone composite QRNN model (MCQRNN). b. Proposed XAJ-MCQRNN model. $w_{ij}^{(h)}$, $b_j^{(h)}$, $w_{jk}^{(o)}$ and $b_k^{(o)}$ are the parameters in hidden and output layers of MCQRNN model. $\hat{Q}_{MCQRNN}(t + T)$ is the forecast streamflow of MCQRNN model at horizon t+T. $\hat{Q}_{XAJ}(t + 1),...,\hat{Q}_{XAJ}(t + T)$ are the forecast streamflows of XAJ model during horizons t+1 up to t+T. $\hat{Q}_{XAJ-MCQRNN}(t + T)$ is the forecast streamflow of XAJ-MCQRNN model with τ_k quantile at horizon t+T. t and T are the current time and forecast horizon, respectively.

169	where $h_j(t + T)$ and $\widehat{Q}_{MCQRNN}^{\tau_k}(t + T)$ are the <i>j</i> th node's output transformed from
170	input variables in the hidden layer and the model output with the τ_k quantile ($1 \le k \le K$)
171	in the output layer at horizon T, respectively. $\widehat{P}(t + s)$ is the forecast rainfall at
172	horizon s ($1 \le s \le T$). P($t - m$) and Q($t - n$) are the <i>m</i> th antecedent rainfall and the
173	<i>n</i> th antecedent streamflow, respectively. $f(\cdot)$ is the hyperbolic tangent function in the
174	hidden layer. $g(\cdot)$ is the sigmoid transfer function in the output layer. k and j are the
175	indexes of quantile and node, respectively. p and q are the numbers of antecedent
176	rainfall and antecedent streamflow variables at horizon T, respectively. $w_{sj}^{(h)}$ is the
177	weight parameter which connects the sth forecast rainfall and the <i>j</i> th node in the
178	hidden layer, where the superscript (h) represents the hidden layer. $w_{mj}^{(h)}$ and $w_{nj}^{(h)}$
179	are the weight parameters which connects the mth (nth) antecedent rainfall
180	(streamflow) input variable and the <i>j</i> th node in the hidden layer, respectively. $b_j^{(h)}$ is
181	the intercept parameter of the <i>j</i> th node in the hidden layer. $w_{jk}^{(o)}$ and $b_k^{(o)}$ are the <i>j</i> th
182	weight and the intercept parameter of the <i>k</i> th quantile in the output layer, respectively,
183	where the superscript (o) represents the output layer. J is the number of nodes.

To enhance the stability of model training, regularization terms are integrated into the error function to penalize the magnitude of the weight parameters within hidden and output layers, as described below.

187
$$\rho_{\tau_k}(\varepsilon) = \begin{cases} \tau_k \cdot \varphi(\varepsilon) & \varepsilon \ge 0\\ (\tau_k - 1) \cdot \varphi(\varepsilon) & \varepsilon \ge 0 \end{cases}$$
(2a)

188
$$\varphi(\varepsilon) = \begin{cases} \frac{\varepsilon}{2\alpha} & 0 \le |\varepsilon| \le \alpha \\ |\varepsilon| - \frac{\alpha}{2} & |\varepsilon| > \alpha \end{cases}$$
(2b)

189
$$\mathbf{E} = \sum_{k=1}^{K} \omega_{\tau_k} \cdot \sum_{t=1}^{D} \rho_{\tau_k} \left(\mathbf{Q}(t+T) - \widehat{\mathbf{Q}}_{\text{MCQRNN}}^{\tau_k}(t+T) \right)$$
(2c)

190
$$\widetilde{E} = E + \lambda^{(h)} \cdot \frac{1}{(T+p+q) \cdot J} \sum_{i=1}^{(T+p+q)} \sum_{j=1}^{J} \left(w_{ij}^{(h)} \right)^2 + \lambda^{(o)} \cdot \frac{1}{J} \sum_{j=1}^{J} \left(w_{jk}^{(o)} \right)^2$$
(2d)

where $\rho_{\tau_k}(\varepsilon)$ and $\varphi(\varepsilon)$ are the Huber-norm function (Chen, 2007) with the τ_k 191 quantile and the Huber function (Huber, 1964) with the variable ε , respectively. $|\varepsilon|$ 192 and α are the absolute error and the given positive value, respectively. The Huber 193 function transforms smoothly from the squared error, which is applied around the 194 origin (α) to accomplish differentiability, and the absolute error. ω_{τ_k} is the weight 195 that represents the contribution of the forecast streamflow with the τ_k quantile to the 196 total error. Q(t + T) is the observed streamflow. K is the number of quantiles. $\lambda^{(h)}$ 197 and $\lambda^{(0)}$ are the coefficients (i.e., regularization items) that denote the penalties 198 applied to the weight parameters in hidden and output layers, respectively. *i* is the 199 index of input variable. $w_{ij}^{(h)}$ is the weight parameter for connecting the *i*th input 200 201 variable and the *j*th node in the hidden layer. D is the number of input data. E and \tilde{E} are the error functions without (the former) and with (the latter) regularization items 202 considering the Huber-norm approximation, respectively. 203

In the case of the specified model architecture (i.e. three layers, shown in Fig. 1(a)) with the numbers of input variables (V), hidden nodes (J), and output variables (O), the total number of weight and intercept parameters in the MCQRNN model is the sum of $(V \times J + J \times O)$ weight parameters and (J + O) intercept parameters.

208 2.2 Xinanjiang (XAJ) conceptual hydrological model

The XAJ model is a conceptual rainfall-runoff model suitable for flood forecasts of humid and semi-humid catchments (Zhao, 1992). From the viewpoint of model architecture, the XAJ model has four implementation phases (Fig. 1(b)). Part I is to

compute evapotranspiration by three representative soil layers. Part II is to calculate 212 runoff production under runoff formation on repletion of storage. Part III is to separate 213 214 total runoff into the components of surface runoff, interflow and groundwater. Part IV is to compute flow concentrations by means of the Nash Unit Hydrograph and 215 216 Muskingum routing. The advantage of the XAJ model is that the model has not only 217 the explicit physical meaning of rainfall-runoff processes but also a simple manner for flood forecasting. The mathematical equation of the rainfall-runoff process in the XAJ 218 model during horizons t+1 up to t+T is depicted as follows. 219

220
$$\widehat{\mathbf{Q}}_{\mathbf{XAJ}}^{\mathrm{T}} = \phi [\widehat{P}(t+1), \widehat{P}(t+2), \cdots, \widehat{P}(t+T)]$$
(3a)

221
$$\widehat{\mathbf{Q}}_{\mathbf{X}\mathbf{A}\mathbf{J}}^{\mathrm{T}} = \left[\widehat{\mathbf{Q}}_{\mathbf{X}\mathbf{A}\mathbf{J}}(t+1), \widehat{\mathbf{Q}}_{\mathbf{X}\mathbf{A}\mathbf{J}}(t+2), \cdots, \widehat{\mathbf{Q}}_{\mathbf{X}\mathbf{A}\mathbf{J}}(t+\mathbf{T})\right]$$
(3b)

where $\widehat{\mathbf{Q}}_{\mathbf{X}\mathbf{A}\mathbf{J}}^{\mathbf{T}}$ is the vector of the XAJ model output with lead time T. $\widehat{\mathbf{P}}(t + T)$ and $\widehat{\mathbf{Q}}_{\mathbf{X}\mathbf{A}\mathbf{J}}(t + T)$ are the forecast rainfall (i.e., mode input) and flow (i.e., model output) at horizon *t*+T, respectively. $\boldsymbol{\Phi}[\cdot]$ is the transformation function of rainfall-runoff processes including four parts (Fig. 1(b)).

The XAJ model has 15 parameters, including 4 evapotranspiration parameters, 3 runoff production parameters, 4 runoff separation parameters, and 4 flow concentration parameters. Owing to the effectiveness and practicality, the Shuffled Complex Evolution method developed at The University of Arizona (SCE-UA) (Duan et al., 1994) was adopted to optimize the XAJ model parameters in this study. More details on the XAJ model can be found in Zhao (1992).

232 2.3 Hybridization of the XAJ and MCQRNN (XAJ-MCQRNN)

233 The comparison between MCQRNN (Fig. 1(a)) and XAJ-MCQRNN (Fig. 1(b)) models

established in this study is summarized as follows: when making FPD forecasts, the former adopts the forecast rainfall data ($\hat{P}(t + 1), \hat{P}(t + 2), \dots, \hat{P}(t + T)$) provided by available numerical forecast products as input variables to test the model during horizons *t*+1 up to *t*+T, while the latter adopts the forecast streamflow data $\hat{Q}_{XAJ}(t + 1), \hat{Q}_{XAJ}(t + 2), \dots, \hat{Q}_{XAJ}(t + T)$ made by the XAJ model during horizons *t*+1 up to *t*+T as input variables to test the model.

From the perspective of model complementarity, the XAJ model can produce stable point forecasts of flood hydrographs so that the MCQRNN model can create more accurate and reliable FPD forecasts after being supplied with point forecasts by the XAJ model. The general equation of the proposed hybrid model for the quantile τ_k is described below.

245
$$\widehat{Q}_{XAJ-MCQRNN}^{\tau_k}(t+T) = \psi [\widehat{Q}_{XAJ}(t+T), \cdots, \widehat{Q}_{XAJ}(t+2), \widehat{Q}_{XAJ}(t+1), Q(t),$$

(4)

246
$$Q(t-1), \cdots, Q(t-q), P(t), P(t-1), \cdots, P(t-p)$$

where $\widehat{Q}_{XAJ-MCQRNN}^{\tau_k}(t + T)$ is the forecast streamflow of the XAJ-MCQRNN model with the quantile τ_k at horizon t+T. $\psi[\cdot]$ is the quantile regression function that is the combination of the hyperbolic tangent function $f(\cdot)$ in the hidden layer and the sigmoid transfer function $g(\cdot)$ in the output layer.

251 2.4 Training process of the MCQRNN model

The gradient-based nonlinear optimization algorithm (Kingma and Ba, 2015; Cannon, 2018) was used to optimize the weight $(w_{sj}^{(h)}, w_{mj}^{(h)}, w_{nj}^{(h)})$ and $w_{jk}^{(o)}$ in Eqs. 1(a) and 1(b)) and intercept $(b_j^{(h)})$ and $b_k^{(o)}$ in Eqs. 1(a) and 1(b)) parameters of the MCQRNN while the training process of the XAJ-MCQRNN was performed after being supplied with point forecasts by the XAJ at the same time. Furthermore, the Genetic Algorithm (GA) (Goldberg and Deb, 1991; Zhou et al., 2019) was used to optimize the hyperparameters (the maximal iteration I_{max} , the number of nodes J, the regulation coefficients $\lambda^{(h)}$ and $\lambda^{(o)}$, and the learning rate η). Fig. 2 illustrates the flow chart of the XAJ-MCQRNN training process. The implementation procedure is described as follows.

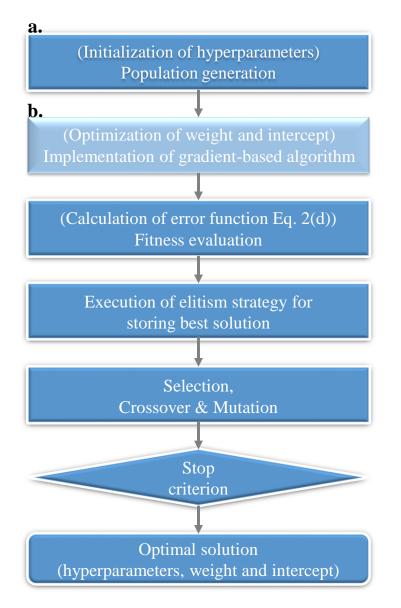
Step 1: Randomly generate an initial population X_0 of size I_{pop} with respect to the hyperparameters. Integer-coded and real-coded solutions are adopted for hyperparameters I_{max} and J as well as for hyperparameters $\lambda^{(h)}$, $\lambda^{(o)}$ and η , respectively. The search spaces of I_{max} , J, $\lambda^{(h)}$, $\lambda^{(o)}$ and α are set to be [200, 500], [1, 30], [0.001, 0.01], [0.001, 0.01] and [0.001, 0.05], respectively.

Step 2: Perform the gradient-based nonlinear optimization algorithm for optimizing
 weight and intercept parameters of the MCQRNN model, and execute the
 tournament selection, the crossover operator with probability (P_c) and the mutation
 operator with probability (P_m) to create an offspring population Y₀ of size I_{pop}.

Step 3: Evaluate the fitness values of Y_u for the *u*th generation, combine Y_{u-1} and Y_u into an intermediate population X_u of size $2 * I_{pop}$, partition this combined population into different ranks according to fitness values, and store the best solution using the elitism strategy.

Step 4: Implement the tournament selection to select a new parent population X_{u+1} of
size I_{pop} from X_u, create an offspring population Y_{u+1} using crossover and mutation
operators, and evaluate their fitness values.

- 278 Step 5: Repeat Steps 3 and 4 when the generation number *u* is smaller than the maximal
- 279 generation (G_{max}). Otherwise, output the optimal results after stopping iteration.



280

Fig. 2 Flow diagram of the XAJ-MCQRNN model trained simultaneously by: a. the Genetic Algorithm applied to the optimization of hyperparameters; b. the gradientbased nonlinear optimization algorithm applied to the optimization of weight and intercept parameters.

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In this study, the population size (I_{pop}), the maximal generation (G_{max}), the
crossover probability (P<sub>c</sub>) and the mutation probability (P<sub>m</sub>) of GA were set to be 200,
100, 0.85 and 0.1, respectively. The aforementioned computations regarding the GA,
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XAJ model and MCQRNN model are conducted in R software (<u>https://www.r-</u>
 project.org/), where the computation of the MCQRNN is based on the freely available
 QRNN package (https://CRAN.R-project.org/package=qrnn).

As river streamflow data are time series, this study applied the Root Mean Square 292 Error (RMSE), the Nash-Sutcliffe Efficiency (NSE) and the Mutual Information (MI) 293 to evaluate the point forecast results of the two MCQRNN models. The RMSE value 294 indicates the error between forecasts and observations, and its value ranges from 0 to 295 infinity (Legates and McCabe, 1999). The NSE is commonly employed to evaluate the 296 297 forecast accuracy of hydrological models and its value ranges from negative infinity to 1 (Nash and Sutcliffe, 1970). Considering that the upper bound (=1) of the NSE doesn't 298 leave much room for improvement, a logarithm conversion for the NSE (LNSE) is used 299 300 instead of an unbounded quality indicator to evaluate model accuracy. The MI value suggests the goodness-of-fit between forecasts and observations, and its value ranges 301 from 0 to infinity (Shannon, 1948). A model with low RMSE and high LNSE and MI 302 303 values suggests it can produce high forecast accuracy. The computations of RMSE, LNSE and MI values are described below. 304

305
$$RMSE = \sqrt{\frac{1}{D} \sum_{t=1}^{D} \left(Q(t+T) - \widehat{Q}_{Model}^{\tau_k}(t+T) \right)^2}$$
(5)

306
$$LNSE = -\ln(1 - NSE) = -\ln(\frac{\sum_{t=1}^{D} \left(Q(t+T) - \widehat{Q}_{Model}^{\tau_{k}}(t+T)\right)^{2}}{\sum_{t=1}^{D} \left(Q(t+T) - \overline{Q}_{T}\right)^{2}})$$
(6)

307
$$\mathbf{MI} = \sum_{t=1}^{D} \sum_{t=1}^{D} p\left(\mathbf{Q}(t+T), \widehat{\mathbf{Q}}_{\text{Model}}^{\tau_k}(t+T)\right) \log_2\left(\frac{p\left(\mathbf{Q}(t+T), \widehat{\mathbf{Q}}_{\text{Model}}^{\tau_k}(t+T)\right)}{p\left(\mathbf{Q}(t+T)\right)f\left(\widehat{\mathbf{Q}}_{\text{Model}}^{\tau_k}(t+T)\right)}\right)$$
(7)

where $\widehat{Q}_{Model}^{\tau_k}(t+T)$ is the forecast value of a model (MCQRNN or XAJ-MCQRNN) with the τ_k quantile at horizon T. \overline{Q}_T is the average of observed values at horizon T. 310 $p(\cdot, \cdot)$ is the joint probability density function of observations and forecasts. $p(\cdot)$ is the 311 probability density function of observations or forecasts. The median (i.e., $\tau_k=0.5$) 312 forecasts of a model are commonly employed to evaluate the prediction accuracy of 313 point forecast results (Zhou et al., 2020).

The Coverage Ratio (CR) of the forecast interval relative to observations and the 314 Relative Bandwidth (RB) of the forecast interval (Xiong and O'Connor, 2008) were 315 used to evaluate the accuracy of the forecast interval results in this study. The CR 316 represents the coverage interval of the forecasts and its value ranges from 0 to 100%. 317 318 The RB represents the width of the forecast interval and its value ranges from 0 to infinity. A model with its CR value closer to 100% and its RB closer to 0 implies it can 319 forecast more accurately. The computations of CR and RB values are depicted as 320 321 follows.

322
$$CR = \frac{1}{D} \times \sum_{t=1}^{D} \theta_t \times 100\%, \quad \theta_t = \begin{cases} 1, & Q(t+T) \in \left[\widehat{Q}_L(t+T), \widehat{Q}_U(t+T)\right] \\ 0, & Q(t+T) \notin \left[\widehat{Q}_L(t+T), \widehat{Q}_U(t+T)\right] \end{cases}$$
(8)

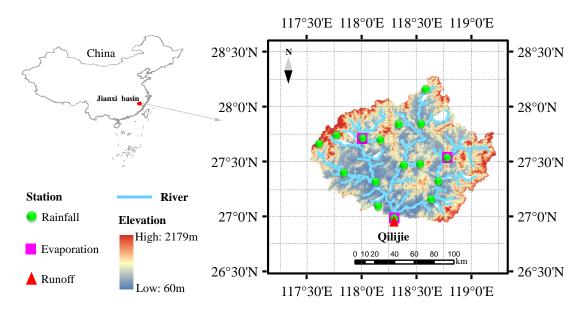
where $\hat{Q}_L(t + T)$ and $\hat{Q}_U(t + T)$ are the lower and upper boundaries of forecast interval results at horizon T with respect to a given confidence level (e.g. 90%), respectively (e.g. L=5%, U=95%). The θ_t values are either one or zero, in which one implies the observed data fall within its forecast intervals while zero implies the observed data fall outside of its forecast intervals at *t* time.

329

330 **3** Study area and materials

331 3.1 Study area

The Jianxi River catchment with an area of 14787 km² is located in southern China (Fig. 332 3). The catchment climate is affected by the southwest Indian Ocean and southeast 333 334 Pacific Ocean subtropical monsoons and regional landforms (Lin et al., 2020). The annual rainfall ranges from 1800 mm to 2200 mm and the annual runoff ranges from 335 950 to 1700 mm, the highest amount (74%) of which occurs within six months 336 (April-September). Due to the moist and rainy features as well as red, yellow, and 337 paddy soils, runoff production of this catchment is dominated by the runoff generation 338 on repletion of storage, which is in line with the typical rainfall-runoff characteristics 339 340 in southern China.



341

Fig. 3 Locations of the Jianxi River catchment and hydro-meteorological (rainfall,
evaporation and runoff) gauge stations.

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345 3.2 Materials
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This study collected the data associated with flood events during the flood season (April 1st–September 30th), including the 3-hour (time step) rainfall data of 16 gauge stations, the 3-hour evaporation of 3 gauge stations and the 3-hour streamflow data of

³⁴⁴

the Qilijie hydrological station from 2009 to 2015, and the 3-hour forecast rainfall of 349 ERA-Interim datasets of the European Centre for Medium-Range Weather Forecasts 350 351 (ECMWF) from 2014 to 2015. The spatial resolution of each grid in ERA-Interim is 0.125°E×0.125°N, while 32 grid points are required to fully cover the Jianxi River 352 catchment (Fig. 3). More details on the ERA-Interim datasets of the ECMWF can be 353 found in Berrisford et al. (2011). The areal mean value of observed rainfall data was 354 calculated by using the datasets of 16 gauge stations colored in green (Fig. 3), the areal 355 mean value of observed evaporation data was calculated by using the datasets of 3 356 357 gauge stations colored in purple (Fig. 3), and the areal mean value of forecast rainfall data was calculated by using the datasets of 32 grid points through the Thiessen polygon 358 method (Thiessen, 1911). 359

A total of 20448 (=8 time step × 365 days × 6 non-leap years + 8 time step × 366 days × 1 leap year) time series values were divided into three datasets for model training (8760 from 2009-2011), validation (5848 from 2012-2013), and testing (5840 from 2014-2015). The training dataset was applied to adjusting the parameters (weights and intercepts) of the XAJ model (the MCQRNN model). The validation dataset was applied to checking whether a prediction model is overfitted or undertrained. The test dataset was applied to evaluating the model prediction accuracy.

367 3.3 Model construction

A 12-hour forecast horizon has been considered in this study since the longest transform time in the rainfall-runoff processes is 12 hours in this catchment. Besides, the current forecast horizon at the Qilijie station is only 6 hours, inducing the demand for improving the lead time and forecast accuracy. In the light of the observed 3-hour rainfall-runoff datasets of the Jianxi River catchment, the model output was set to be t+1 (Horizon=3 hours) up to t+4 (Horizon=12 hours) time-step-ahead streamflow, where *t* is the current time.

As aforementioned, the GA was performed to determine the optimal hyperparameters in association with MCQRNN models at four horizons. The optimal values of the maximal iteration (I_{max}), the number of nodes (J), the regulation coefficients ($\lambda^{(h)}$ and $\lambda^{(o)}$) and the learning rate (η) were 300, 12, 0.006, 0.004 and 0.009, respectively, while the weight and intercept parameters optimized by the gradient-based nonlinear optimization algorithm within the QRNN package were adopted in this study.

This study adopted the Partial Mutual Information and Partial Weights (PMI-PW) 382 method (Sharma et al., 2016) to quantify the contribution of input combination to model 383 performance (Table 1). To estimate the input variables weights for constructing the 384 385 MCQRNN and XAJ-MCQRNN models, the following framework was adopted. Apart from the observed streamflow and rainfall data (traced back to the previous 12 hours), 386 the rainfall of the ERA-Interim during horizon t+1 up to t+4 was used to train, validate 387 and test the former, while the forecast streamflow of the XAJ model during horizon t+1388 up to t+4 was used to train, validate and test the latter. 389 390

Table 1 Weights of input variables for constructing models by the Partial Mutual Information and Partial Weights (PMI-PW) method

combination Horizon $t+1$ Horizon $t+2$ Horizon $t+3$ Horizon $t+4$	Variable	Input	Contribution				
	Variable	combination	Horizon $t+1$	Horizon $t+2$	Horizon $t+3$	Horizon <i>t</i> +4	

		MCQRNN	XAJ-	MCQRNN	XAJ-	MCQRNN	XAJ- MCQRNN	MCQRNN	XAJ-
			MCQRNN		MCQRNN				MCQRNN
Rainfall	P(<i>t</i> +4)							0.03	
	P(<i>t</i> +3)					0.04		0.06	
	P(<i>t</i> +2)			0.05		0.06		0.08	
	P(<i>t</i> +1)	0.05		0.06		0.09		0.10	
	$\mathbf{P}(t)$	0.07	0.07	0.09	0.08	0.11	0.09	0.17	0.15
	P(<i>t</i> -1)	0.09	0.09	0.11	0.11	0.15	0.14	0.09	0.10
	P(<i>t</i> -2)	0.12	0.10	0.17	0.13	0.08	0.09	0.06	0.06
	P(<i>t</i> -3)	0.18	0.14	0.08	0.09	0.04	0.04	0.02	0.05
Forecast	$\widehat{Q}_{XAJ}(t+4)$								0.25
streamflow	$\widehat{Q}_{XAJ}(t+3)$						0.23		0.19
of XAJ model	$\widehat{\mathbf{Q}}_{\mathrm{XAJ}}(t+2)$				0.22		0.17		0.10
	$\widehat{\mathbf{Q}}_{XAJ}(t+1)$		0.20		0.14		0.11		0.06
Observed	Q(<i>t</i>)	0.20	0.18	0.21	0.11	0.24	0.09	0.25	0.04
streamflow	Q(<i>t</i> -1)	0.15	0.09	0.13	0.08	0.12	0.04	0.09	
	Q(<i>t</i> -2)	0.09	0.07	0.07	0.04	0.05		0.04	
	Q(<i>t</i> -3)	0.05	0.06	0.03		0.02		0.01	
Su	ım	1	1	1	1	1	1	1	1

393

394 **4 Results**

To improve the predictability and reliability of FPD forecasts, this study intends to explore and evaluate the accuracy of the XAJ model coupled with the MCQRNN on short-term (12 hours) flood forecasts at different horizons. The results, findings and discussion were as follows.

399 4.1 Reliability of XAJ and MCQRNN models on point forecasts of flood processes

The point forecasts of floods under the circumstance of the quantile τ_k =0.5 (i.e. median forecasts) were specified to test the reliability of the constructed models. Table 2 summarizes the RMSE, LNSE and MI values of the XAJ, MCQRNN and XAJ-MCQRNN models in training, validation and testing stages at four horizons. It is apparent from this table that the XAJ-MCQRNN model performs better than the XAJ and MCQRNN models in the three stages at four horizons. Take the testing stage for example, the LNSE and MI values of the XAJ-MCQRNN model exceed 0.90 and 22
respectively while the RMSE values are less than 140 m³/s.

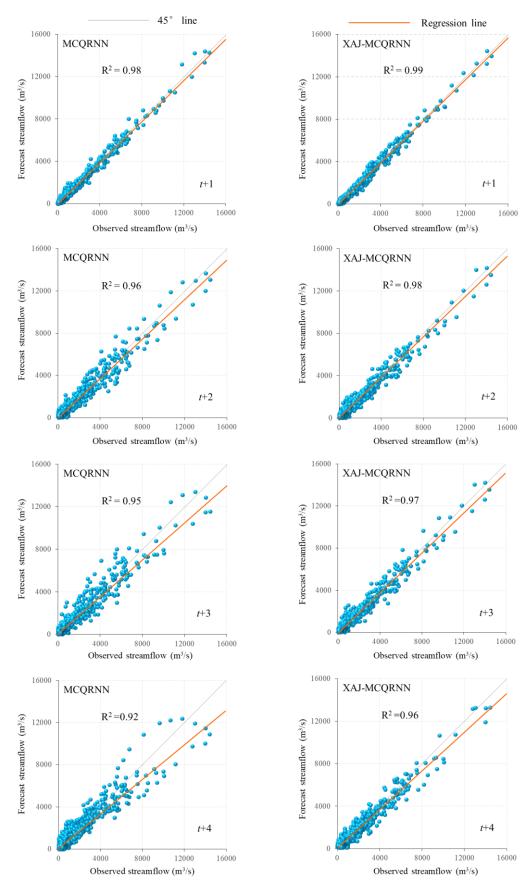
408	Two main results are acquired from the Table 2. Firstly, the comparison of the XAJ-
409	MCQRNN and XAJ models in the testing stage reveals that there are significant
410	differences in the improvement rates of RMSE and NSE values at four horizons. The
411	improvement rates of RMSE (LNSE & MI) for median flood forecasting reach 4.7%
412	(9.0% & 4.3%) and 5.2% (17.0% & 6.1%) at horizons t+1 and t+2, respectively, while
413	they increased to 6.6% (22.2% & 8.8%) and 8.1% (28.4% & 11.2%) at horizons t+3
414	and t+4, respectively. Secondly, the comparison of the XAJ-MCQRNN and MCQRNN
415	models in the testing stage points out that the former can provide stable forecast results
416	after being supplied with point forecasts by the XAJ model either at shorter horizons
417	(t+1 and t+2) or at longer horizons $(t+3 and t+4)$. That is to say, the XAJ-MCQRNN
418	model can effectively extract the dependence between rainfall and runoff processes
419	even in the case of the12-hour forecast horizon. The fluctuations of forecast rainfalls
420	are stronger at long horizons ($t+3$ and $t+4$) than at short horizons ($t+1$ and $t+2$). Higher
421	fluctuations of forecast rainfall data are easy to induce overfitting problems, which
422	would demand more complex models to mimic the relationship between rainfall and
423	runoff. This is considered as a driver to improve the forecast of the XAJ-MCQRNN
424	model.
425	
426	
427	
428	and Mutual Information (MI) values acquired from the XAJ, MCQRNN and XAJ-
429	MCQRNN models in training, validation and testing stages
<u>ao</u>	Horizon $PMSE(m^{3}/s)$ INSE MI

Stage	Horizon	RMSE (m^3/s)	LNSE	MI
	-			

		XAJ	MCQRNN	XAJ- MCQRNN	XAJ	MCQRNN	XAJ- MCQRNN	XAJ	MCQRNN	XAJ- MCQRNN
Training	<i>t</i> +1		71	68		3.91	3.91		1.87	1.94
	<i>t</i> +2	01	89	84	2 22	3.51	3.51	1 75	1.79	1.90
	<i>t</i> +3	91	115	106	3.22	3.00	3.22	1.75	1.68	1.85
	<i>t</i> +4		137	124		2.53	2.81		1.54	1.78
Validation	<i>t</i> +1		77	73		3.51	3.51		1.85	1.93
	<i>t</i> +2	102	94	88	3.00	3.22	3.51	1.72	1.78	1.91
	<i>t</i> +3	102	121	111	5.00	2.66	3.00	1.72	1.69	1.84
	<i>t</i> +4		146	130		2.41	2.81		1.60	1.77
Testing	<i>t</i> +1	84	90	80 (4.7)*	3.22	3.22	3.51 (9.0)	1.85	1.85	1.93 (4.3)
	<i>t</i> +2	96	103	91 (5.2)	3.00	3.00	3.51 (17.0)	1.79	1.74	1.90 (6.1)
	<i>t</i> +3	122	131	114 (6.6)	2.41	2.30	2.81 (22.2)	1.70	1.67	1.85 (8.8)
	<i>t</i> +4	149	168	137 (8.1)	2.12	1.97	2.53 (28.4)	1.61	1.56	1.79 (11.2)
430			r in the brack	ket is the impr	roveme	nt rate of the 2	XAJ-MCQRNN	M model	over the XAJ	
431	mode	1.								
432										
433		To furtl	her evaluate	the forecast	accur	acy of MCQ	RNN models	for mak	ting median	
434	forec	asts of	floods, the	regression a	nalysis	of the obser	rved and forec	ast strea	mflow data	
435	is pro	esented	l in Fig. 4. I	t is too hard	l to ju	dge the diffe	rence in mod	el quali	ty when the	
436	corre	correlation between observations and forecasts is high. However, this is different for								
437	the c	the case of low correlation, where the gap between the regression and 45-degree lines								
438	is la	is large. A large gap denotes a significant biased-prediction. From the standpoint of								
439	corre	correlation (Fig. 4), the XAJ-MCQRNN model can more adequately alleviate the								
440	biase	biased-prediction phenomenon (under-prediction in our case) because of the larger								
441	value	values of the coefficient of determination R^2 as well as the smaller gaps between the								
442	regression and 45-degree lines, compared to the MCQRNN model. As expected, there									
443	are h	nigher	correlations	between of	oservat	tions and for	recasts at hor	rizons <i>t</i> -	+1 and <i>t</i> +2,	
444	wher	eas lar	ger improv	ements of the	he cor	relation betw	ween observa	tions ar	nd forecasts	
445	occu	r at hoi	rizons $t+3$ and	nd <i>t</i> +4.						
	, ,	T1 1			.1	1				

The hybrid model still consistently underestimates most flood processes (Fig. 4).

The back-fitting algorithm with the autoregressive strategy (Zhang et al., 2018) was 447 performed to correct the systematic bias of point forecasts of the hybrid model. After 448 implementing bias-correction, Table 3 summarizes the Kolmogorov-Smirnov (KS) test 449 results from the standpoint of density distribution. Due to the high variation of flood 450 datasets (streamflow value $\geq 1000 \text{ m}^3/\text{s}$), the observations at each horizon are divided 451 into three parts (Part I: 1000 m³/s \leq value < 3000 m³/s; Part II: 3000 m³/s \leq value < 452 9000 m³/s; and Part III: value \geq 9000 m³/s) to effectively examine the predictability of 453 the proposed model at various flood magnitudes. The larger KS test indicator values 454 455 suggest smaller difference between observed and forecast distributions and better model performance. Interestingly, the XAJ-MCQRNN model creates a pretty good 456 similarity between observed and forecast distributions of the three parts at all horizons 457 458 whereas the MCQRNN model only performs well when flood magnitudes are small (Part I). From the table, we can see that the probability density distribution of the 459 forecasts acquired from the XAJ-MCQRNN model is more similar in shape to that of 460 observations at each horizon. In other words, the values of the forecasts obtained from 461 the XAJ-MCQRNN model in three parts are closer to those of observations, in 462 comparison to the forecasts obtained from the MCQRNN model. The results 463 demonstrate that the XAJ-MCQRNN model can not only sufficiently forecast the 464 probability density distribution of flood data but also accurately forecast different flood 465 magnitudes at four horizons. 466



468 Fig. 4 Regression analysis between the observed streamflow data and the median469 forecasts of streamflow data in the testing stage at four horizons.

		KS test indicator*					
Model	Horizon	Part I: 1000 m³/s≤value<3000 m³/s	Part II: $3000 \text{ m}^3/\text{s} \leq \text{value} < 9000$ m^3/s	Part III: value≥9000 m³/s			
	<i>t</i> +1	0.03	0.06	0.08			
MCQRNN	<i>t</i> +2	0.03	0.07	0.10			
WCQKINN	<i>t</i> +3	0.04	0.10	0.13			
	<i>t</i> +4	0.05	0.13	0.15			
	<i>t</i> +1	0.01	0.03	0.06			
XAJ-	<i>t</i> +2	0.01	0.04	0.06			
MCQRNN	<i>t</i> +3	0.02	0.06	0.08			
	<i>t</i> +4	0.03	0.07	0.09			

Table 3 Kolmogorov Smirnov (KS) test results of the two distributions of observations
and forecasts in three parts for each given horizon at the testing stage

*The KS test is performed at a significance level of 0.05. The null hypothesis states that the
probability density distribution of forecasts is similar in shape to that of observations. If the value
of the KS test indicator is smaller than the value of D(n, 0.05) (=0.05, 0.09 and 0.11 for the Part I,
II and III, respectively), the null hypothesis would not be rejected.

In brief, the point (i.e., median) forecasts of floods made by the XAJ-MCQRNN model offered solid evidence of good model performance and favorable stability in multi-step-ahead flood forecasting. The next subsection is concerned with the comparison of the MCQRNN and XAJ-MCQRNN models for making interval forecasts of floods.

482 4.2 Reliability of MCQRNN models on interval forecasts of flood processes

The interval forecasts of floods for the case of the quantiles $(0.01 \le \tau_k \le 0.99)$, with an increment of 0.01) were employed to test the reliability of the two models (MCQRNN and XAJ-MCQRNN). The back-fitting algorithm with the autoregressive strategy (Zhang et al., 2018) was also executed to correct the systematic bias of interval forecasts of the hybrid model. Table 4 provides the RB and CR values of the MCQRNN and XAJ-MCQRNN models in three stages at four horizons. The results indicate that

489	the XAJ-MCQRNN model acquires pretty good forecast accuracy at all the horizons
490	whereas the MCQRNN model only performs well at shorter horizons of $t+1$ and $t+2$
491	(CR is higher than 92%, but RB is lower than 12%). For 12-hour forecasts, the XAJ-
492	MCQRNN model can enhance the CR value by 1.5% up to 5.9% and decrease the RB
493	values by 8.8% up to 25.7% in the testing stages, as compared with the MCQRNN
494	model. This means the XAJ-MCQRNN model can not only significantly improve
495	probabilistic forecast accuracy in terms of a narrow prediction interval (as represented
496	by CR values) but also adequately eliminate the impacts of flood magnitudes on the
497	bandwidth of the prediction intervals (as represented by RB values). The 12-hour
498	forecast accuracy of the XAJ-MCQRNN model is superior to that of the MCQRNN
499	model since the XAJ-MCQRNN model utilizes the streamflow forecasts made by the
500	XAJ model to reduce the uncertainties of the rainfall forecasts from the ECMWF,
501	whereas the MCQRNN model adopts the rainfall forecasts of the ECMWF to make
502	multi-step-ahead flood forecasts in testing stages.
502	

Table 4 Results of Coverage Ratio (CR) and Relative Bandwidth (RB) values acquired
 from the MCQRNN and XAJ-MCQRNN models in training, validation and testing
 stages at four horizons

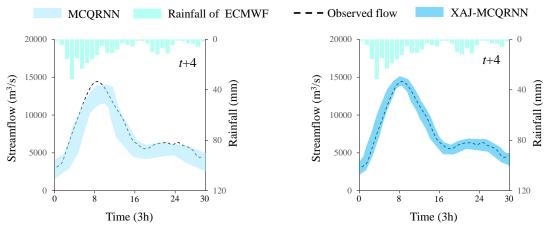
C to go	Homizon	R	AB (%)	CR (%)		
Stage	Horizon -	MCQRNN	XAJ-MCQRNN	MCQRNN	XAJ-MCQRNN	
	<i>t</i> +1	4.91	4.49 (8.5)*	95.17	96.98 (1.9)	
Tasiains	<i>t</i> +2	8.62	7.77 (9.9)	93.83	95.99 (2.3)	
Training	<i>t</i> +3	12.56	11.20 (10.8)	90.60	94.04 (3.8)	
	t+4	17.24	15.05 (12.7)	87.72	91.67 (4.5)	
	<i>t</i> +1	6.55	6.02 (8.1)	94.93	96.45 (1.6)	
V-1: 1 -4:	<i>t</i> +2	10.10	9.15 (9.4)	93.26	95.31 (2.2)	
Validation	<i>t</i> +3	14.81	13.34 (9.9)	90.09	93.33 (3.6)	
	t+4	19.37	16.62 (14.2)	86.36	90.07 (4.3)	
Testing	<i>t</i> +1	8.16	7.44 (8.8)	94.32	95.73 (1.5)	
	<i>t</i> +2	11.65	10.01 (14.1)	92.79	94.74 (2.1)	

<i>t</i> +3	16.00	13.07 (18.3)	89.56	92.87 (3.7)
<i>t</i> +4	23.33	17.33 (25.7)	84.43	89.41 (5.9)

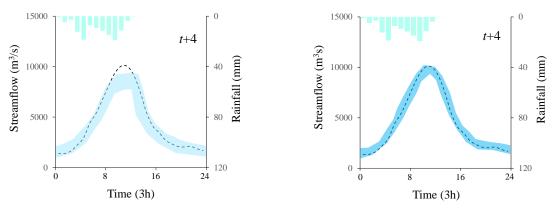
* The number in the bracket is the improvement rate of the XAJ-MCQRNN model over the MCQRNN model.
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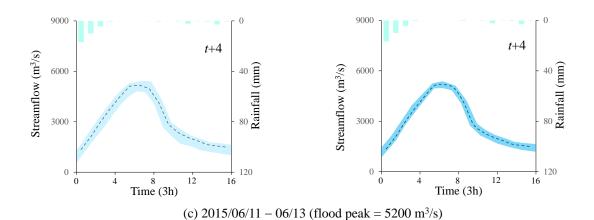
510	Moreover, to clearly determine the predictabilities of the MCQRNN and XAJ-
511	MCQRNN models, the three flood events: (a) high flood magnitude with total
512	precipitation of 134 mm and maximal streamflow of 14400 m^3/s (maximum streamflow
513	with a return period of 45a); (b) medium flood magnitude with total rainfall of 60 mm
514	and maximal streamflow of 10100 m^3/s (the return period of this peak is 20a); and (c)
515	low flood magnitude with total rainfall of 26 mm and maximal streamflow of 5200 $m^3\!/\!s$
516	(the return period of this peak is 10a), were selected to examine both models by
517	assessing whether the observed streamflow data fall within the 90% prediction interval,
518	i.e. [5% quantile, 95% quantile], at horizon $t+4$ in testing stages, as illustrated in Fig. 5.
519	Three interesting results are acquired. First, the 90% prediction intervals made by the
520	XAJ-MCQRNN model can cover the majority of the observed streamflow data, in
521	comparison to those of the MCQRNN model. Second, the XAJ-MCQRNN model can
522	create a predictive distribution narrower than that of the MCQRNN model in each flood
523	event. Third, the XAJ-MCQRNN model can largely mitigate the biased-prediction
524	phenomenon (under-prediction in our case). The prediction interval aims to promote
525	the sharpness of the predictive distributions as much as possible, where sharpness is
526	used to represent the concentration of the predictive distributions. Concerning short-
527	term forecasts, the XAJ-MCQRNN model can raise the concentration of the predictive
528	distributions while obtaining high coverage of the observed streamflow data in all cases.



(a) 2014/06/19 - 06/22 (flood peak = $14400 \text{ m}^3/\text{s}$)



(b) 2014/05/21 - 05/24 (flood peak = $10100 \text{ m}^3/\text{s}$)





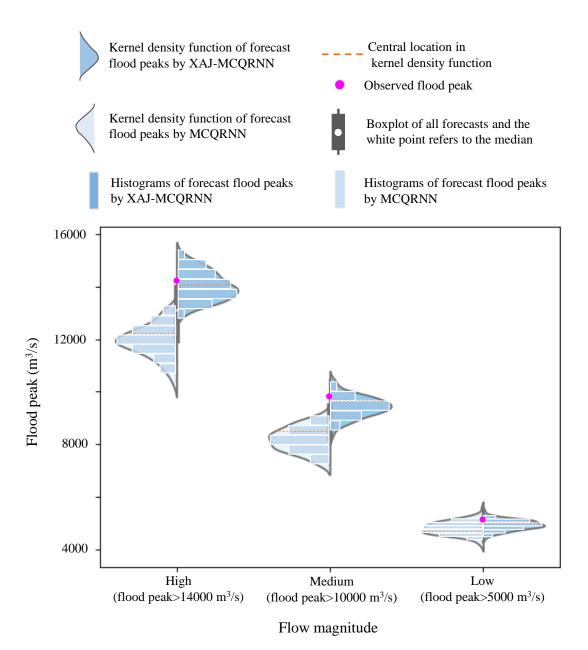
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532

Fig. 5 Interval forecast results of three flood events at horizon t+4 in the testing stages, given a 90% prediction interval of [5% quantile, 95% quantile]. The rainfall forecasts during horizons t+1 up to t+4 were collected from the ERA-Interim datasets of the

533 ECMWF. Left panel for MCQRNN, and right for XAJ-MCQRNN.

The density distribution (i.e., violin plot) is also adopted to evaluate the reliability 534 of interval forecasts. Fig. 6 illustrates the predictive violin-plots of the flood peaks of 535 536 the above-specified flood events at horizon t+4 in testing stages. In each violin plot, the probability density distribution of the forecasts made by the MCORNN (XAJ-537 MCQRNN) model is located at the left (right) part, while the statistical boxplot of all 538 forecasts is located at the central part. The violin plots point out that the difference 539 between the forecasts acquired from MCQRNN and XAJ-MCQRNN models displays 540 a trend climbing from the low, the medium to the high values of flood peaks at horizon 541 542 t+4. The bandwidths of the prediction intervals are notably larger in the medium-high flood peaks than in the low flood peak due to the larger fluctuations of flood magnitudes 543 in the former. Interestingly, the range of kernel density functions corresponding to the 544 545 XAJ-MCQRNN model is significantly narrower than that of the MCQRNN model while the central locations (orange dashed lines) of kernel density functions related to 546 the XAJ-MCQRNN model are closer to the observed flood peaks (purple points) in all 547 cases. That means the XAJ-MCQRNN model produces higher sharpness and 548 predictions with smaller bias than the MCQRNN model. Briefly, the XAJ-MCQRNN 549 model not only can produce more accurate and reliable probability density forecasts but 550 also can alleviate the biased-prediction phenomenon associated with the extreme flood 551 events through integrating the data-driven and conceptual-based mechanisms for 552 rainfall-runoff modelling. 553



554

Fig. 6 Violin plots for evaluating the uncertainty of MCQRNN and XAJ-MCQRNN model forecasts on flood peaks of high, medium and low flood magnitudes at horizon t+4 in the testing stages.

558

559 5 Conclusions and discussion

The demand for the hybridization of machine learning and conceptual models is motivated by real-world applications in the best interests of enhancing the accuracy and reliability of short-term FPD forecasting. This study proposed a hybrid rainfall-runoff model (i.e., XAJ-MCQRNN) that integrated the Xinanjiang (XAJ) conceptual model and the MCQRNN to make short-term FPD forecasts. Its capability of efficient learning
and accurate forecasting is tested and verified with the long-term (2009-2015) flood
events at the Jianxi River catchment in China. The MCQRNN model is constructed and
used for comparison purpose.

The results of median point forecasts on flood processes reveal that the proposed 568 XAJ-MCQRNN model performs distinguishably better than the MCQRNN model in 569 short-term (12 hours) flood forecasting with higher NSE and lower RMSE values as 570 well as a better goodness-of-fit to observed flood processes. The results of interval 571 572 forecasts of flood processes further demonstrate that the XAJ-MCQRNN model is superior to the MCQRNN model at four horizons. The XAJ-MCQRNN model has 573 smaller RB, larger CR values, and higher sharpness of the predictive distribution. These 574 575 achievements provide solid evidence that the XAJ-MCQRNN model can make considerably more reliable and accurate point and interval forecasts of flood processes 576 at long forecast horizons and can more effectively overcome the phenomena of 577 overfitting and time-shift than the MCQRNN model. Moreover, the reason that the 578 XAJ-MCQRNN model is successful in obtaining superb probability density forecast 579 results is attributed to the pivotal strategy that the XAJ conceptual model supplements 580 the point forecasts of flood processes through training the MCQRNN model to alleviate 581 predictive uncertainty. 582

Therefore, the XAJ-MCQRNN by virtue of data-driven and conceptual-based hydrological models can provide forecasting and early warning of flood processes, thus reducing flood risks associated with the extreme rainstorm phenomenon. This study is

a good demonstration of the hybrid approach which unites two different groups of 586 scientists including data scientists and disciplinary scientists (e.g., hydrologists). To use 587 588 the strength of various point forecasts meanwhile alleviating their weaknesses, model combinations in the form of hybridization (e.g., Zhang et al., 2018; Lin et al., 2020; 589 Hosseiny et al. 2020; Konapala et al., 2020; Kao et al., 2021) have been applied to 590 making short-term flood point forecasts for basins with humid subtropical climate. This 591 is the first study to apply conceptual models with artificial neural networks for flood 592 probability density (FDP) forecasting for such basins. Notwithstanding these promising 593 594 achievements, further research can be conducted to investigate the far-reaching effects of short-term and even long-term flood probability forecasting and warning on flood 595 prevention and water resources management in humid, semi-humid and arid areas by 596 597 combining more hybrid modelling techniques with medium-long term weather forecast products. 598

599

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Abstract

Making accurate and reliable probability density forecasts of flood processes is fundamentally challenging for machine learning techniques, especially when prediction targets are outside the range of training data. Conceptual hydrological models can reduce rainfall-runoff modelling errors with efficient quasi-physical mechanisms. The Monotone Composite Quantile Regression Neural Network (MCQRNN) is used for the first time to make probability density forecasts of flood processes and serves as a benchmark model, whereas it confronts the drawbacks of overfitting and biasedprediction. Here we propose an integrated model (i.e. XAJ-MCQRNN) that incorporates Xinanjiang conceptual model (XAJ) and MCQRNN to overcome the phenomena of error propagation and accumulation encountered in multi-step-ahead flood probability density forecasts. We consider flood forecasts as a function of rainfall factors and runoff data. The models are evaluated by long-term (2009-2015) 3-hour streamflow series of the Jianxi River catchment in China and rainfall products of the European Centre for Medium-Range Weather Forecasts. Results demonstrated that the proposed XAJ-MCQRNN model can not only outperform the MCQRNN model but also prominently enhance the accuracy and reliability of multi-step-ahead probability density forecasts of flood process. Regarding short-term forecasts in testing stages at four horizons, the XAJ-MCQRNN model achieved higher Nash-Sutcliffe Efficiency but lower Root Mean Square Error values, while improving Coverage Ratio and Relative Bandwidth values in comparison to the MCQRNN model. Consequently, the improvement can benefit the mitigation of the impacts associated with uncertainties of extreme flood and rainfall events as well as promote the accuracy and reliability of flood forecasting and early warning.

Highlights

- Machine learning assists hybrid model to promote flood forecasting and early warning
- Hybridizing MCQRNN with XAJ model for flood probability density forecasting
- XAJ-MCQRNN conquers overfitting and biased-prediction bottlenecks
- XAJ-MCQRNN improves accuracy and reliability of flood probability density forecasts

Credit Author Statement

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Declaration of interests

 \boxtimes The authors declare that they have no known competing financial interests or personal relationships that could have appeared to influence the work reported in this paper.

□The authors declare the following financial interests/personal relationships which may be considered as potential competing interests: